Hyper-Kamiokande and proton decay

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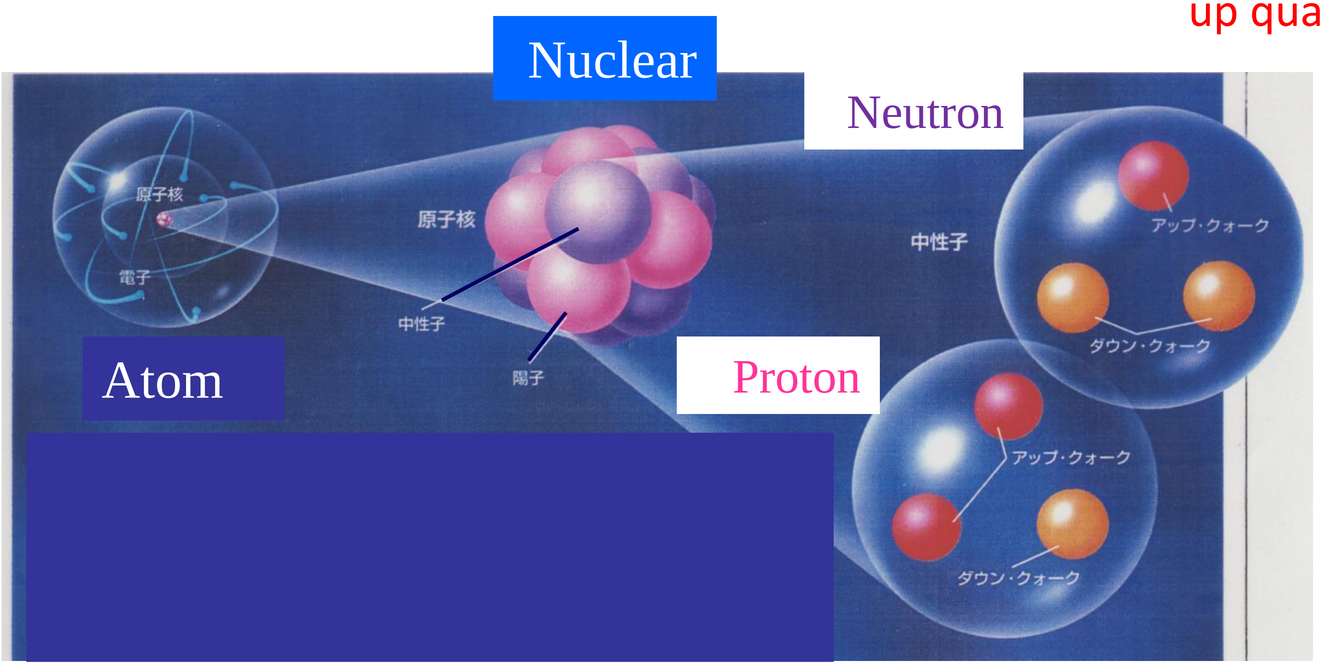
1. Does Proton Decay ?

- Nucleus consists of protons and neutrons.

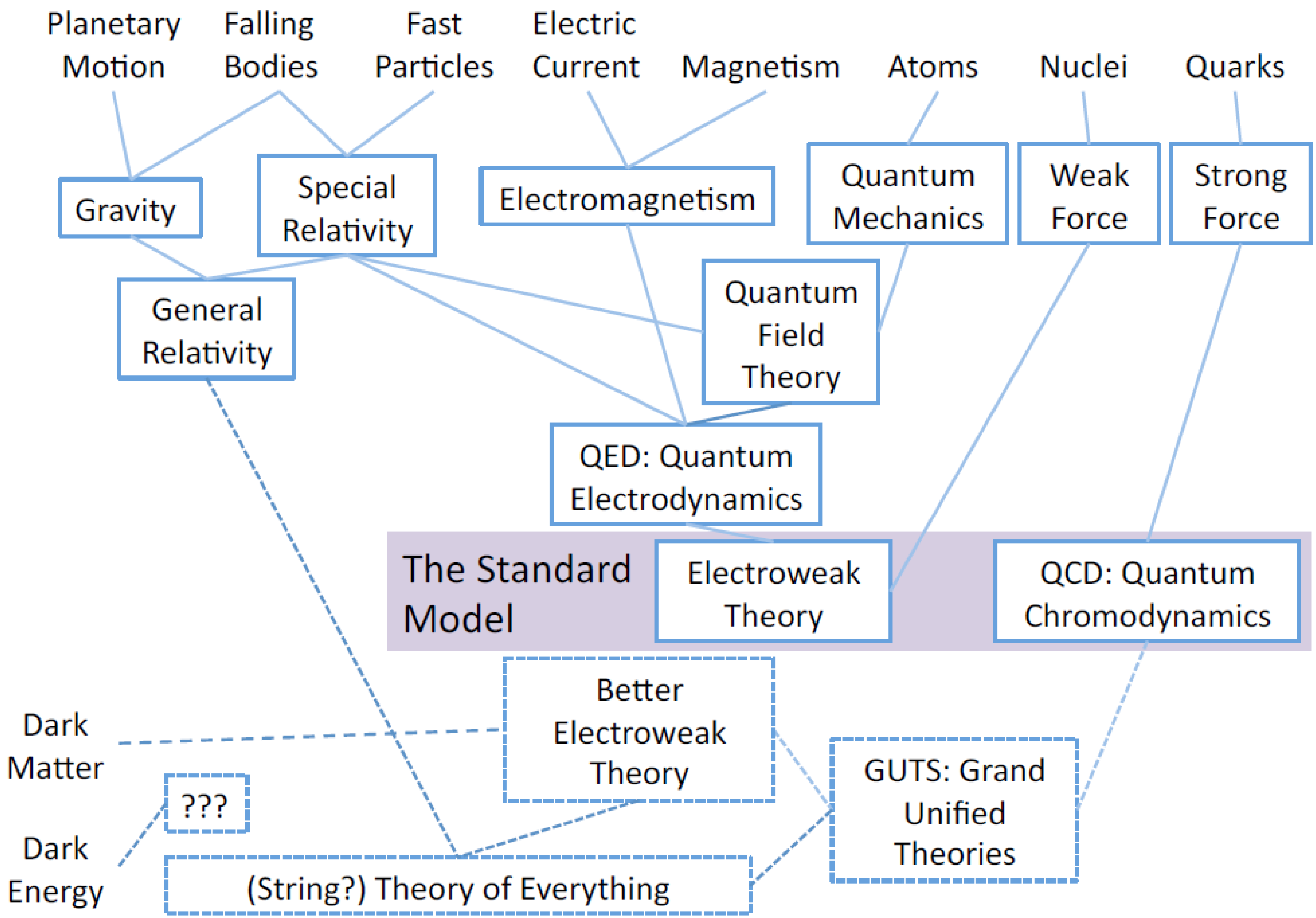


up quark

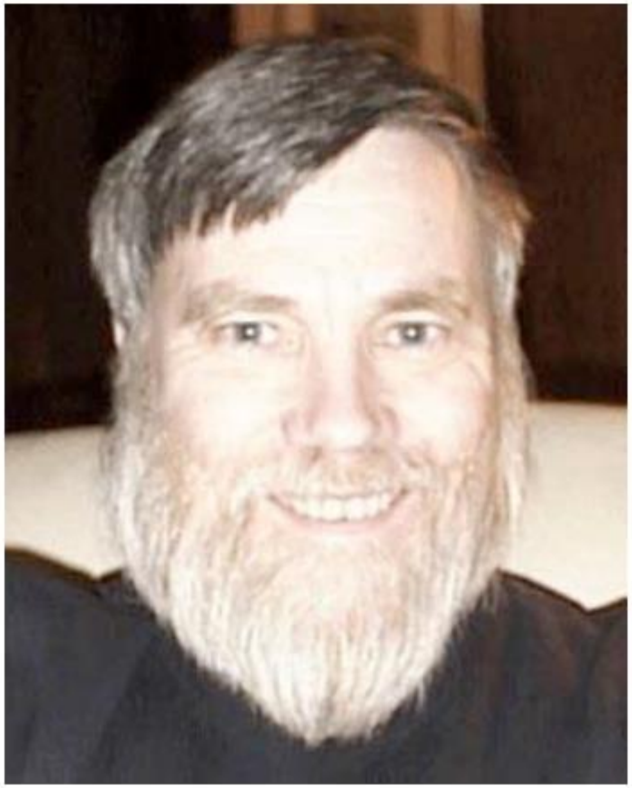
down quark

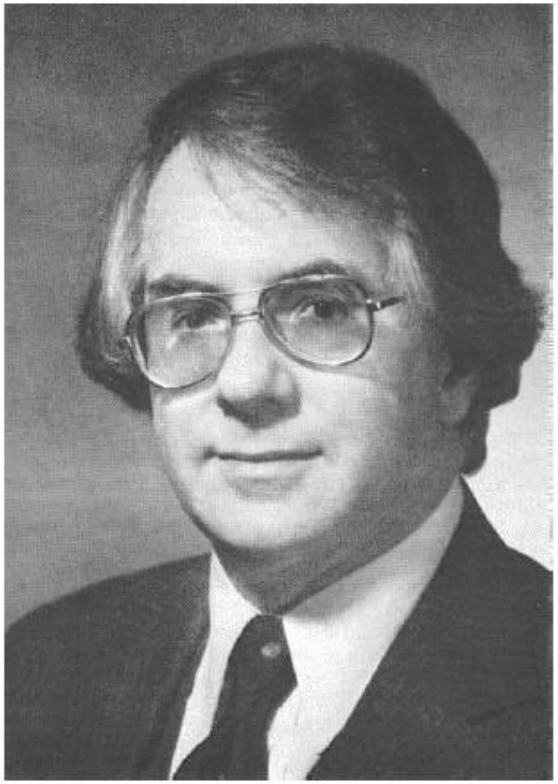
- It is well known that neutron decays spontaneously as β-decay: n → $p+e^{-}+\overline{\nu_e}$
  - Note that $M_n > M_p$.
- People thought proton is stable because of baryon number conservation.
  - n,p has baryon number 1.
  - We have never observed phenomena with baryon number violation.
  - Proton is the lightest baryon in the world.
  - 1929: Weyl suggests absolute stability of proton
- But is it really true ?

Can we explain everything by a single theory ?



SU(5) by Georgi and Glashow (1974)





Grand Unified Theories

Assume SU(3)⊗SU(2)⊗U(1) is part of a larger symmetry group

QCD

E.g. SU(5)

EW

$$\bar{5} = \begin{pmatrix} \bar{d}_g \\ \bar{d}_r \\ \bar{d}_b \\ e^- \\ -\nu_e \end{pmatrix}_L \qquad 10 = \begin{pmatrix} 0 & \bar{u}_b & -\bar{u}_r & -u_g & -d_g \\ & 0 & \bar{u}_g & -u_r & d_r \\ & & 0 & -u_b & -d_b \\ & & & 0 & -e^+ \\ & & & & 0 \end{pmatrix}_L$$

$$24 = \begin{pmatrix} G_{11} - \frac{2B}{\sqrt{30}} & G_{12} & G_{13} & \bar{X}_1 & \bar{Y}_1 \\ G_{21} & G_{22} - \frac{2B}{\sqrt{30}} & G_{23} & \bar{X}_2 & \bar{Y}_2 \\ G_{31} & G_{32} & G_{33} - \frac{2B}{\sqrt{30}} & \bar{X}_3 & \bar{Y}_3 \\ X_1 & X_2 & X_3 & \frac{W^3}{\sqrt{2}} + \frac{3B}{\sqrt{30}} & W^+ \\ Y_1 & Y_2 & Y_3 & W^- & -\frac{W^3}{\sqrt{2}} + \frac{3B}{\sqrt{30}} \end{pmatrix}$$

Transition between lepton and quark !

generators

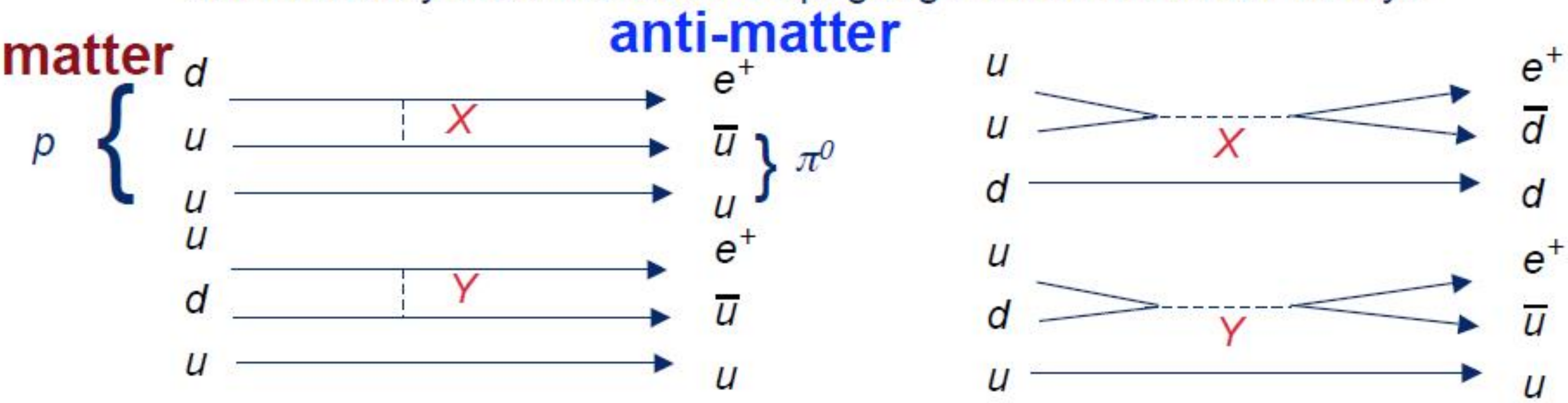
Consequences:

- Single (unified) coupling
- Charge quantization: $Q_d = Q_e/3$, $Q_u = -2Q_d$ ⇒ $Q_p = -Q_e$
- New gauge interactions (X, Y bosons) ⇒ proton decay

Proton Decay in SU(5) By Georgi and Glashow (1974)

- Decay mechanisms

dominated by the dimension=6 op. gauge boson mediated decays



($X^{\pm 4/3}$, $Y^{\pm 1/3}$: new gauge bosons)

- Predictions

$$\tau/B\,(p \rightarrow e^{+}\pi^{0}) = 4 \times 10^{29\pm 1.7}\ \text{years},\quad B\,(p \rightarrow e^{+}\pi^{0}) \approx 40 \sim 60\ \%$$

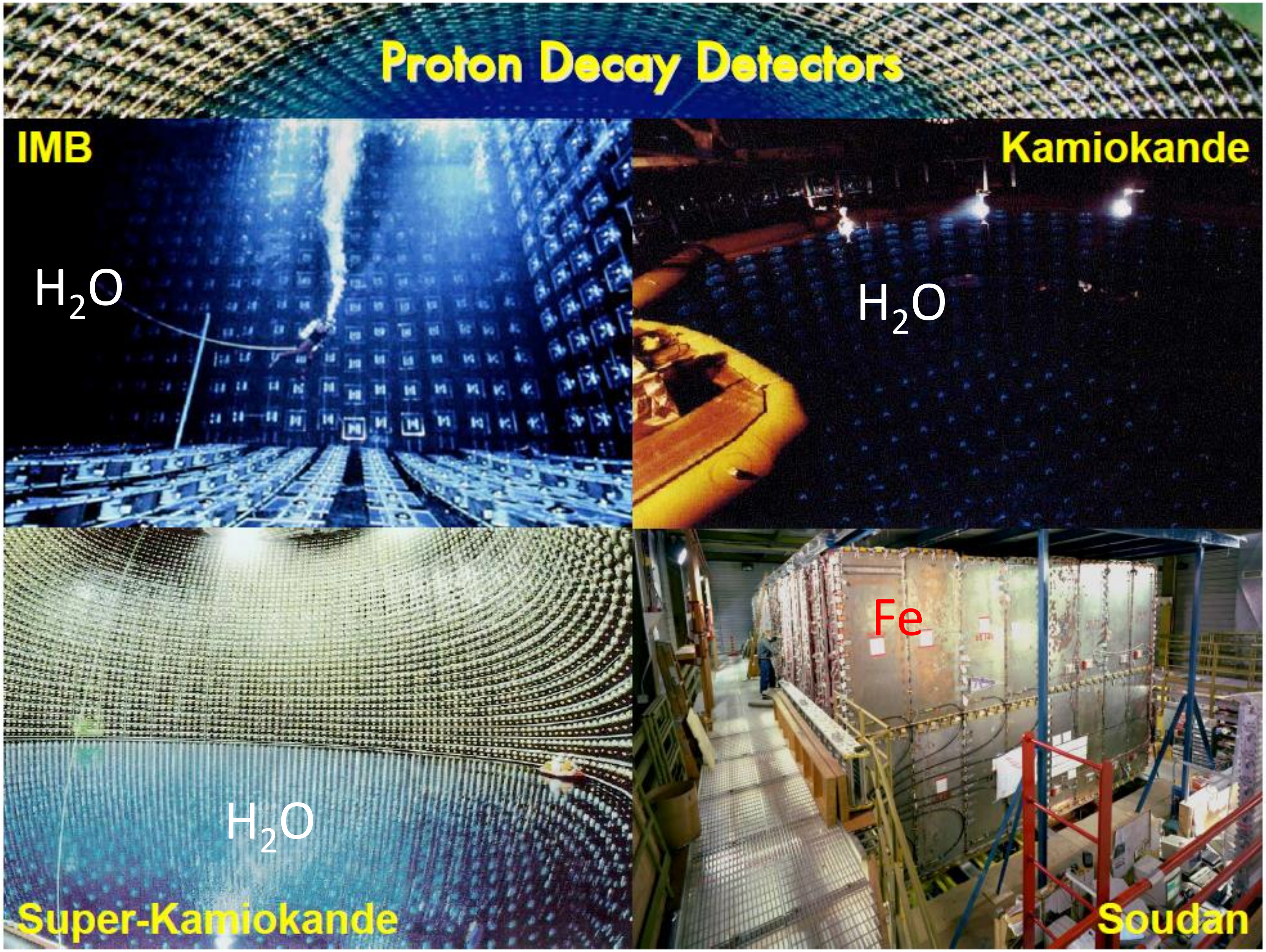
$p \rightarrow e^{+}\pi^{0}$ became the most famous and popular decay mode.

2. How to find proton decay

- Watch a proton for very long time (> 10^{30} years).
  - Age of the universe: ~ 10^{10} years
  - Obviously impossible.

OR

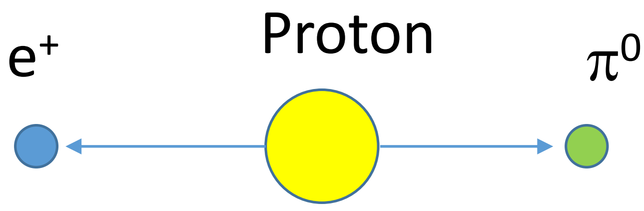
- Watch many protons for (relatively) short time.
  - Lifetime τ: $N(t)=N(t=0)\exp(-t/\tau)$
  - Need huge detector !



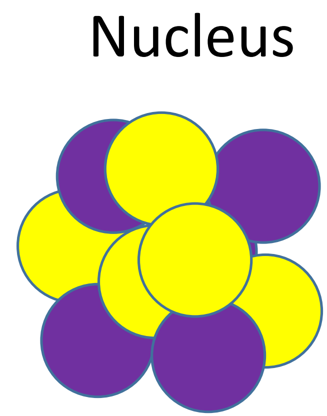
Higher sensitivity in Water Cherenkov Detectors

2. Dominant decay mode:
$p \rightarrow e^+\pi^0$

What's important for p→$e^+\pi^0$?



In "free" proton case, e^+ and π^0 emit in back-to-back. Energy corresponding to proton mass is fully used.

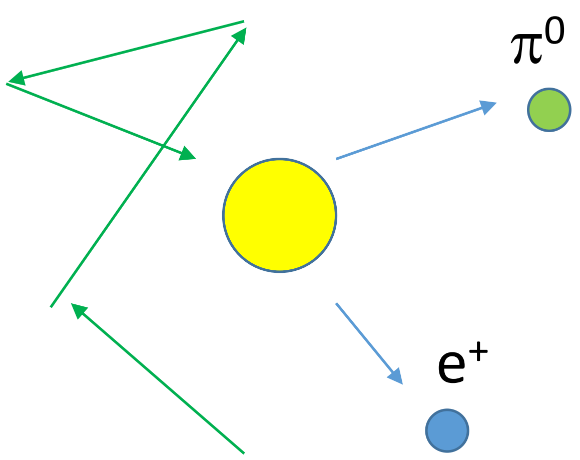


What happens if a bound proton in nucleus decays ?

Inefficiencies and uncertainties of proton decay search come from nuclear effect !

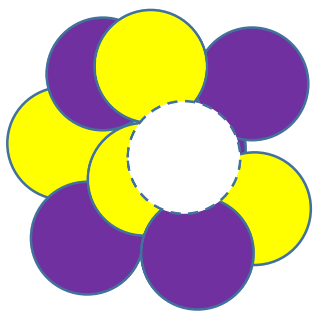
Key 1: Proton never stops in nucleus

- Protons don't exist locally in nucleus. It is always moving in the nuclear potential (Fermi motion, p_f ~ 225 MeV/c).



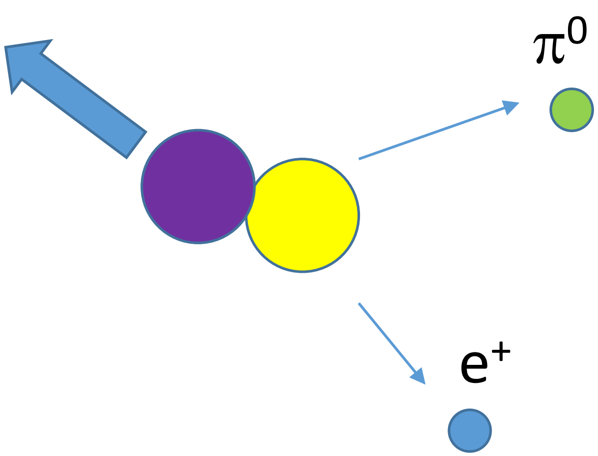
Key 2: Binding energy

- Energy corresponding proton mass should be used for compensating its binding energy (s-state: ~40 MeV, p-state:15 MeV in Oxygen).



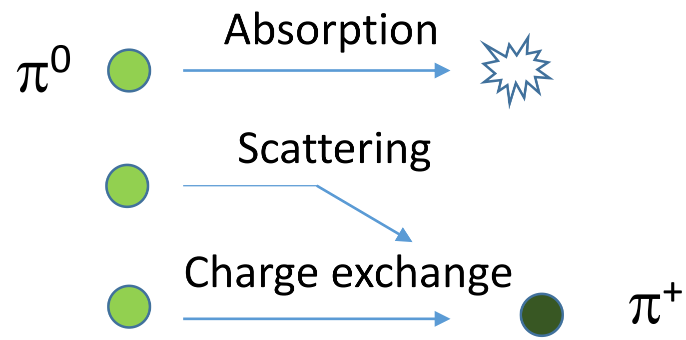
Key 3: Proton strongly binding to other nucleus

- ~ 20% protons are strongly binding to other nucleon which also bring energy when the proton decays (correlated decay)



Key 4: π interacts in nucleus

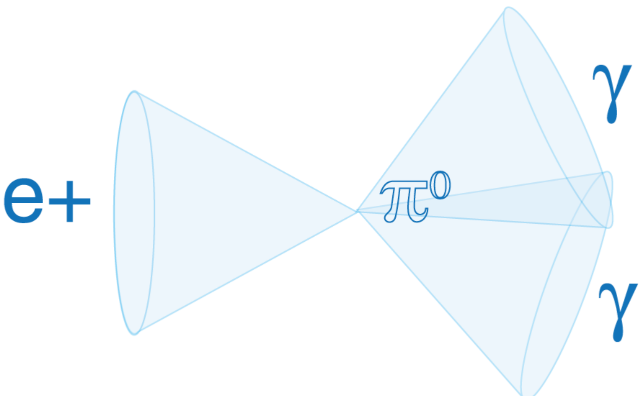
- Mesons (π,K, e.t.c.) in decay products are affected in nuclear interactions before exiting nucleus.



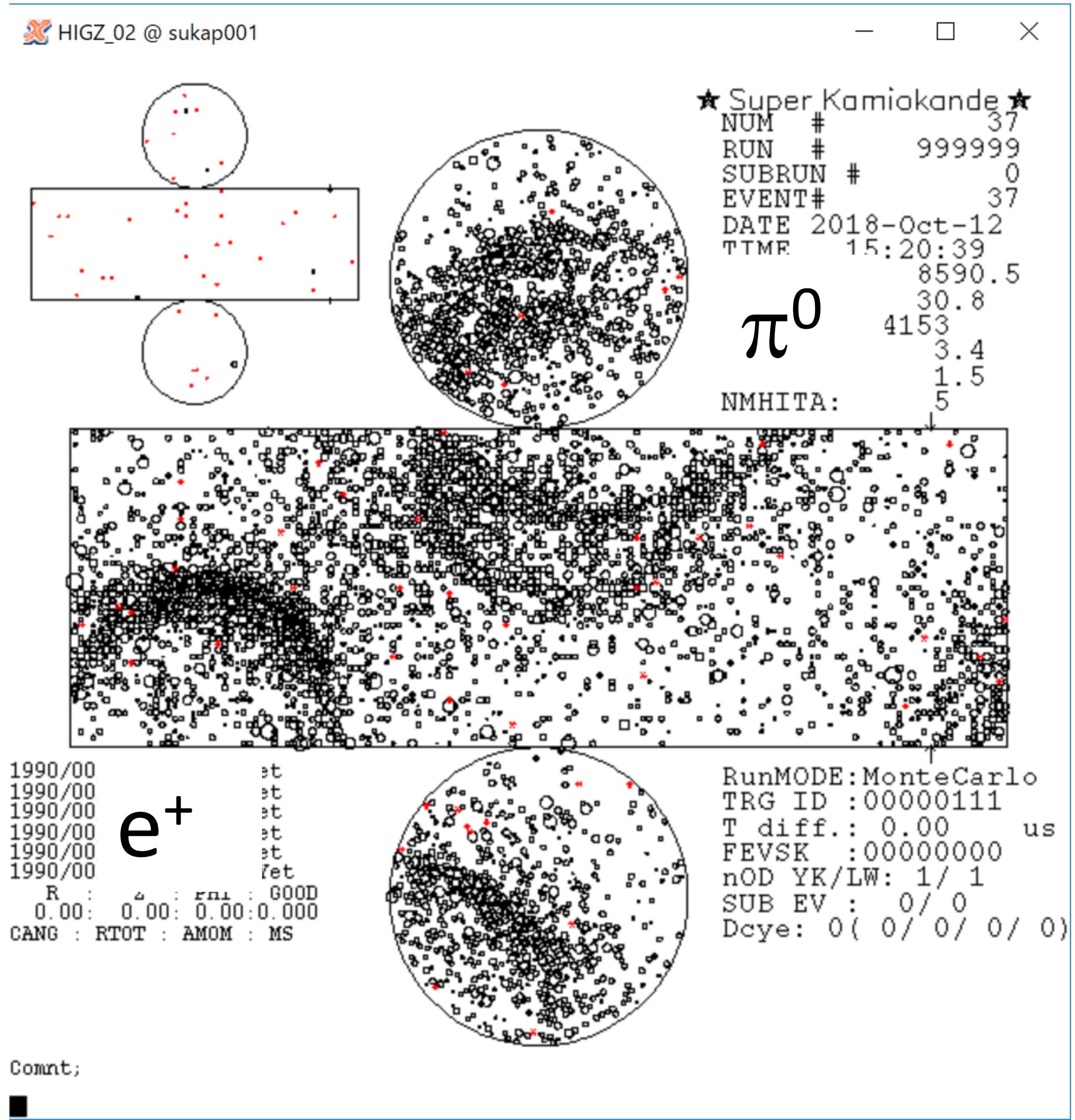
Why water is used for proton decay search ?

- Easy to construct larger detector.
  - Much cheaper than iron.
  - You can find large water tank everywhere (common technology).
- High efficiency and low uncertainty.
  - H_2O has two hydrogens which are not affected by nuclear effect . They are regarded as “free” proton.
    - ✓ Bound proton: ~ 200 MeV/c ~ 0.2c =6×10^7 m/s
    - ✓ velocity of molecular in liquid ~ 10^2 m/s
  - Free protons contribute high selection efficiency and low uncertainty.

How look like p→$e^+\pi^0$ in SK ?



Three e-like rings should be observed.



Stopped π^0 case

π^0

γ_1 ~~~~ ● ~~~~ γ_2

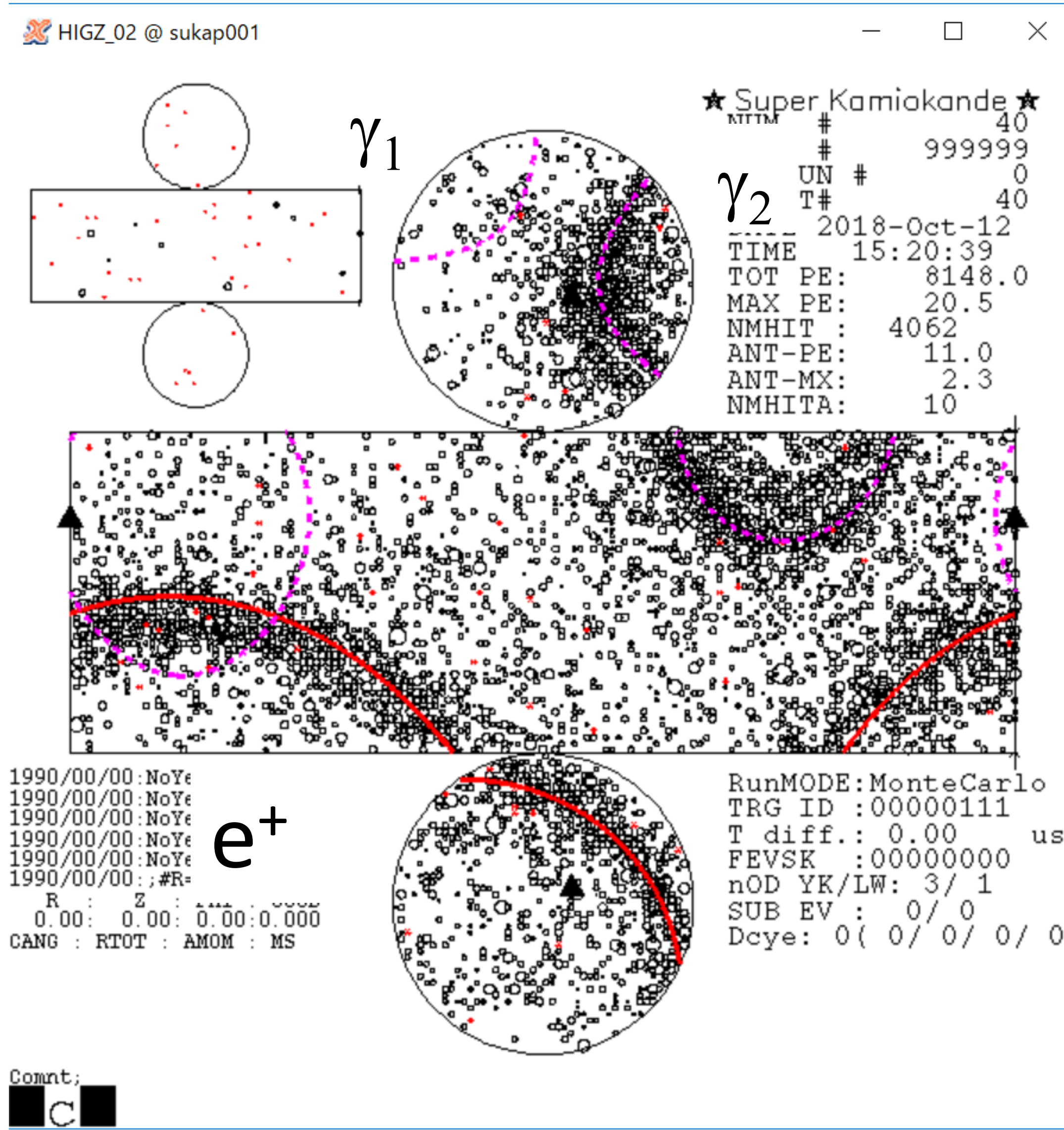
$E_1 = E_2$

If a γ is emitted π^0 direction

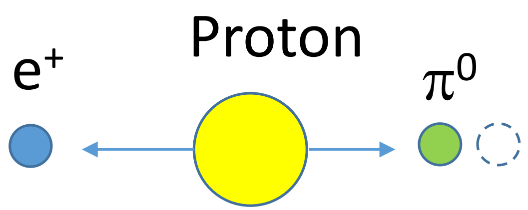
π^0

γ_1 ~~ ● ➡ ~~~~ γ_2

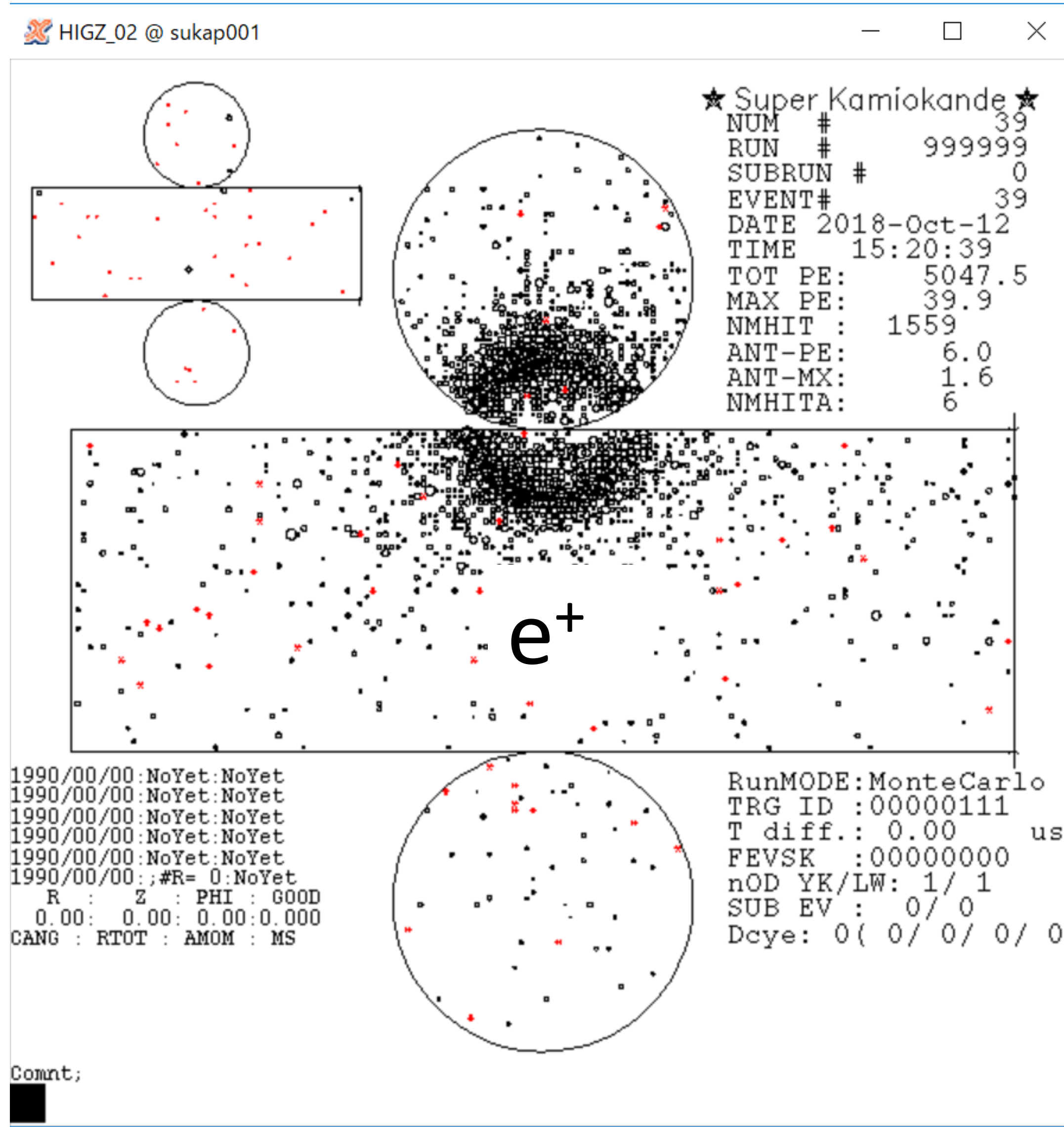
$E_1 < E_2$



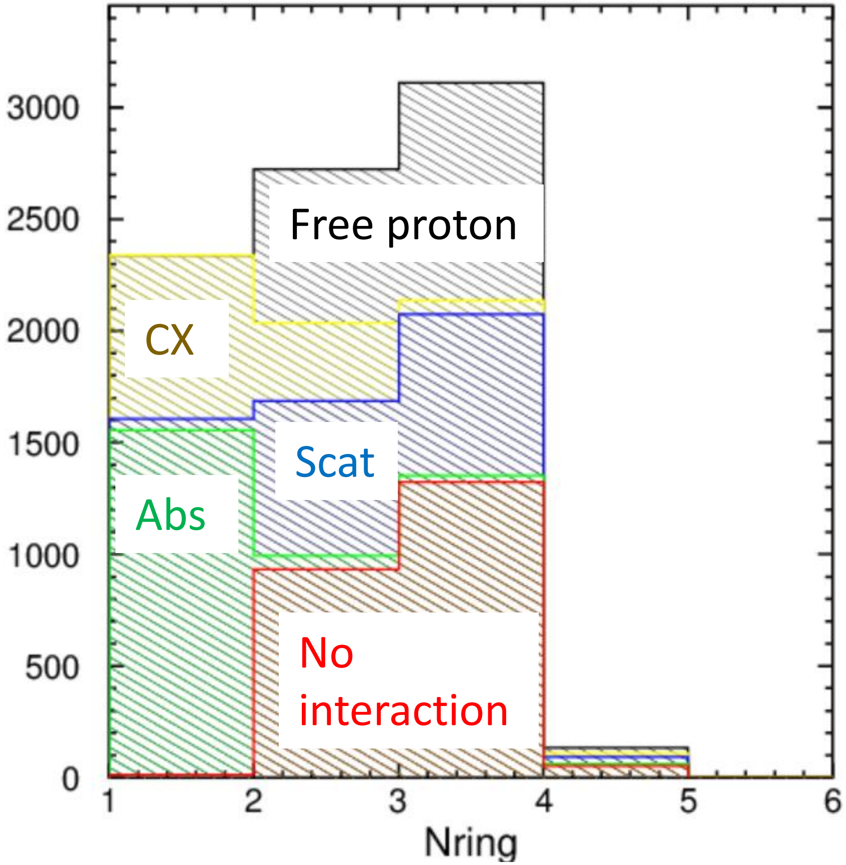
Sometimes one γ is failed to reconstruct and observed only two rings.



If π^0 is absorbed before exiting nucleus, only e^+ is observed (one ring).



Observed number of ring for $p \rightarrow e^+\pi^0$



Free proton: H in H_2O

No interaction in Nucleus

Abs: π^0 absorption in Nucleus

Scat: scattered

CX: charge exchange

($\pi^0 \rightarrow \pi^\pm$, below threshold)

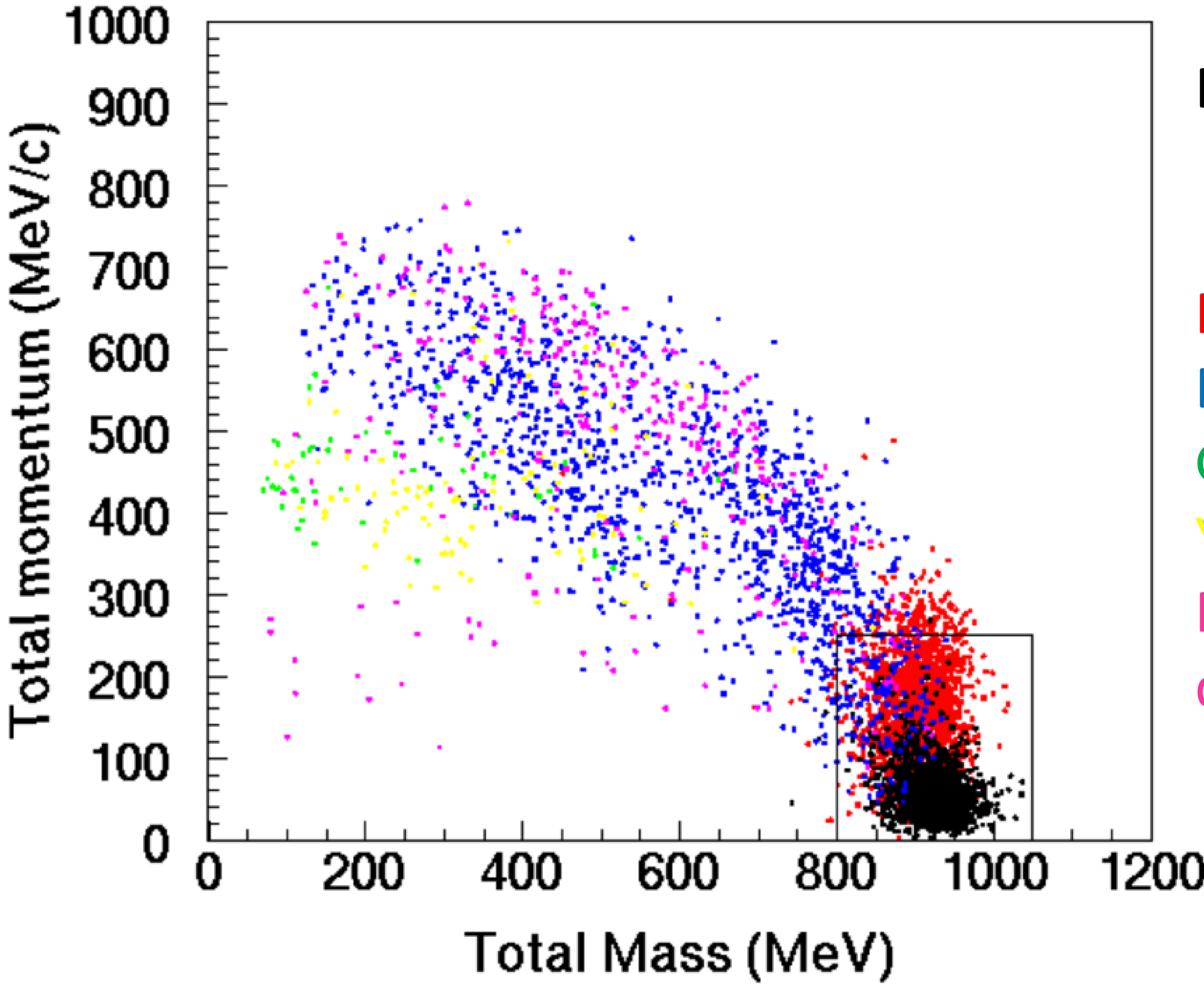
Choose 2 or 3 rings.

Selection criteria for $p \rightarrow e^+\pi^0$

1. Event vertex should be located 2 m inward from the tank wall (fiducial volume cut, 22.5kton).
2. 2 or 3 ring event.
3. All ring should be e-like (Particle IDentification).
4. No Michel electrons.
5. Reconstruct π^0 mass for 3 ring events. It should be $85 < M\pi^0 < 185$ MeV/c^2
6. Reconstruct total mass and momentum should be $800 < M_{tot} < 1050$ MeV/c^2, $P_{tot} < 250$ MeV/c.

Total mass vs Total momentum for p→$e^+\pi^0$

- Selection efficiency ~ 40 %
- Inefficiency is dominated by unavoidable physics processes.

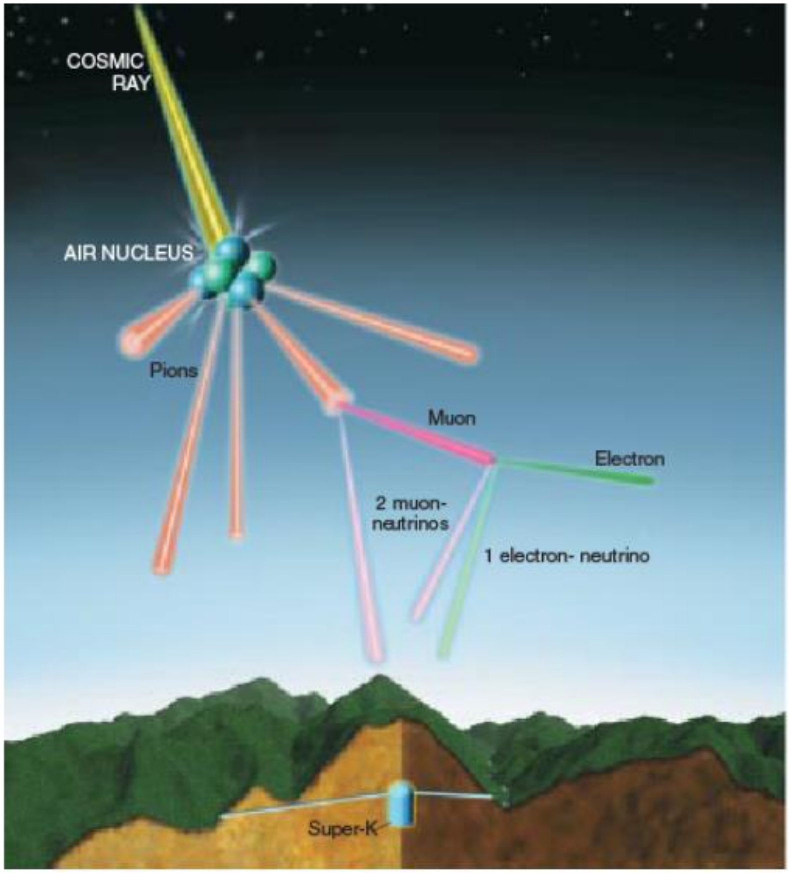


Black: Free proton

Bound proton
Red: No π interaction
Blue: π scatter
Green: π absorption
Yellow: π CX
Purple: Correlated decay

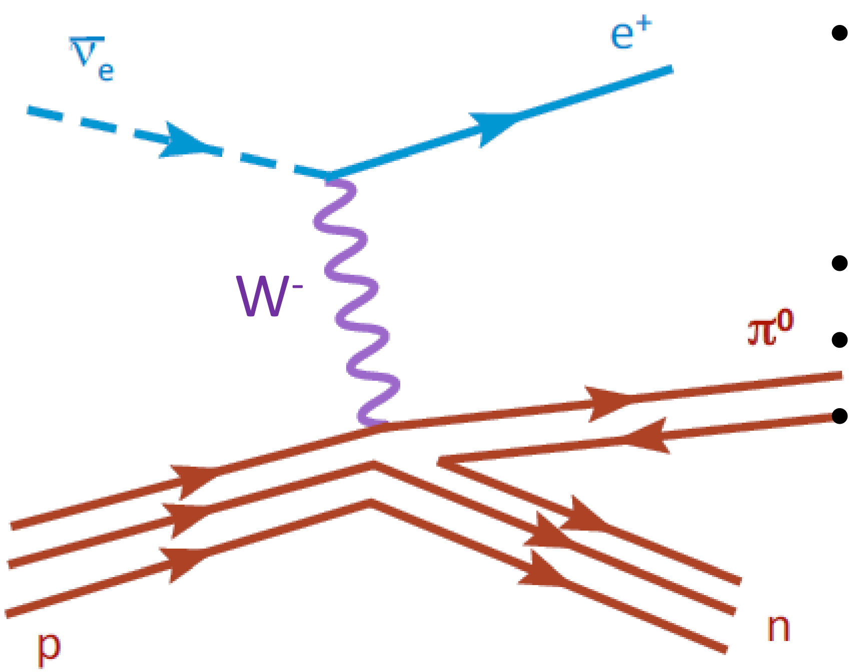
2-2. What's Background events for proton decay searches ?

- Atmospheric neutrino is dominant backgrounds for proton decay searches.
    - ➢ Visible energy ~ 1 GeV.
    - ➢ Solar or SN ν is too low energy.
    - ➢ Cosmic ray μ are rejected by outer detector.



Typical background for p→$e^+\pi^0$

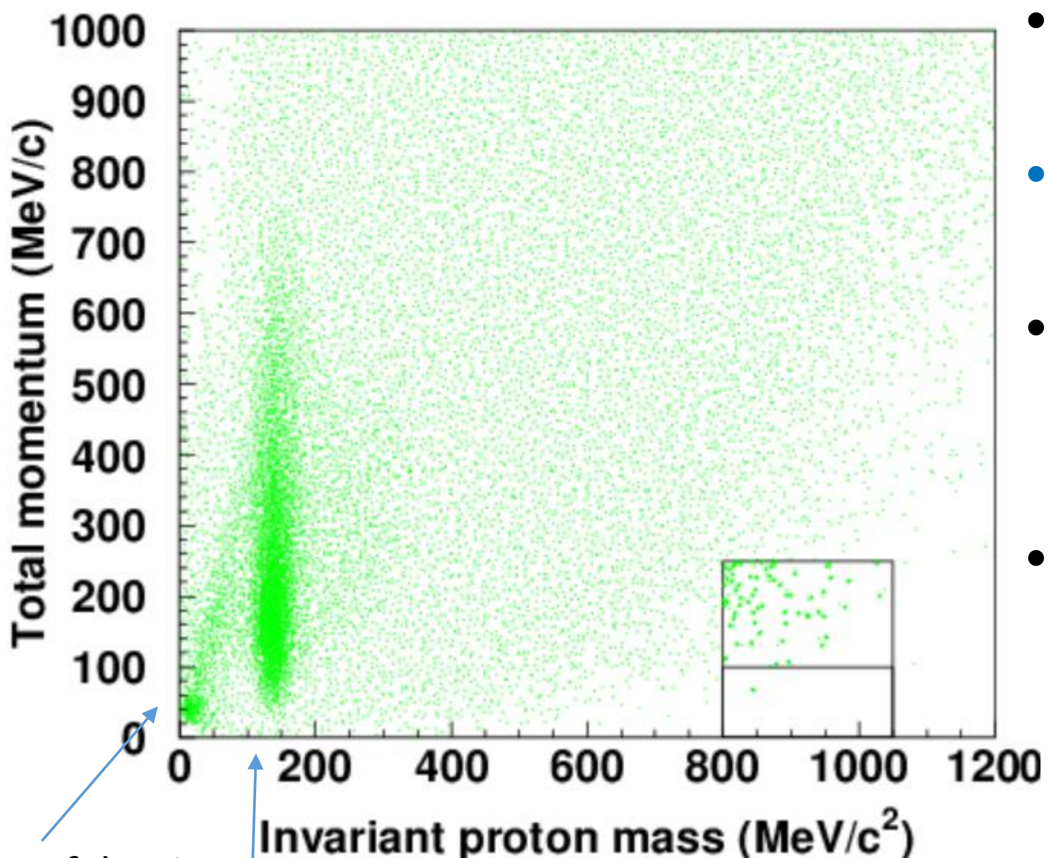
Charged current π^0 production



- Exchange W boson between ν and proton (charged current interaction).
- ν changes to e^+.
- π^0 and neutron are produced.
- Because neutron doesn't emit Chrenkov light, visible particles after the reaction are same as p→$e^+\pi^0$

Total mass vs Total momentum for atmospheric ν background MC

(After all cuts except for total mass and momentum)

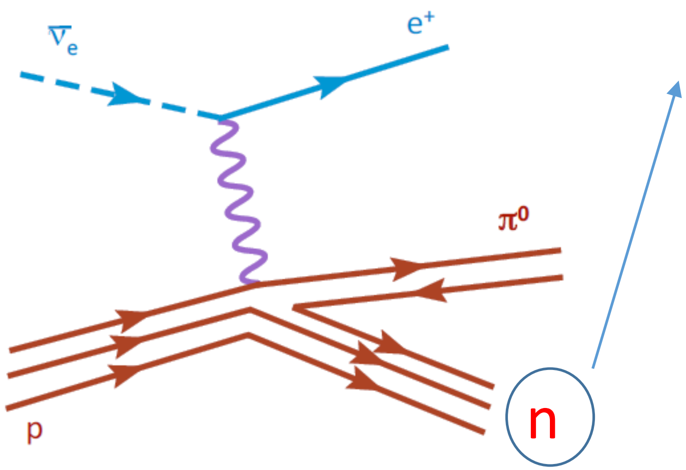


Due to fake ring

π^0 due to 2Re+e is allowed.

- Generate huge atm.n MC, 2000 year of SK!
- Expected BG:
  ~1.3 ev/Mton*yr
- Neutrino events tend to have higher total momentum.
- Almost background free in lower momentum region (<100 MeV/c).
  - ➢ The region corresponds to free proton decay.

Further background reduction

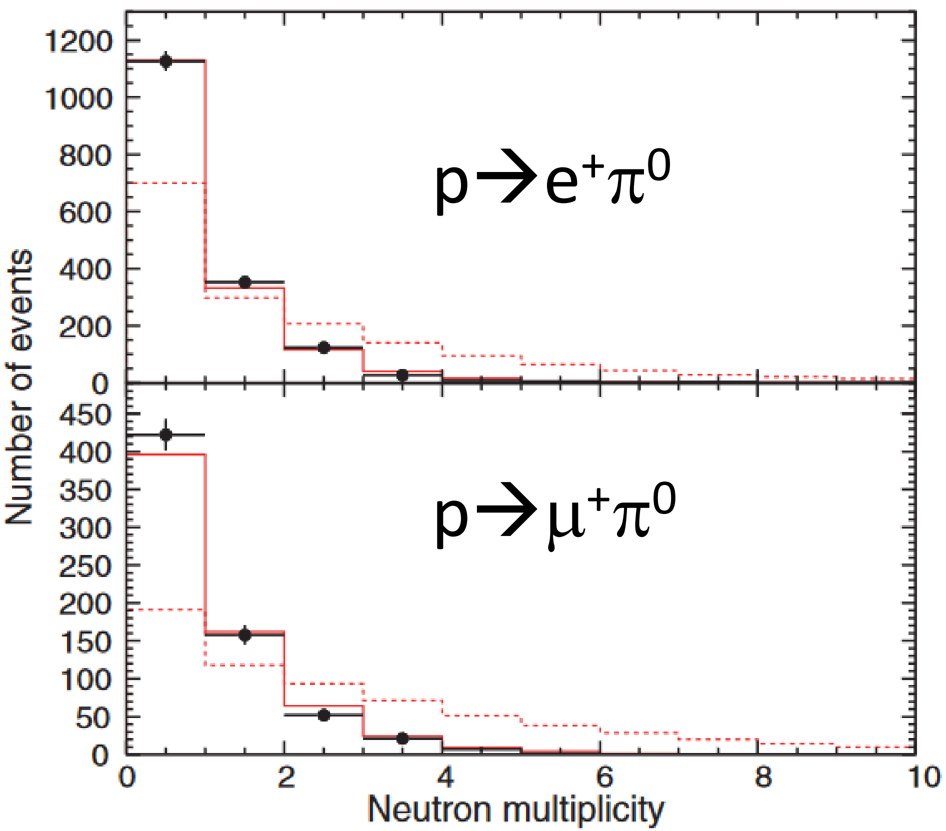


- Neutron doesn't emit Chrenkov light.
- However, neutron is thermalized in water and finally captured by hydrogen (~200 μs);

$$n + p \rightarrow d + \gamma \ (2.2\ \text{MeV})$$

- If we can detect delayed 2.2 MeV γ ray, we can reduce background more.
- Neutron capture is also important for SN Relic ν and separate ν and ν-bar interactions in atmospheric n oscillation analysis.

How powerful to reject background

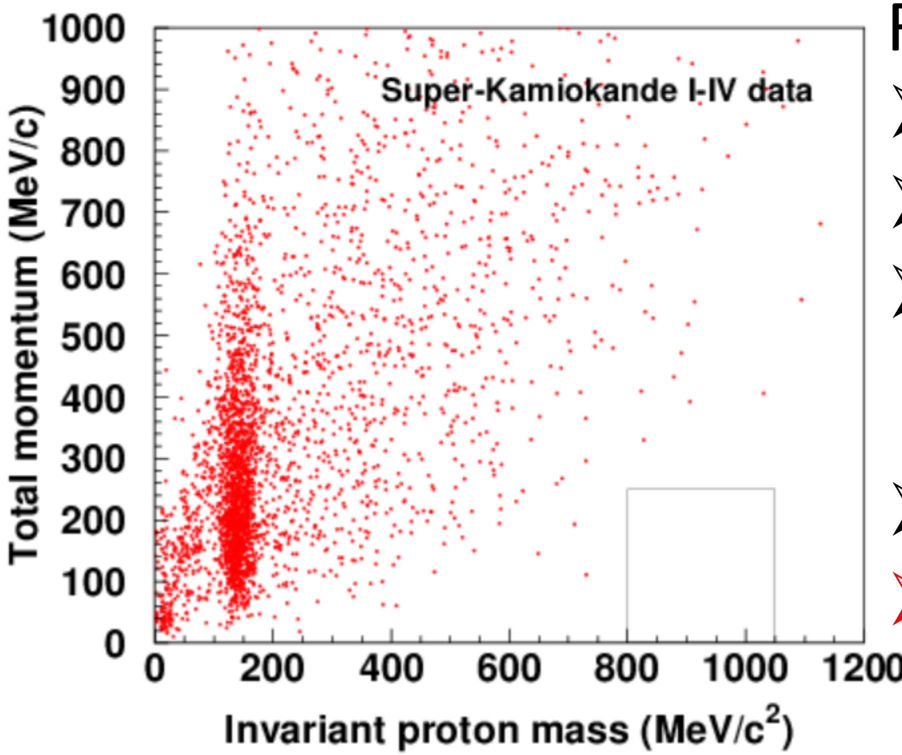


- Sample: out of signal box in M_{tot} vs P_{tot} plot.
  - Dot: data,
  - Histogram: Atm.ν MC

    (solid: reconstructed, dash: true)
- ~ 50 % background events are rejected with neutron=0.
- On the other hand, ~ 7.5 % of $p \rightarrow e^+\pi^0$ are accompanied with neutron from deexcitation of nucleus. Neutron tagging reduces a few % in selection efficiency.

2-3. SK result (so far)

- We have not find any evidences of nucleon decays !



Result of $p \rightarrow e^{+}\pi^{0}$

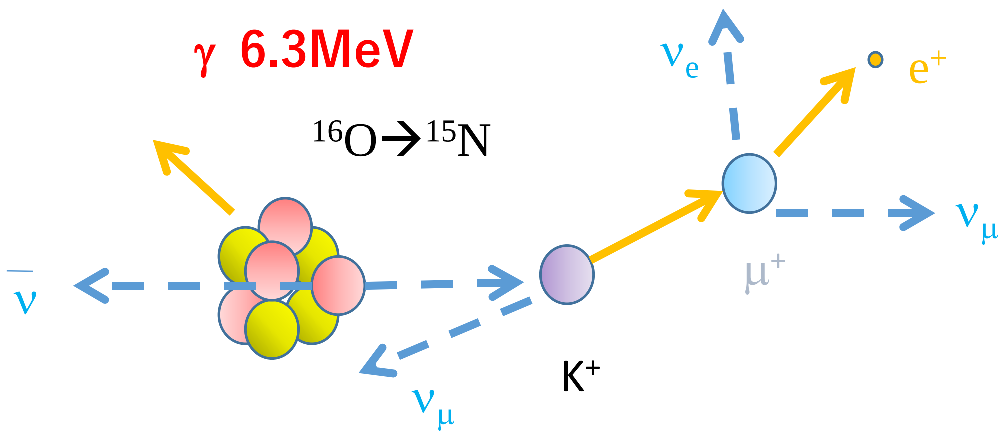
- ➢ Exposure: 450 kton・year
- ➢ Efficiency: 38.6 % (SK-IV)
- ➢ Expected BG: 0.63 events
  - 0.05 evetns in P_{tot} <100MeV/c
  - 0.58 events in 100 ~ 250 MeV/c
- ➢ Observed: 0 event
- ➢ Lower limit of proton life time: > 2.4×10^{34} years

3. SUSY favored decay mode: $p \rightarrow \nu K^+$

3-1 How to find $p \rightarrow \nu K^+$ in Water Cherenkov detector

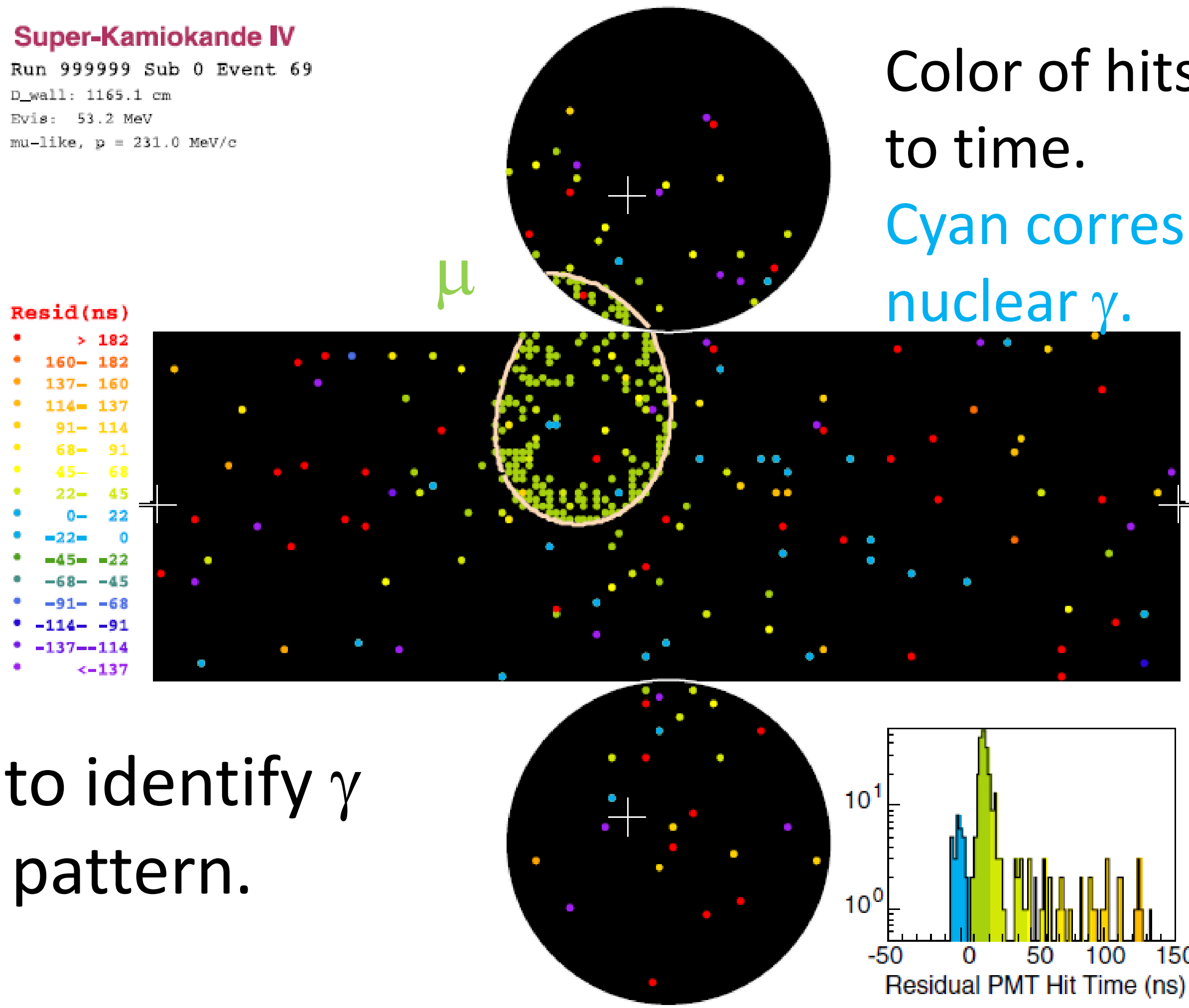
- K^+ has low momentum, most of them stop in water and decay with 12 nsec lifetime.
- Major K^+ decay mode
  - $K^+ \rightarrow \nu\mu^+$: 64 %
  - $K^+ \rightarrow \pi^+\pi^0$: 21 %
- "Stopping K^+" means two body decay products of K^+ should have monochromatic momentum as seen in the previous question !
  - $K^+ \rightarrow \nu\mu^+$: 236 MeV/c
  - $K^+ \rightarrow \pi^+\pi^0$: 206 MeV/c
- Using this property, Water Cherenkov detector can search for $p \rightarrow \nu K^+$.

3-2. Search for $p \rightarrow \nu K^+$, $K^+ \rightarrow \nu \mu^+$



- Visible particle is only μ^+ with Michel electron.
- Search for data excess around 236 MeV/c of μ comparing with atmospheric ν MC.
- After proton decay, 40 % of remaining nucleus emits 6 MeV γ for deexcitation. It is useful to reduce background.

Example of p→νK$^+$, K$^+$→νμ$^+$ with γ

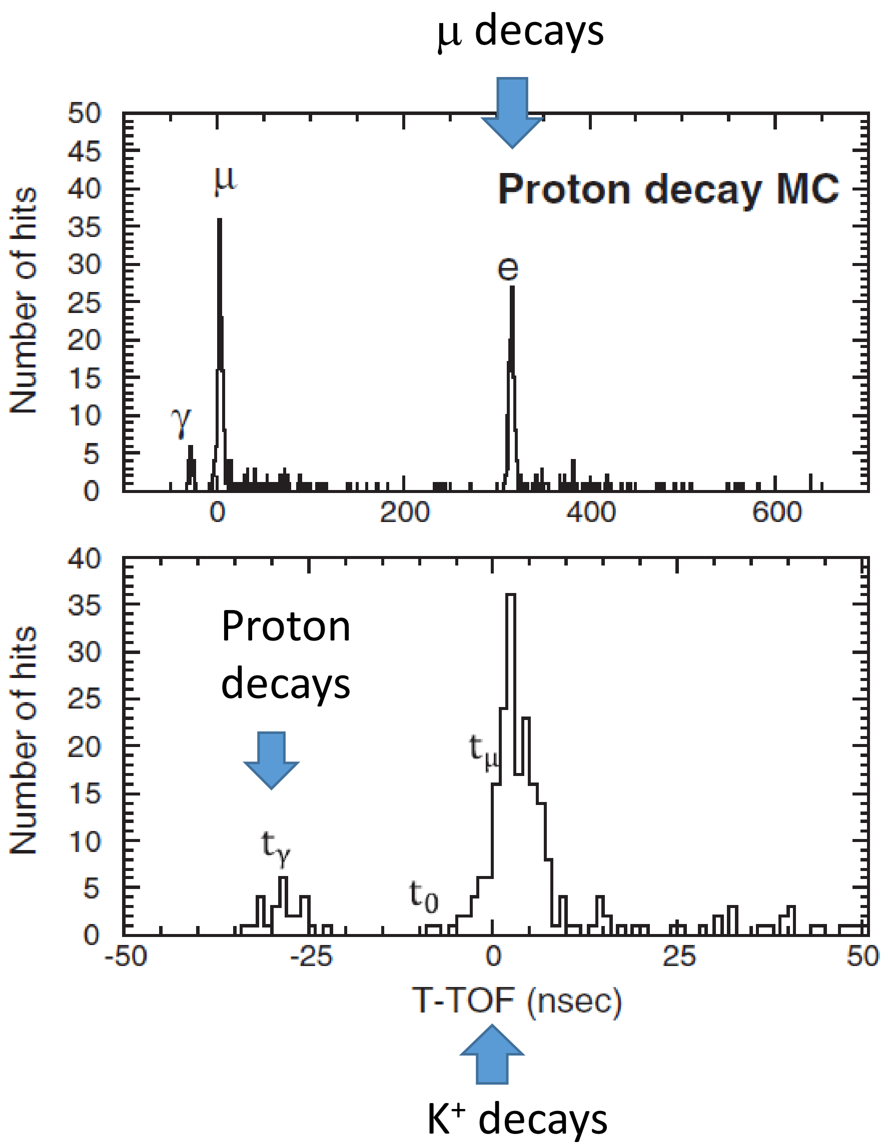


Color of hits corresponds to time.

Cyan corresponds to nuclear γ.

Difficult to identify γ from hit pattern.

Time structure with nuclear γ



- 3 hit clusters in time should be observed in case of signal.
- The event is triggered by μ hits.
- γ signal is much smaller than μ and easily hidden by tail of μ hits.
- Make 12 nsec time window and slide it toward left from t_0 (end of μ tail) to search for maximum hit cluster.

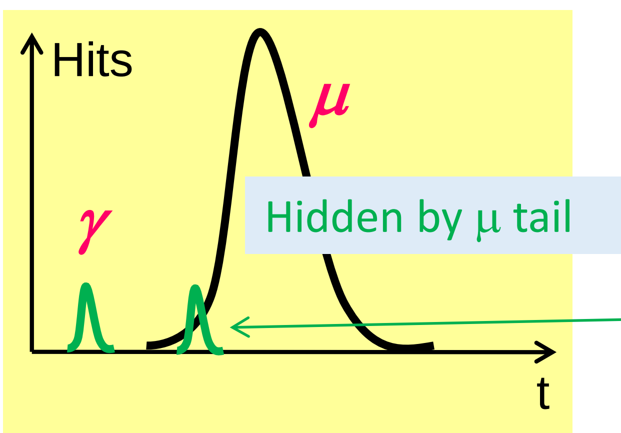
Selection criteria for $p \rightarrow \nu K^+$, $K^+ \rightarrow \nu \mu^+$

- 1 μ-like ring with Michel electron
- $215 < P\mu < 260$ MeV/c
- Proton rejection cuts
- Search Max hit cluster ⇦ Reduce background by 5×10^{-4} !

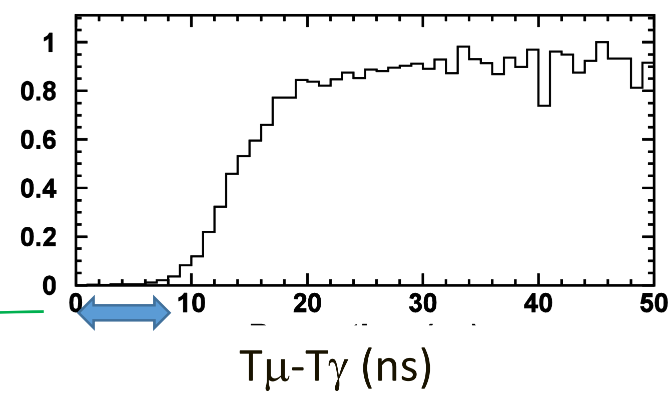
  by sliding time window (12ns width);
  - $4 < N\gamma < 30$ hits
  - $T_\mu - T_\gamma < 75$ nsec
- No neutron
- Selection efficiency = (selected events)/(proton decay in fiducial volume): 9 %
  - $Br(K^+ \rightarrow \nu \mu^+) = 64$ %, only 40 % emits nuclear γ ➔ 26 % even if detector is perfect.

Remark for this analysis

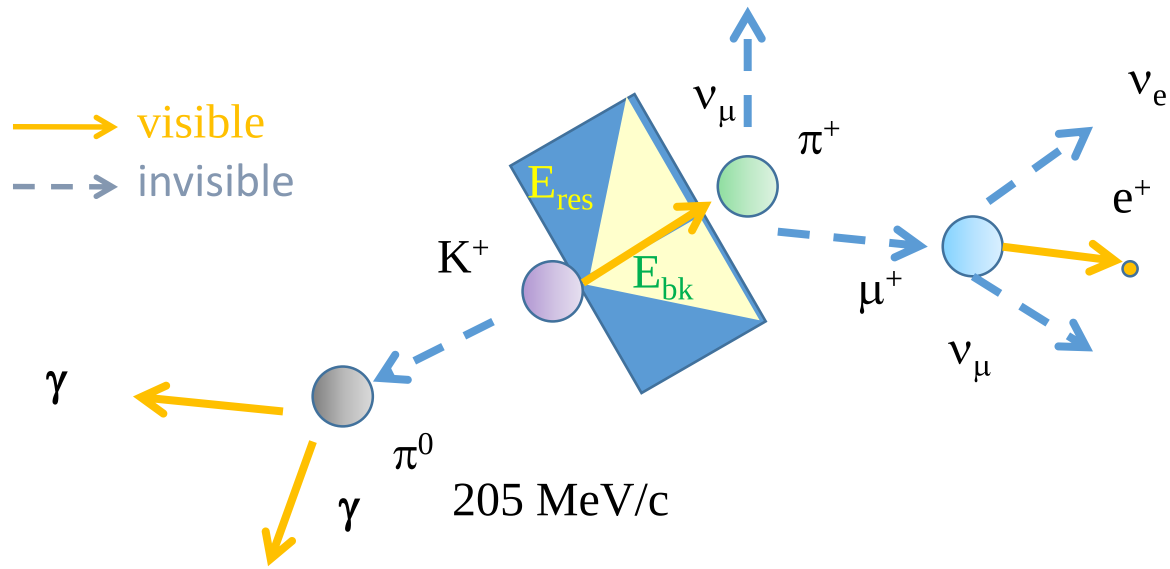
- This analysis is limited by time resolution of PMTs.
  - If γ is close to μ, γ peak is hidden by μ hits.
  - Time resolution of SK PMT is 2.2 nsec at 1 photoelectron.
  - If μ peak becomes sharper, the selection efficiency will be improved.



γ tagging efficiency

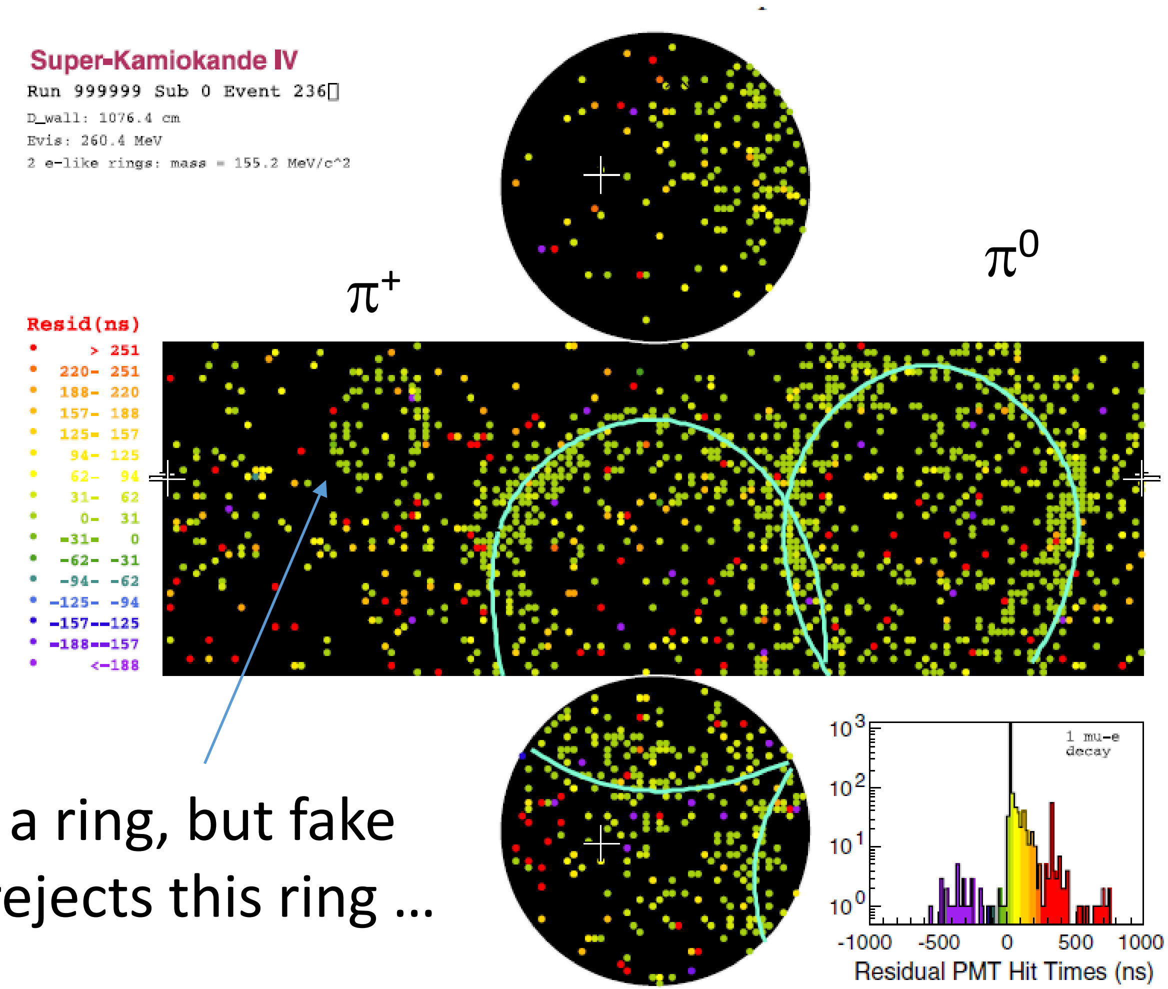


3-3. Search for p→νK$^+$, K$^+$→$\pi^+\pi^0$



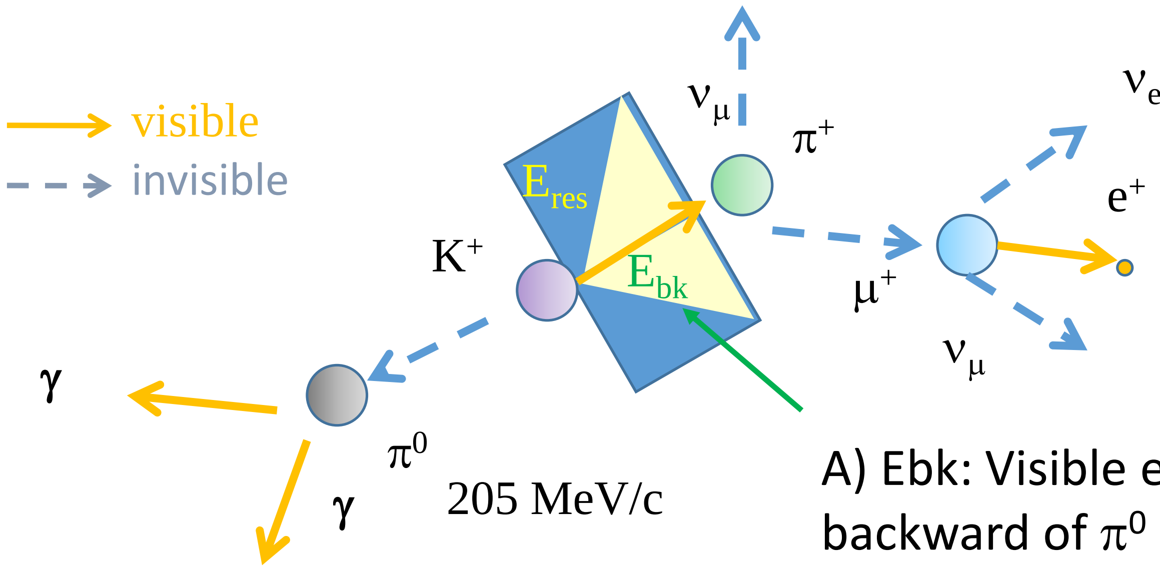
- Both π^+ and π^0 has 205 MeV/c in momentum. This is just above Cherenkov threshold for π^+, thus it is not identified as a ring in most of case.
- π^+ decays into μ (invisible) and ν, μ decays into e$\nu_e\nu_\mu$.
- π^0 decays into 2 γs.
- Search for 206 MeV/c π^0 with Michel electron.

Example of p→νK$^+$, K$^+$→$\pi^+\pi^0$



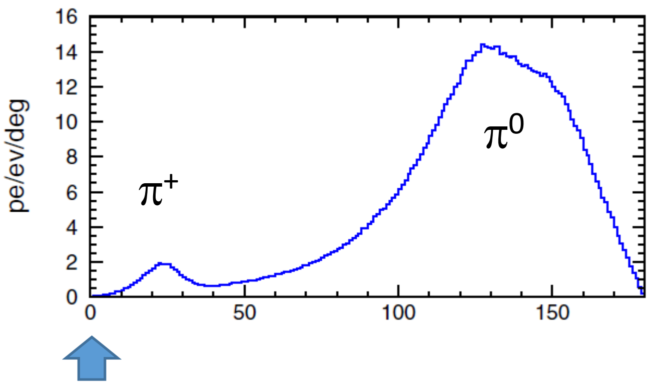
Look like a ring, but fake ring cut rejects this ring …

Use π^+ information to select events



A) Ebk: Visible energy sum in backward of π^0 direction (140°-180°)

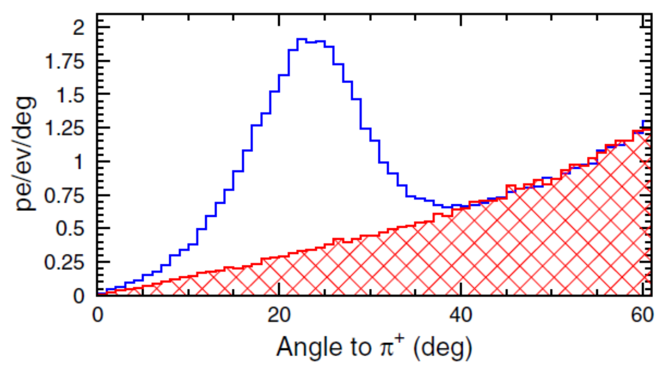
Charge distribution



π^+ direction

Zoom

B) Make likelihood for hit pattern.



Selection criteria for $p \rightarrow \nu K^+$, $K^+ \rightarrow \pi^+\pi^0$

- 1 or 2 e-like rings with decay-e.
- $85 < M\pi^0 < 185$ MeV.
- $175 < P\pi^0 < 250$ MeV/c.
- E_{bk}: visible energy sum in 140-180 deg. of π^0 dir,
  E_{res}: in 90-140 deg,
  L_{shape}: Likelihood based on charge profile
  $10 < E_{bk} < 50$ MeV
  $E_{res} < 12$ MeV (20 MeV for 1ring)
  $L_{shape} > 2.0$ (3.0 for 1ring)
- No neutrons
- Selection efficiency: 10 % ($Br(K^+ \rightarrow \pi^+\pi^0)$=21 %)

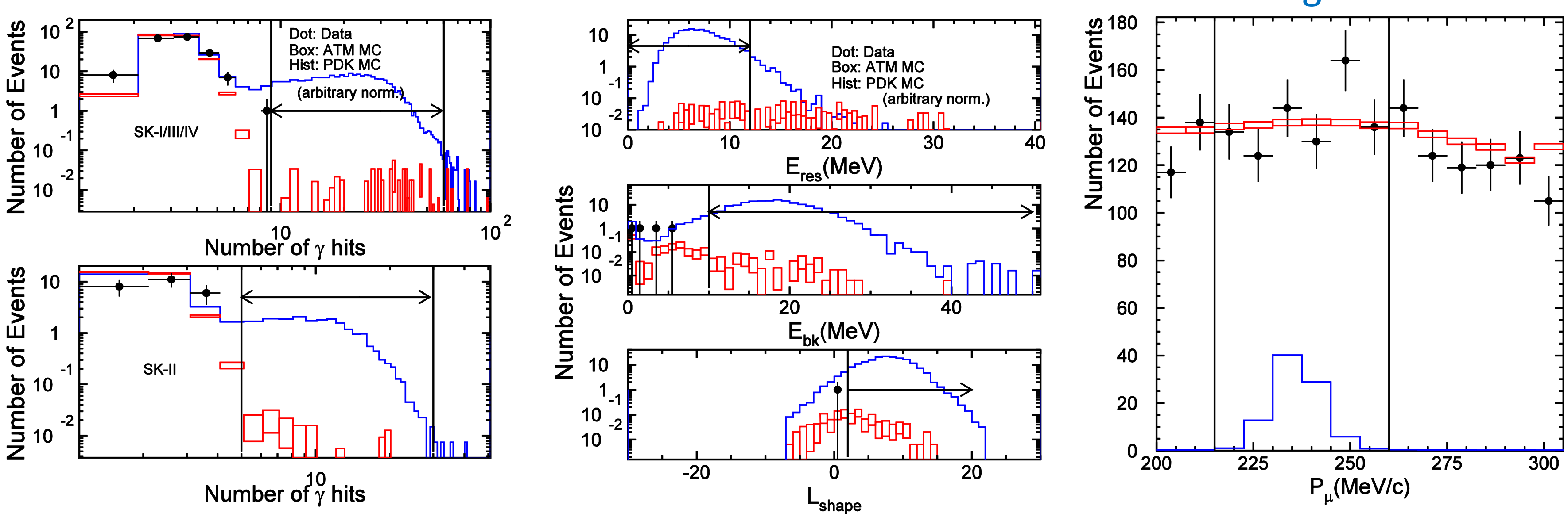
Background for $p \rightarrow \nu K^+$

- Dominant background is K^+ production by neutrino interactions.
  - $\nu p \rightarrow \nu \Lambda K^+$, $\Lambda \rightarrow p \pi^-$ (BR:64 %, mostly invisible in WCD)
  - Emit nuclear γ as same as the signal.
- It is also rare interaction and we had poor information from very old bubble chamber. Large uncertainty.
- Recently MINERvA measures K^+ production. It is very useful information for this analysis.

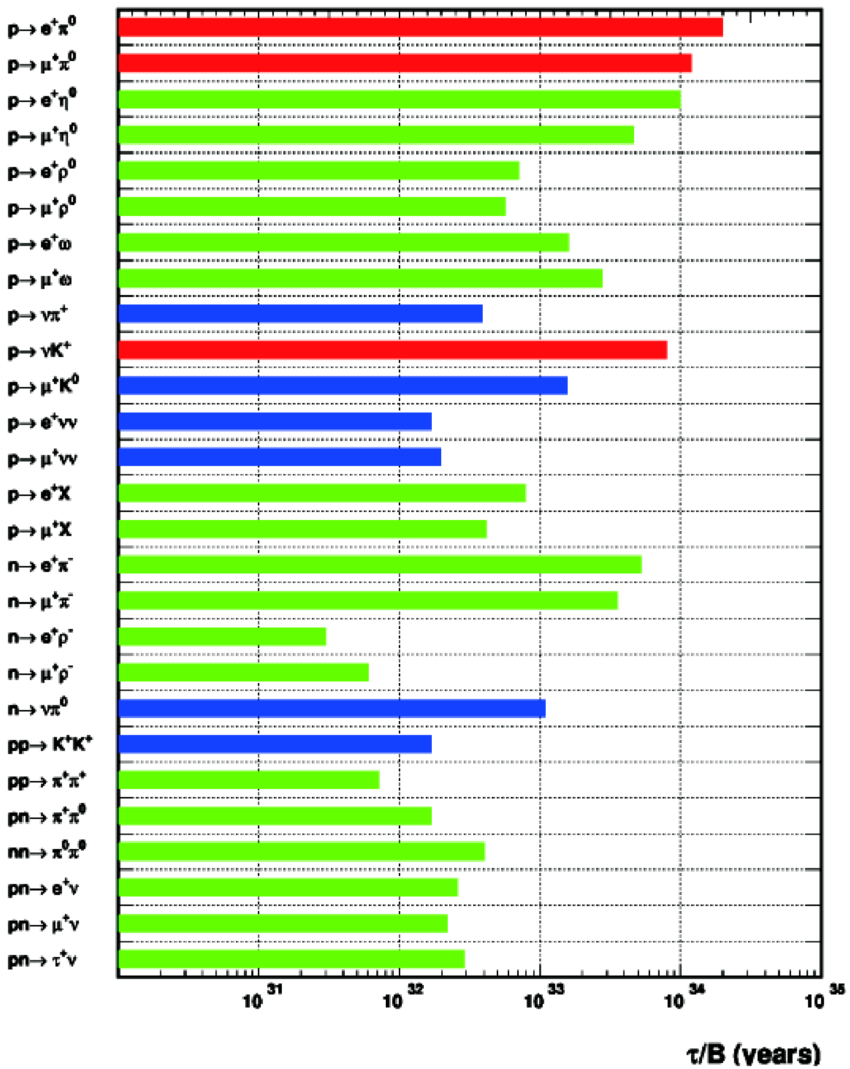
3-4. SK results (So far)

- Exposure: 365 kton・year
- Expected background: 0.3 events for $K^+ \rightarrow \nu\mu$ with nuclear γ, 0.6 events for $K^+ \rightarrow \pi^+\pi^0$.
- No candidates observed and no excess in momentum distribution.
- Lower lifetime limit: > 0.8×10^{34} year

Black: Data
Red: Atm.n MC
Blue: Signal MC



3. Summary of SK results



- Most of modes have been investigated with > 0.3 Mton・year exposure (red and green in the left figure).
- Super-Kamiokande can cover large number of decay modes.
- Many of them are the most stringent limits on nucleon lifetime.
- We observed some candidates, but still consistent with expected backgrounds and no evidence of nucleon decay has been observed.

Future prospects

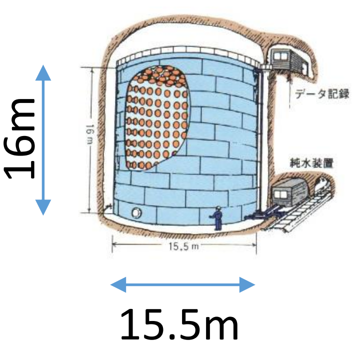
- Still no evidence has been found. Major decay modes are explored up to around 10^{34} years.
- Proton lives longer, ~10^{35} years ?
  - ➢ Run SK 10 times more (~200 years)? → Impossible.
- Absolutely, we need larger detector !

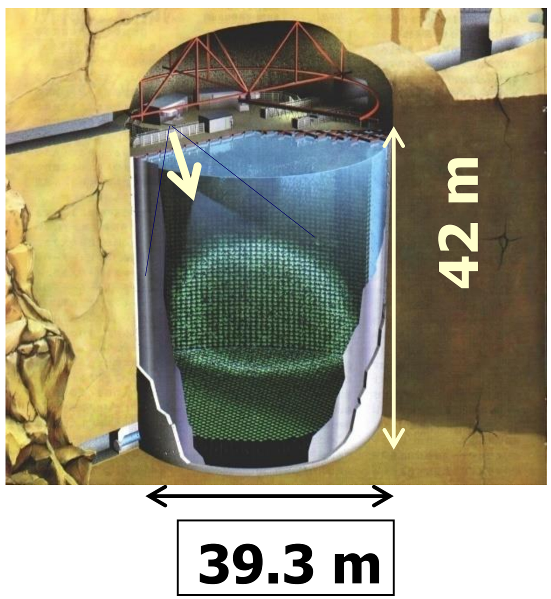
4. Hyper-Kamiokande project

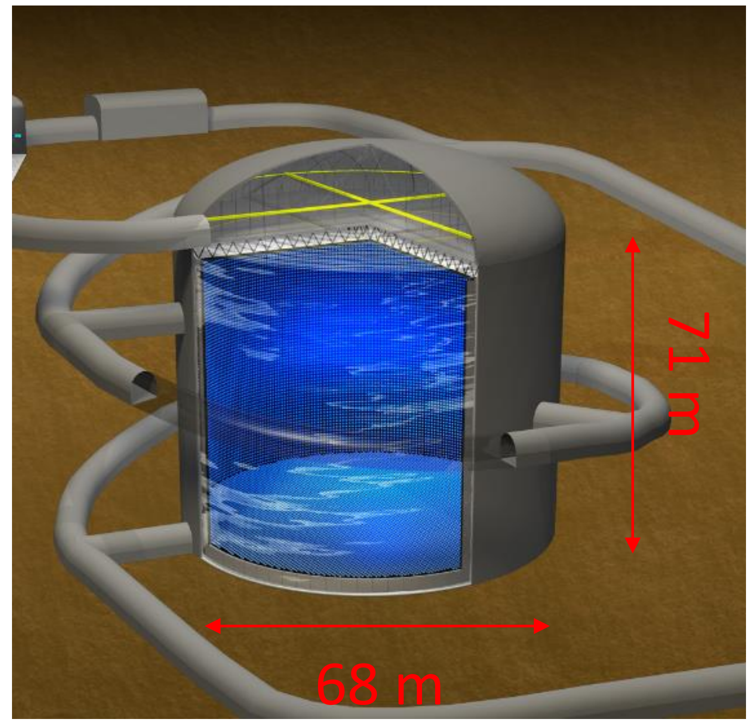
Proton decay ?

Neutrino oscillation

SN Neutrino





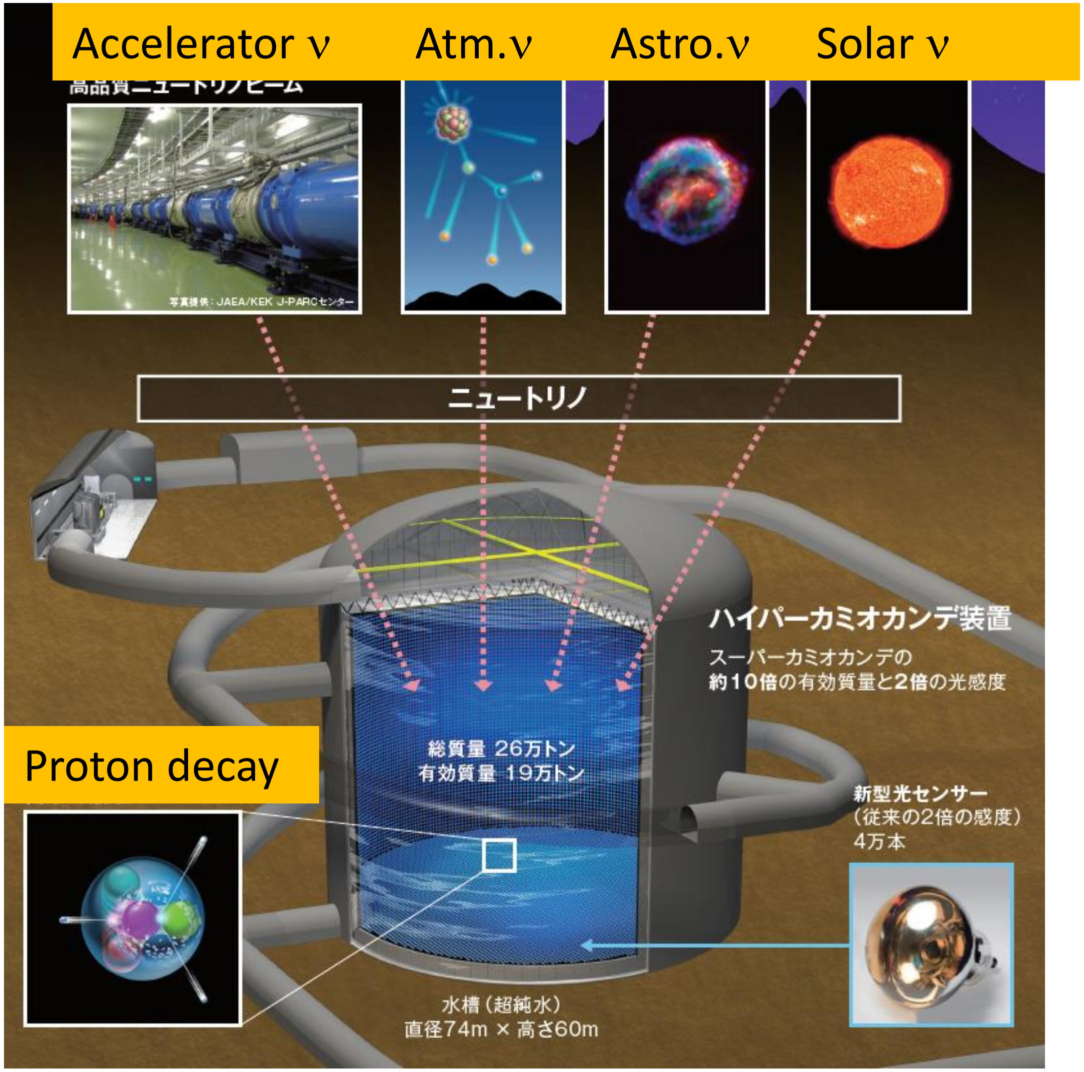


Kamiokande
3kton

Super-Kamiokande
50kton

Hyper-Kamiokande
260kton

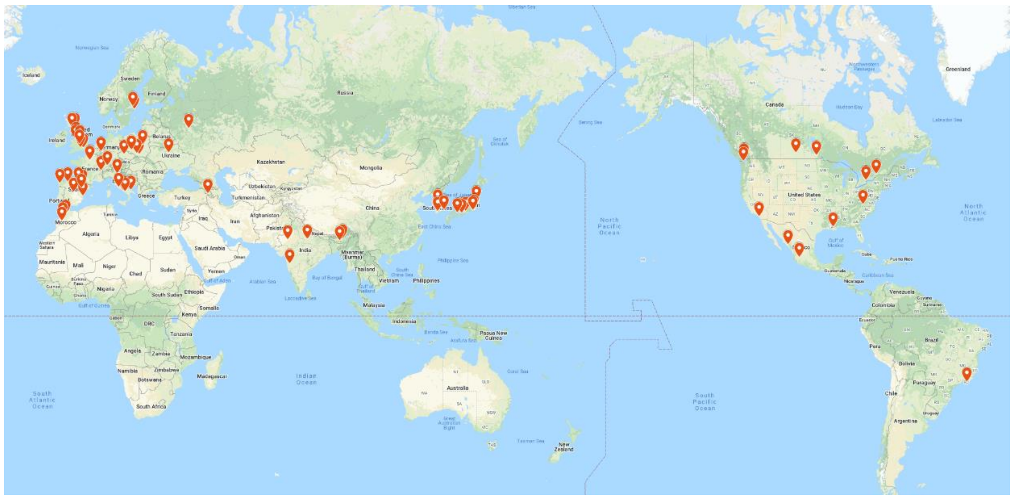
Hyper-K is multi-purpose detector

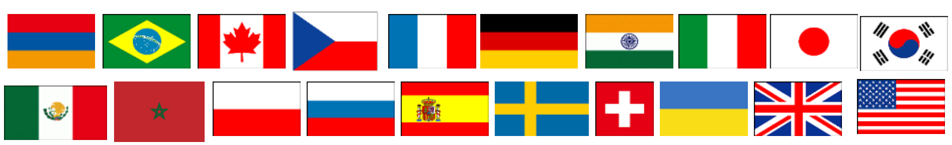


HYPER-K COLLABORATION:

20 countries, 99 institutes, ~500 people as of Jan 2022, and growing

Collaborating Institutes





Europe	281 members
Armenia	3
Czech	4
France	27
Germany	1
Italy	55
Poland	38
Russia	22
Spain	35
Sweden	5
Switzerland	13
Ukraine	4
UK	74

Asia	149 members
India	8
Korea	18
Japan	123

Americas	52 members
Brazil	3
Canada	32
Mexico	8
USA	9

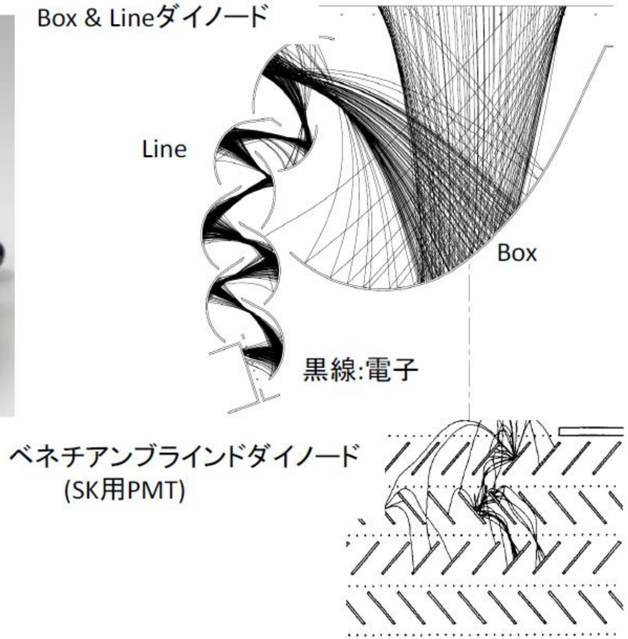
Africa	11 members
Morocco	11

I hope Vietnam joins soon ….

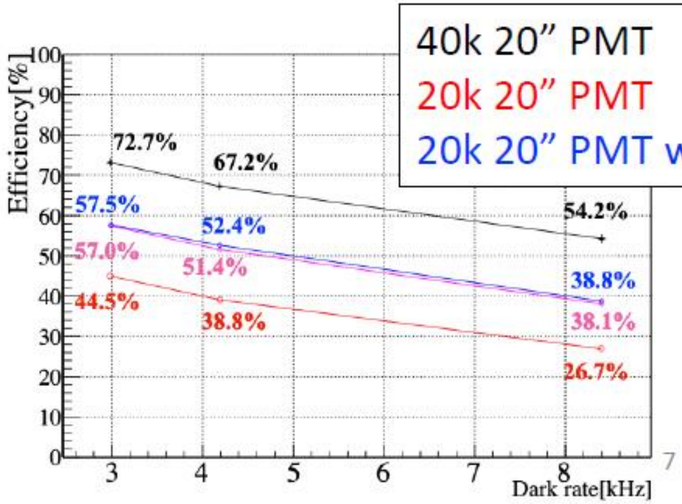
Enhance proton decay search with HK

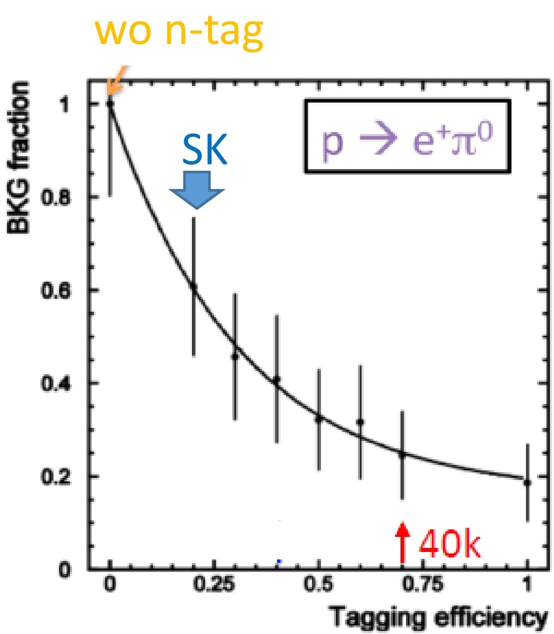
- Fiducial volume: 22.5kton (SK) → 190kton (HK)
- New photo sensor: Box&Line PMT
  - ➢ 2 times better photon counting performance
  - ➢ a half time resolution

Box&Line PMT



Better photon counting contributes neutron tagging



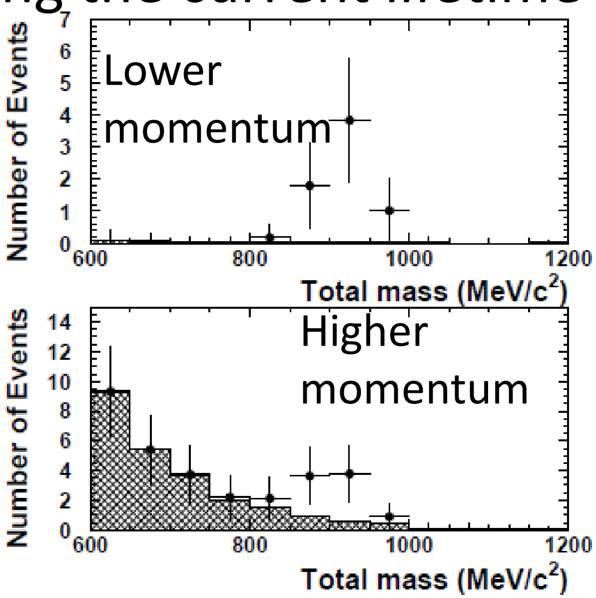


- Neutron tagging efficiency study with several detector set up.
- Efficiency depends on dark rate.
- Achive ~ 70% in the current baseline design (black) with ~ 4kHz dark rate.

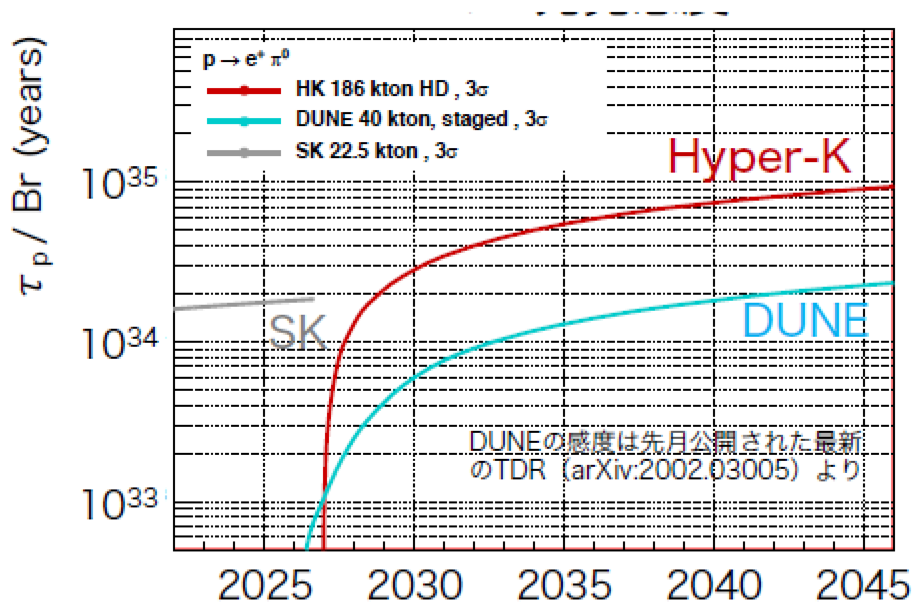
- p→e+p0 background reduction vs. Neutron tagging efficiency
- Background of HK becomes a half of SK !

Sensitivity for p→$e^+\pi^0$

Expected signal after 10 years run assuming the current lifetime limit



3σ discovery potential



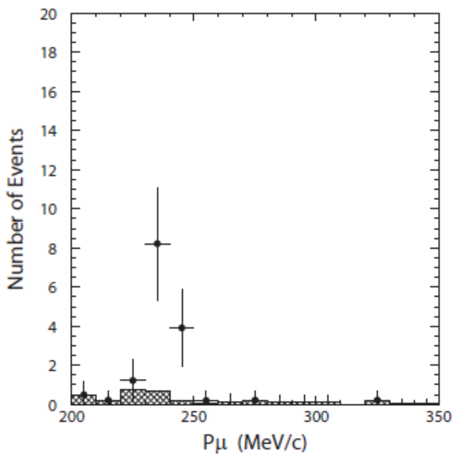
$0 < p_{tot} < 100$ MeV/c		$100 < p_{tot} < 250$ MeV/c	
ϵ_{sig} [%]	Bkg [/Mton·yr]	ϵ_{sig} [%]	Bkg [/Mton·yr]
18.7 ± 1.2	0.06 ± 0.02	19.4 ± 2.9	0.62 ± 0.20

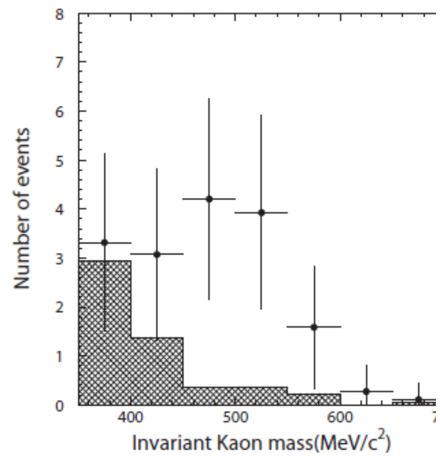
(SK: 0.18) (SK: 1.1)

Reach to 10^{35} years !

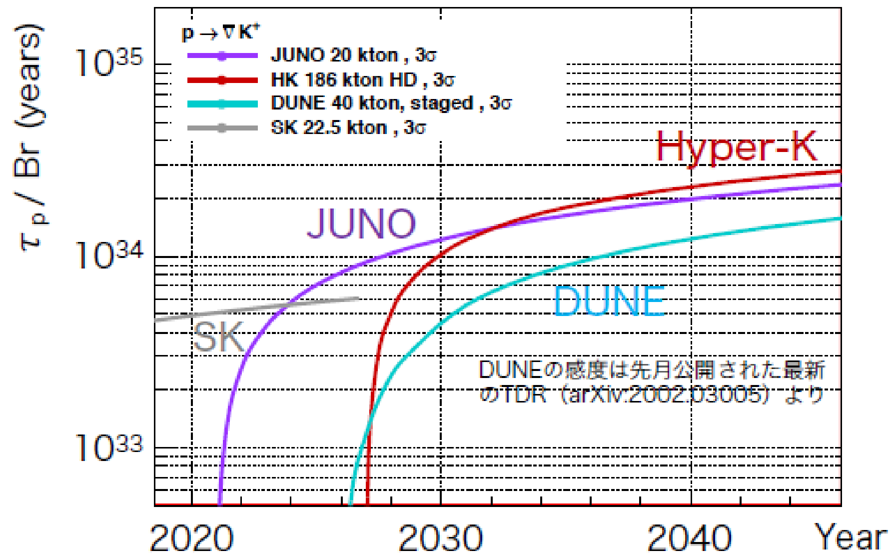
Sensitivity for p→νK$^+$

Expected signal after 10 years run assuming the current lifetime limit





3σ discovery potential



Prompt γ		$\pi^+\pi^0$		p_μ Spectrum		
ϵ_{sig} [%]	Bkg [/Mton·yr]	ϵ_{sig} [%]	Bkg [/Mton·yr]	ϵ_{sig} [%]	Bkg [/Mton·yr]	σ_{fit} [%]
12.7 ± 2.4	0.9 ± 0.2	10.8 ± 1.1	0.7 ± 0.2	31.0	1916.0	8.0

Better sensitivity than other detectors !.

What are still unknown in ν oscillation?

Unknow parameter

$c_{ij} = \cos\theta_{ij},\ s_{ij} = \sin\theta_{ij}$

CP phase

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

- $\theta_{12} = 33.6^\circ \pm 1.0^\circ$ Solar ν, KamLAND
- $\theta_{23} = 45^\circ \pm 6^\circ$ (90%CL) Atm. ν, Acc. ν

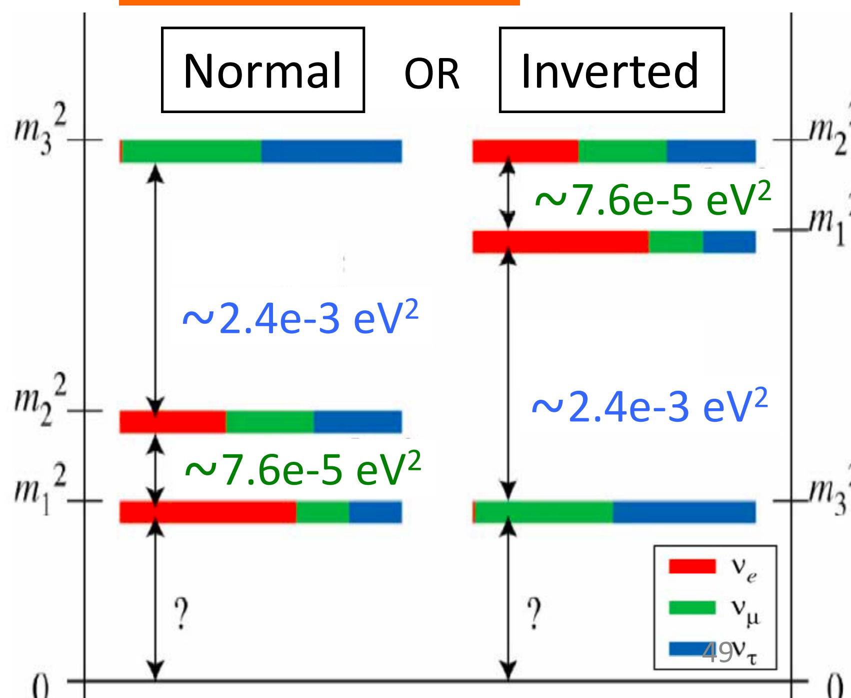
θ_{23} : How close to 45° ?
Octant? (<45°, >45° ?)

- $\theta_{13} = 9.1^\circ \pm 0.6^\circ$ Rector, Acc. ν

Indication of $\theta_{13} \neq 0$ by T2K
PRL107, 041801 (2011)

Later precise measurements by reactor ν experiments

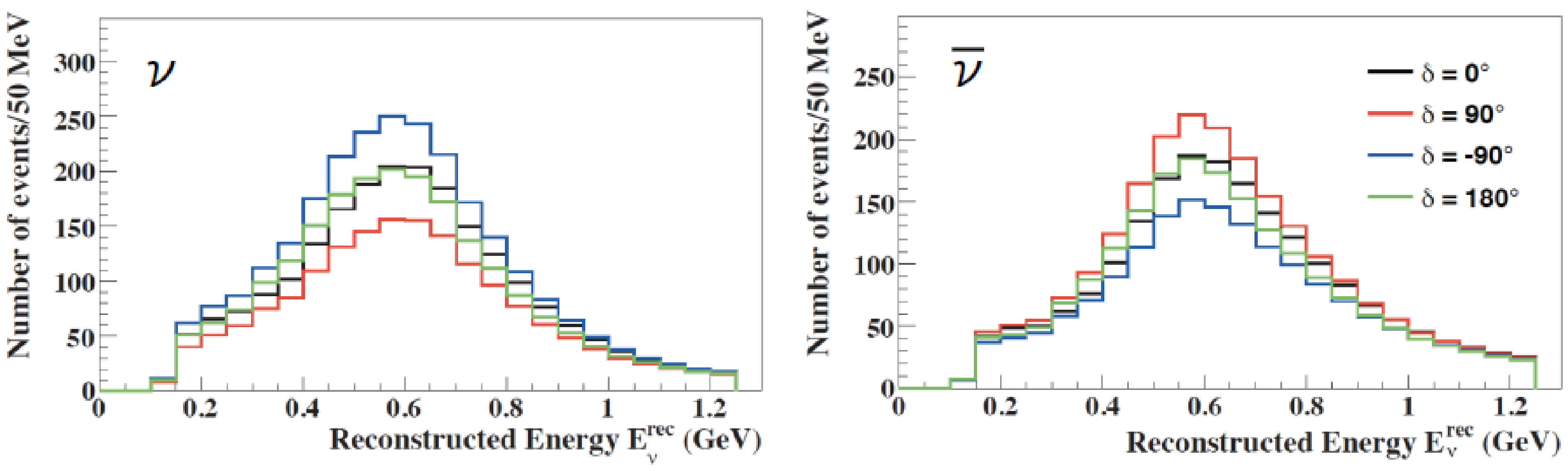
Mass hierarchy



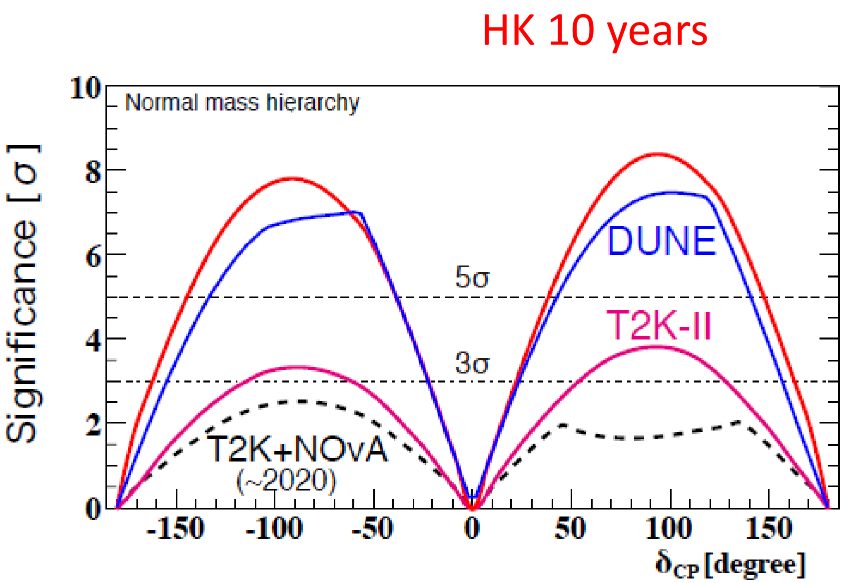
Effects of unknown parameters on ν oscillation are small ➔ Need statistics = larger detector !

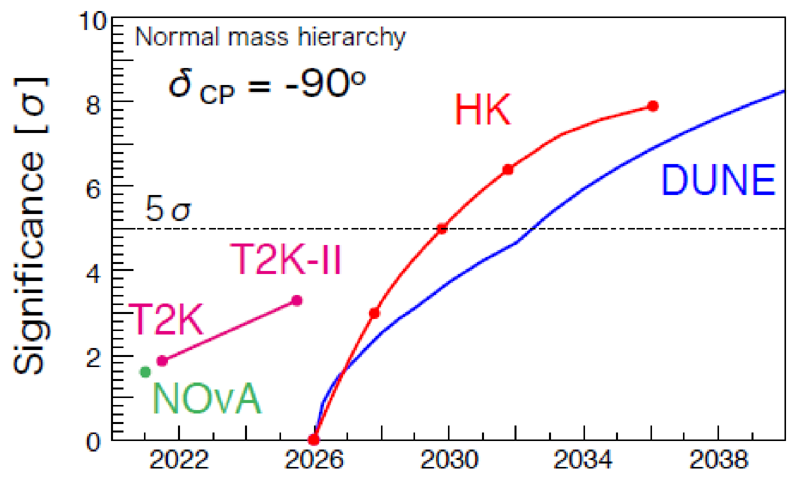
- ν beam experiments: Can study CP phase by comparing ν ν-bar oscillation.

Expected ν_e spectrum at HK (assuming 1.3 MW x 10 years)



Sensitivity of CP violation





- In 60 % region in δ_{CP}, we can discovery δ_{CP} with 5σ.
- If = δ_{CP} $\pm$ 90 degree, we can discover it within 5 years.

Atmospheric ν : $\nu_\mu \rightarrow \nu_e$ enhancement by matter effect

ν_e oscillation due to non-zero θ_{13} provides atm. nu. observation to investigate mass hierarch effect

$\nu_\mu \rightarrow \nu_e$ osc. probability in matter:

$$P(\nu_\mu \rightarrow \nu_e) \approx \sin^2\theta_{23}\sin^2 2\theta_{13}^M \sin^2\left(\frac{1.27\Delta m^2_{31,M} L}{E}\right)$$

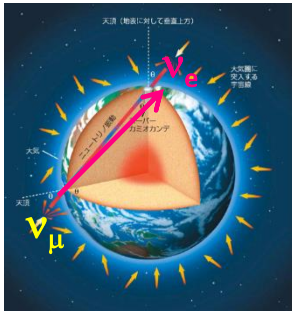
$$\sin^2 2\theta_{13}^M = \frac{\sin^2 2\theta_{13}}{\left(\cos 2\theta_{13} - A_{CC}/\Delta m^2_{31}\right) + \sin^2 2\theta_{13}}$$

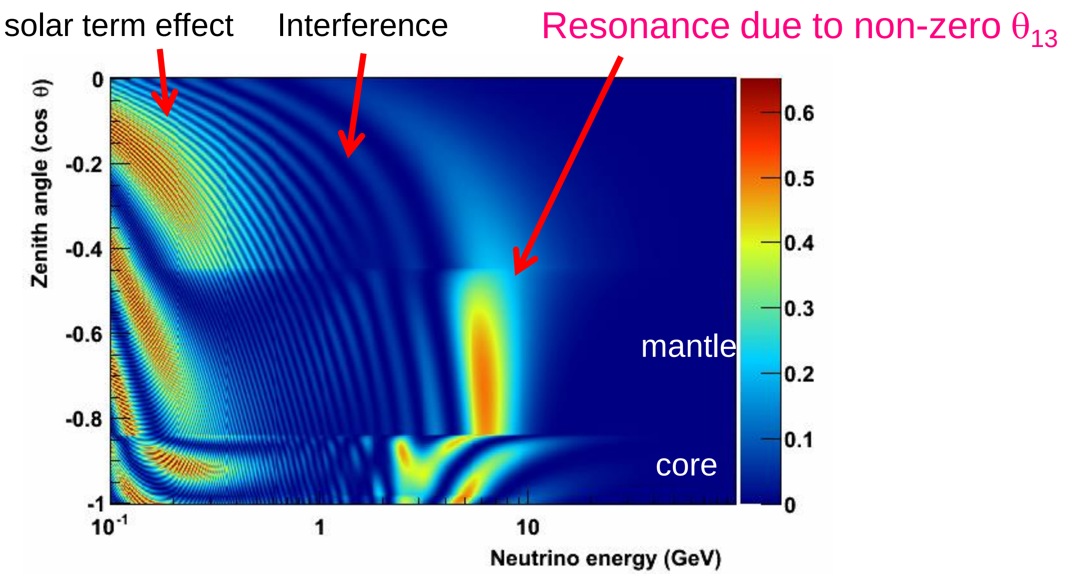
$\sin^2\theta_{13,M}$ has resonance feature when

$$A_{CC} \sim \Delta m^2_{31}\cos 2\theta_{13} \qquad (A_{CC} = 2\sqrt{2}G_F N_e E)$$

$\nu_\mu \rightarrow \nu_e$ resonance in multi-GeV region

$P(\nu_\mu \rightarrow \nu_e)$ of earth-throughgoing ν :





Occurrence of resonance feature depends on neutrino type and mass hierarchy:

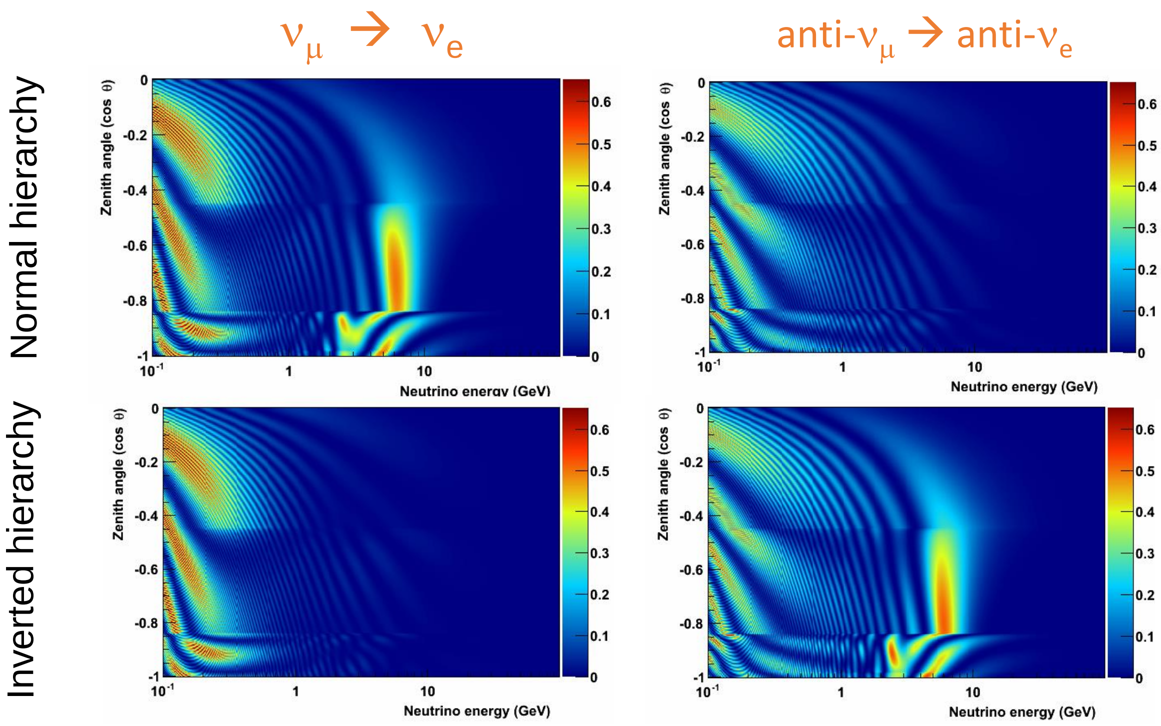
$$\sin^2 2\theta_{13}^M = \frac{\sin^2 2\theta_{13}}{\left(\cos 2\theta_{13} - A_{CC}/\Delta m_{31}^2\right) + \sin^2 2\theta_{13}}$$

In case of Inverted hierarchy:

$$\Delta m^2 \rightarrow -\Delta m^2$$

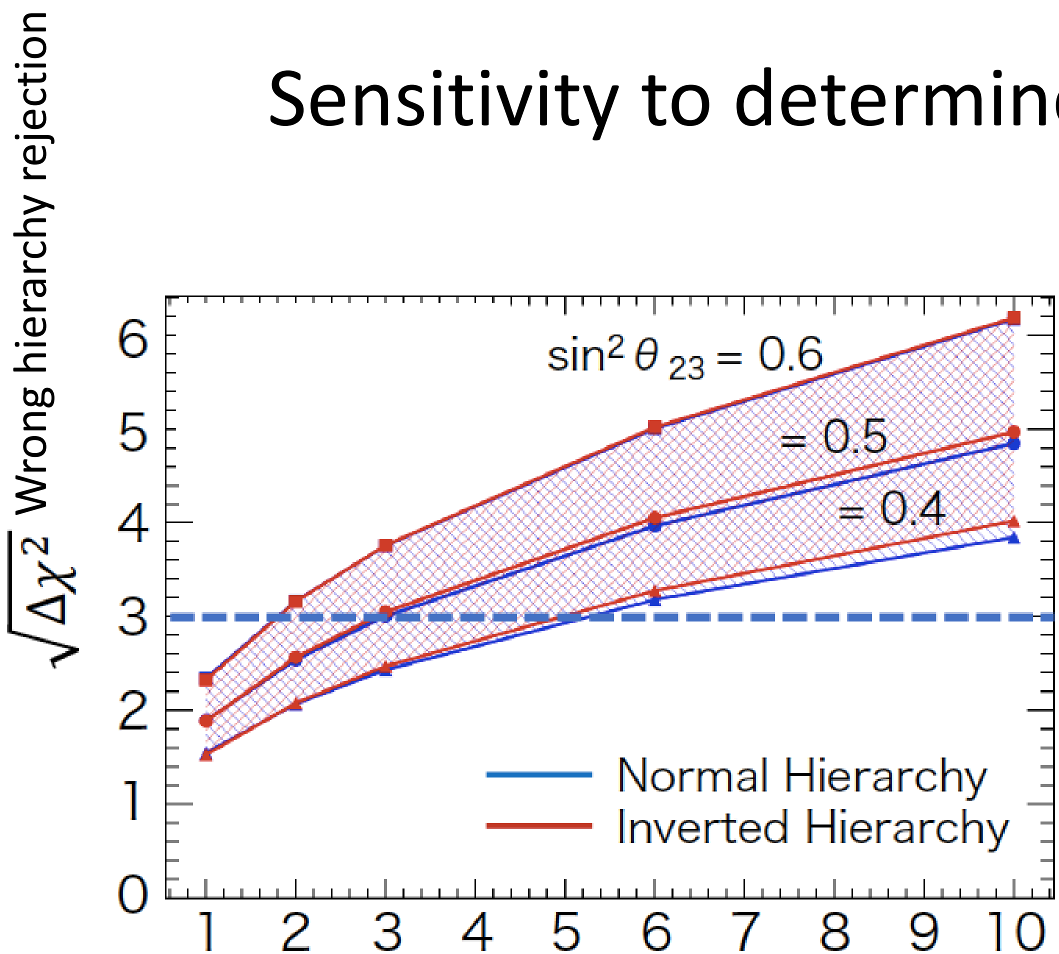
In case of anti neutrino :

$$A_{CC} \rightarrow -A_{CC}$$



Possible to determine mass hierarchy !

Sensitivity to determine mass hierarchy



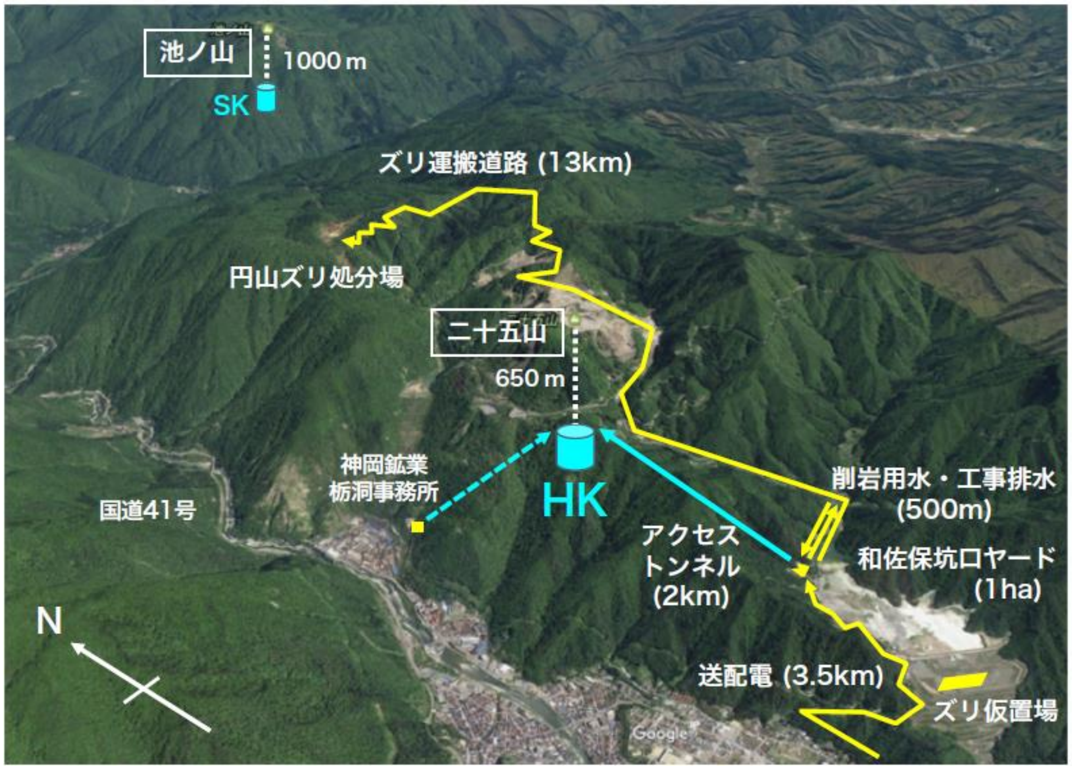
Beam ν: sensitive to δCP, but weak in mass hierarchy.

Atm. ν: large uncertainty from δCP.

➔ Combining both analysis gives good sensitivity to mass hierarchy.

3σ determine within 2 ~ 5 years !

Construction of HyperK has been started !



Making entrance yard for tunnel.

Aim to start observation in 2027 !

Access tunnel has reached to the center of HyperK tank in this June！

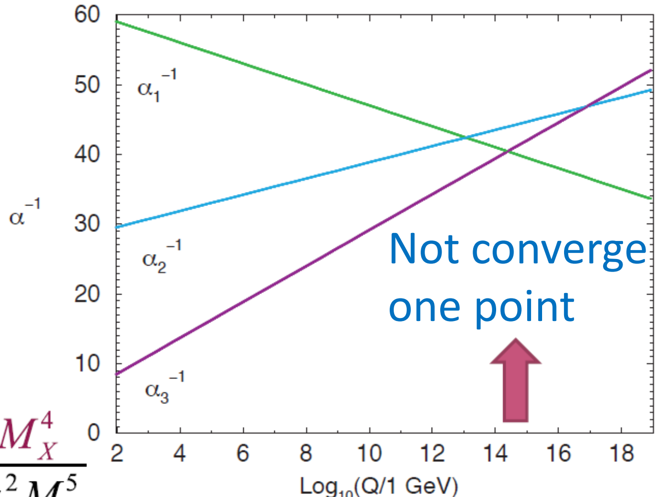
Detector Cavern is becoming a reality

4. Summary

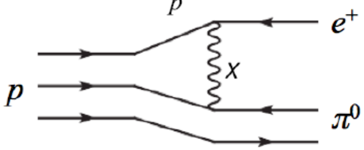
- Proton decay is a key phenomena of Grand Unified Theories beyond the Standard Model.
- Super-Kamiokande is the leading detector to hunt proton decays and have searched for it for more than 20 years.
- However, no evidence has been observed and the current proton lifetime limits are around 10^{34} years.
- It may be around the corner ! Hope three times lucky (3度目の正直 in Japanese） in Hyper-Kamiokande.
- HK also can determine remaining ν oscillation parameters .

Backup

Gauge Coupling Unification

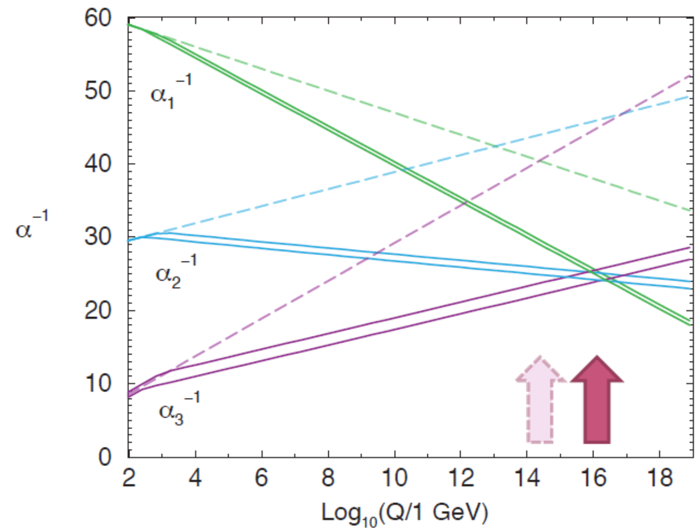


$$\tau \approx \frac{M_X^4}{\alpha^2 M_p^5}$$



$\tau(e^+\pi^0) = 4.5 \times 10^{29\pm1.7}$ *years* (predic

Problems solved by SUSY ...



Unification scale pushed up...

$\tau(e^+\pi^0) \approx 10^{35-38}$ years

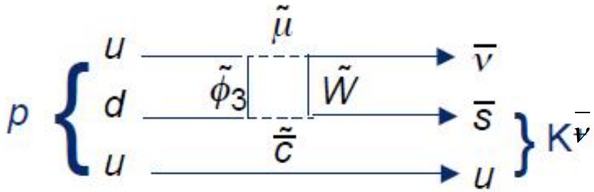
SUSY GUTs

- Unification scale higher than non-SUSY-GUTs ($M_x \sim 2 \times 10^{16}$ GeV)

  suppression of gauge boson mediated decay

$$\tau/B\,(p \to e^{+}\pi^{0}) \approx \left(M_X/2\times10^{16}\,\mathrm{GeV}\right)^{4} \times 10^{36\pm1}\ \text{years}$$

dominated by the D=5 op. (color Higgs triplet, q=1/3) mediated decays



$M_3 \sim 3 \times 10^{16}$ GeV, $M_{susy} \sim 1$ TeV

$$\tau/B\,(p \to K^{+}\bar{\nu}) \approx \left(0.003/\beta_H\right)^{2}\left(M_{\tilde{q}}/1\,\mathrm{TeV}\right)^{2}\left(M_3/10^{16}\,\mathrm{GeV}\right)^{2}\left(2/\tan\beta\right)^{2}\cdots$$

$$\times 9\times10^{31}\ \text{years}$$

(β_H : hadronic matrix element in GeV^3)

⇒ highly model dependent

p→ $\bar{\nu}$ K^{+} is regarded as dominant mode in SUSY-GUTs.

Many Other GUTs Beyond This Simple Story

Model	Ref.	Modes	τ_N (years)
Minimal $SU(5)$	Georgi, Glashow [2]	$p \to e^+\pi^0$	$10^{30} - 10^{31}$
Minimal SUSY $SU(5)$	Dimopoulos, Georgi [11], Sakai [12] Lifetime Calculations: Hisano, Murayama, Yanagida [13]	$p \to \bar{\nu}K^+$ $n \to \bar{\nu}K^0$	$10^{28} - 10^{32}$
SUGRA $SU(5)$	Nath, Arnowitt [14, 15]	$p \to \bar{\nu}K^+$	$10^{32} - 10^{34}$
SUSY $SO(10)$ with anomalous flavor $U(1)$	Shafi, Tavartkiladze [16]	$p \to \bar{\nu}K^+$ $n \to \bar{\nu}K^0$ $p \to \mu^+K^0$	$10^{32} - 10^{35}$
SUSY $SO(10)$ MSSM (std. $d=5$)	Lucas, Raby [17], Pati [18]	$p \to \bar{\nu}K^+$	$10^{33} - 10^{34}$
		$n \to \bar{\nu}K^0$	$10^{32} - 10^{33}$
SUSY $SO(10)$ ESSM (std. $d=5$)	Pati [18]	$p \to \bar{\nu}K^+$	$10^{33} - 10^{34}$ $\lesssim 10^{35}$
SUSY $SO(10)/G(224)$ MSSM or ESSM (new $d=5$)	Babu, Pati, Wilczek [19, 20, 21], Pati [18]	$p \to \bar{\nu}K^+$	$\lesssim 2 \cdot 10^{34}$
		$p \to \mu^+K^0$ $B \sim (1-50)\%$	
SUSY $SU(5)$ or $SO(10)$ MSSM ($d=6$)	Pati [18]	$p \to e^+\pi^0$	$\sim 10^{34.9\pm1}$
Flipped $SU(5)$ in CMSSM	Ellis, Nanopoulos and Wlaker[22]	$p \to e/\mu^+\pi^0$	$10^{35} - 10^{36}$
Split $SU(5)$ SUSY	Arkani-Hamed, *et. al.* [23]	$p \to e^+\pi^0$	$10^{35} - 10^{37}$
$SU(5)$ in 5 dimensions	Hebecker, March-Russell[24]	$p \to \mu^+K^0$ $p \to e^+\pi^0$	$10^{34} - 10^{35}$
$SU(5)$ in 5 dimensions option II	Alciati *et.al.*[25]	$p \to \bar{\nu}K^+$	$10^{36} - 10^{39}$
GUT-like models from Type IIA string with D6-branes	Klebanov, Witten[26]	$p \to e^+\pi^0$	$\sim 10^{36}$

TABLE I: Summary of the expected nucleon lifetime in different theoretical models.

A. Bueno et al. hep-ph/0701101

Uncertainties in the predictions:

Nuclear matrix elements updated w. lQCD, still: x10 uncertainty in lifetime

SUSY masses: ~ x100 uncertainty in lifetime

Proton life time: $10^{30} \sim 10^{35}$ years

Modes beyond $e^+\pi^0$, $K^+\nu$
and other antilepton + meson decays

$p \rightarrow \mu^- \pi^+ K^+$	$B + L$
$n \rightarrow \bar{n}$	$\Delta B = 2$, TeV < scale < GUT
$pp \rightarrow K^+ K^+$	$\lambda''_{uds} < 10^{-8}$
$p \rightarrow e^- \pi^+ \pi^+ \nu\, \nu$	6 dimensions
$n \rightarrow \nu\, \nu\, \nu$	invisible
$p \rightarrow e^+\, \gamma$	radiative

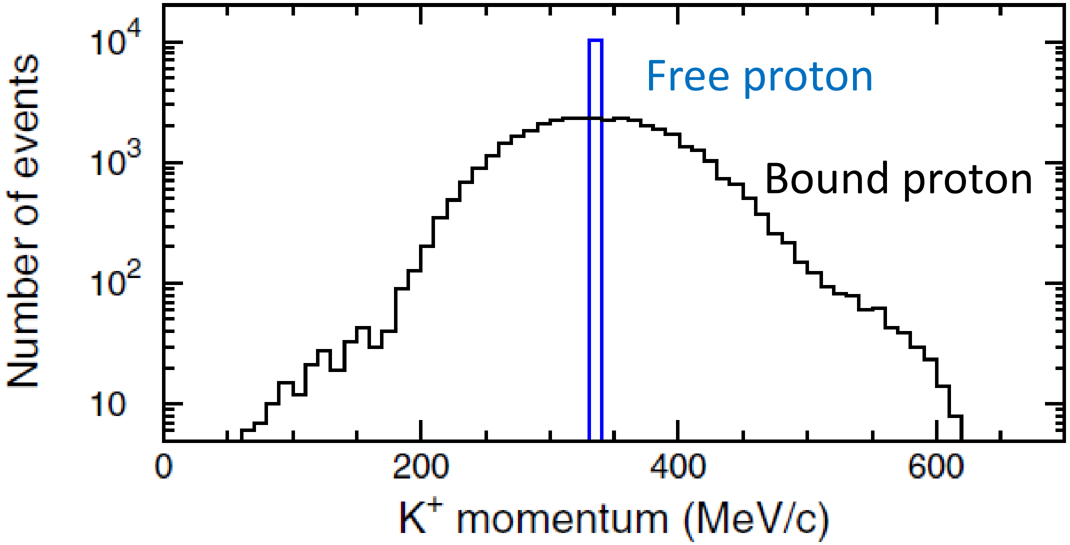
there is plenty to keep us busy ...

How to find 2.2 MeV γ

- After Time-of-Flight subtraction, search for 7 hits in 10 nsec time window. → candidates of γ.
- Make 16 variables related to space and time information of each hits (RMS of phi, theta, hit time, e.t.c.)
- Put them into Neural Network to judge γ or not.
- Neutron tagging efficiency: 21 % (mis-tagging: 1.8 %)

3. p→νK^+ search

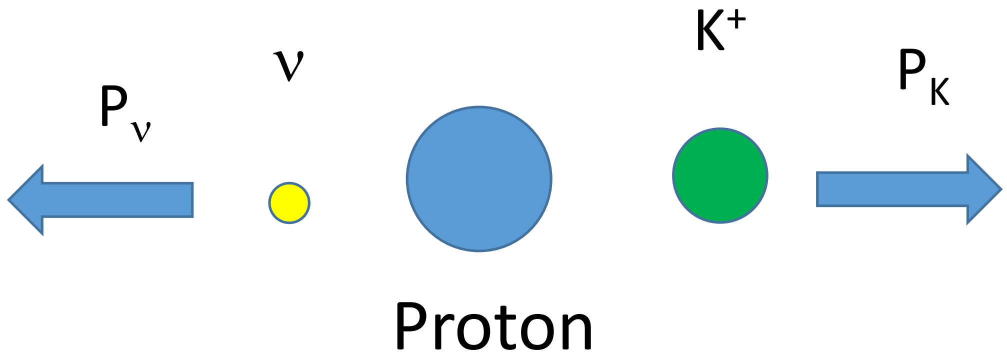
Difficulty of p→νK^+



- K^+ mass: 494 MeV, relatively heavy.
- Cherenkov threshold: 560 MeV/c.
- Most of K^+ can not emit Cherenkov light.

Q. Calculate momentum of K^+ from free proton decay.

Hint: proton mass: 938 MeV, "free" means proton momentum=0.



Conservation of momentum: $P_\nu = P_K$

Conservation of energy: $M_P = \sqrt{M_K^2 + P_K^2} + P_\nu$

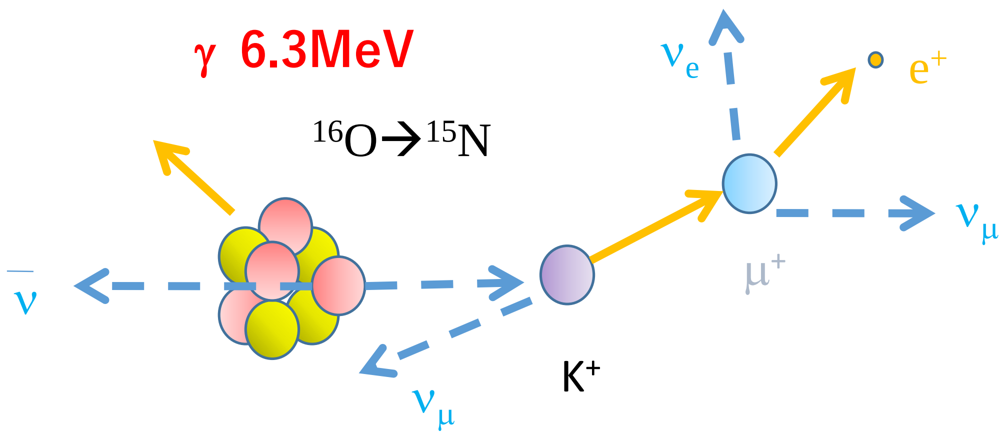
Proton Electron Neutrino

$$P_K = \frac{M_P^2 - M_K^2}{2M_P}$$

3-1 How to find $p \rightarrow \nu K^+$ in Water Cherenkov detector

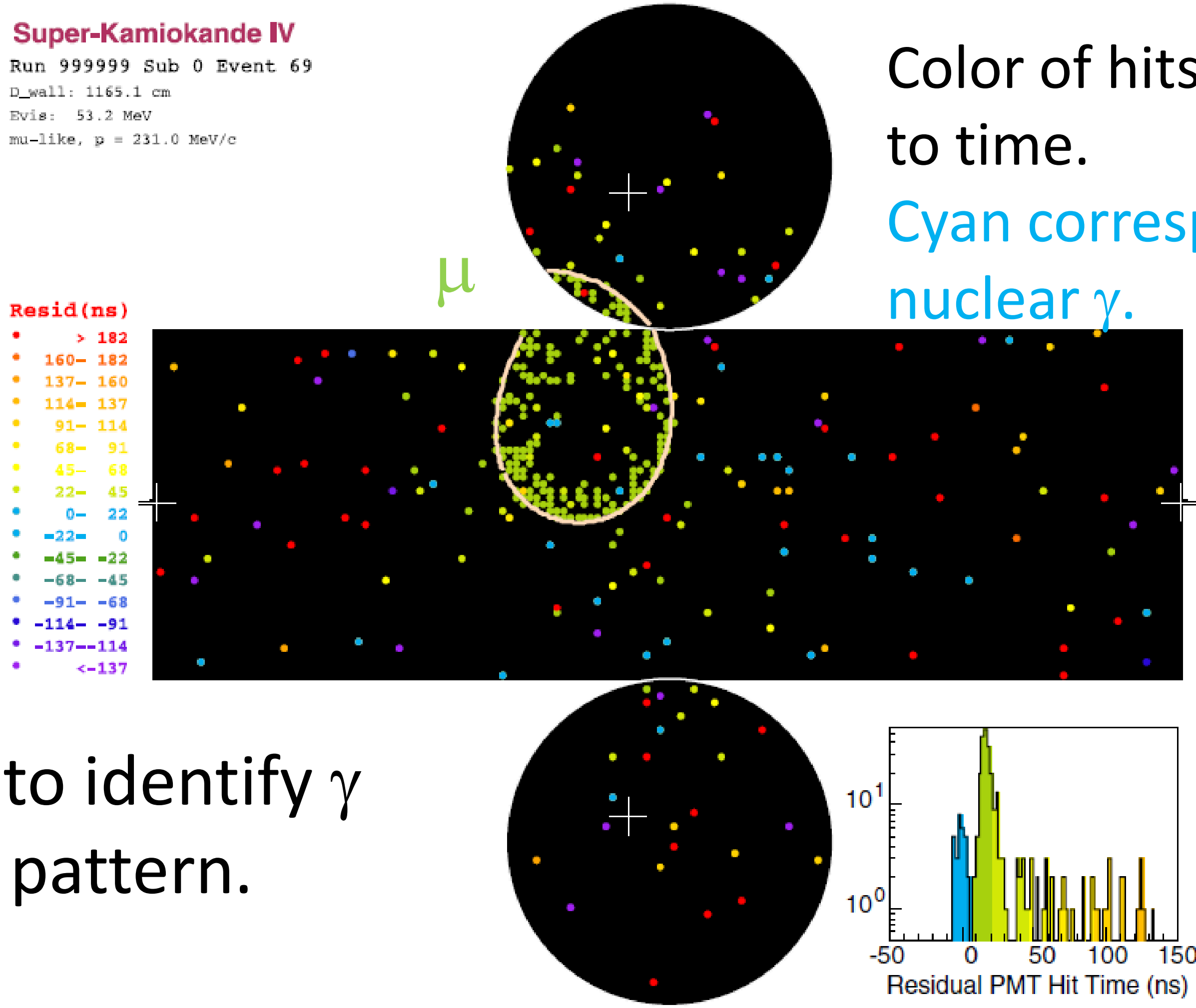
- K^+ has low momentum, most of them stop in water and decay with 12 nsec lifetime.
- Major K^+ decay mode
  - $K^+ \rightarrow \nu\mu^+$: 64 %
  - $K^+ \rightarrow \pi^+\pi^0$: 21 %
- "Stopping K^+" means two body decay products of K^+ should have monochromatic momentum as seen in the previous question !
  - $K^+ \rightarrow \nu\mu^+$: 236 MeV/c
  - $K^+ \rightarrow \pi^+\pi^0$: 206 MeV/c
- Using this property, Water Cherenkov detector can search for $p \rightarrow \nu K^+$.

3-2. Search for $p \rightarrow \nu K^+$, $K^+ \rightarrow \nu \mu^+$



- Visible particle is only μ^+ with Michel electron.
- Search for data excess around 236 MeV/c of μ comparing with atmospheric ν MC.
- After proton decay, 40 % of remaining nucleus emits 6 MeV γ for deexcitation. It is useful to reduce background.

Example of p→νK⁺, K⁺→νμ⁺ with γ

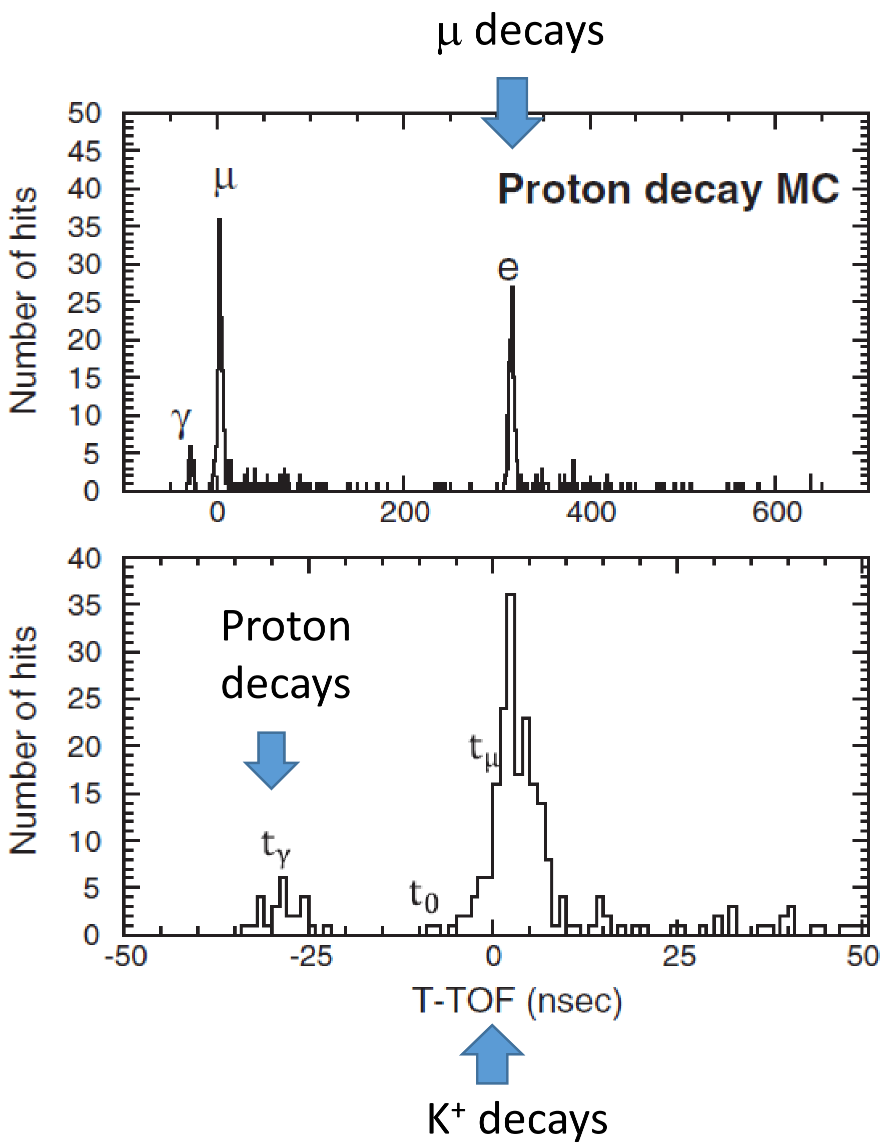


Color of hits corresponds to time.

Cyan corresponds to nuclear γ.

Difficult to identify γ from hit pattern.

Time structure with nuclear γ



- 3 hit clusters in time should be observed in case of signal.
- The event is triggered by μ hits.
- γ signal is much smaller than μ and easily hidden by tail of μ hits.
- Make 12 nsec time window and slide it toward left from t_0 (end of μ tail) to search for maximum hit cluster.

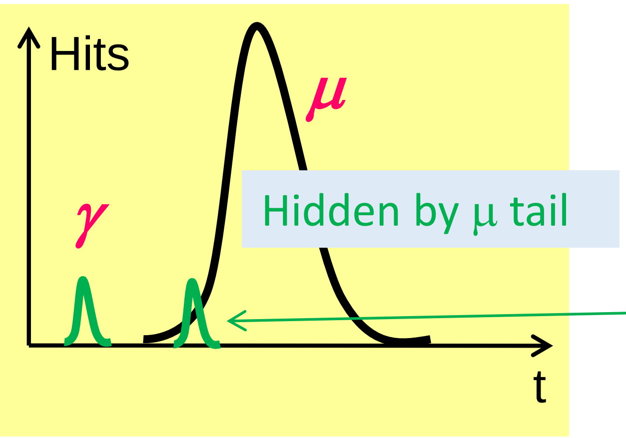
Selection criteria for $p \rightarrow \nu K^+$, $K^+ \rightarrow \nu \mu^+$

- 1 μ-like ring with Michel electron
- $215 < P\mu < 260$ MeV/c
- Proton rejection cuts
- Search Max hit cluster ⟵ Reduce background by 5×10^{-4} !

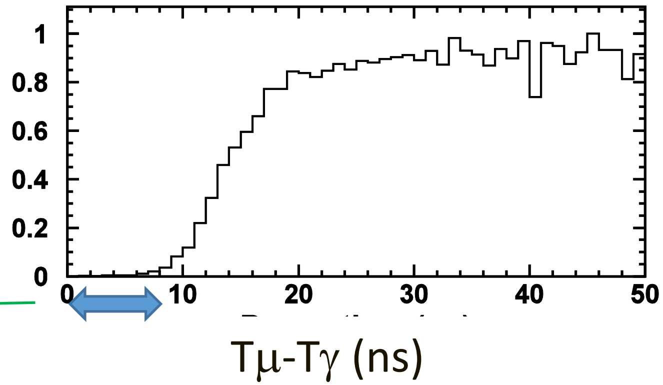
  by sliding time window (12ns width);
  - $4 < N\gamma < 30$ hits
  - $T_\mu - T_\gamma < 75$ nsec
- No neutron
- Selection efficiency = (selected events)/(proton decay in fiducial volume): 9 %
  - $Br(K^+ \rightarrow \nu \mu^+)$= 64 %, only 40 % emits nuclear γ → 26 % even if detector is perfect.

Remark for this analysis

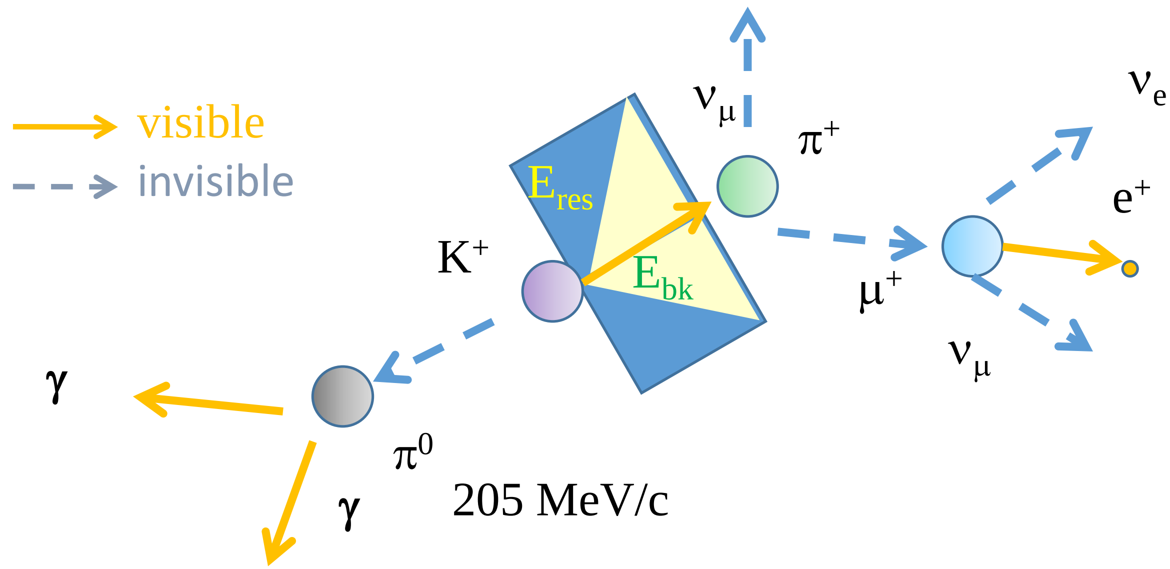
- This analysis is limited by time resolution of PMTs.
  - If γ is close to μ, γ peak is hidden by μ hits.
  - Time resolution of SK PMT is 2.2 nsec at 1 photoelectron.
  - If μ peak becomes sharper, the selection efficiency will be improved.



γ tagging efficiency

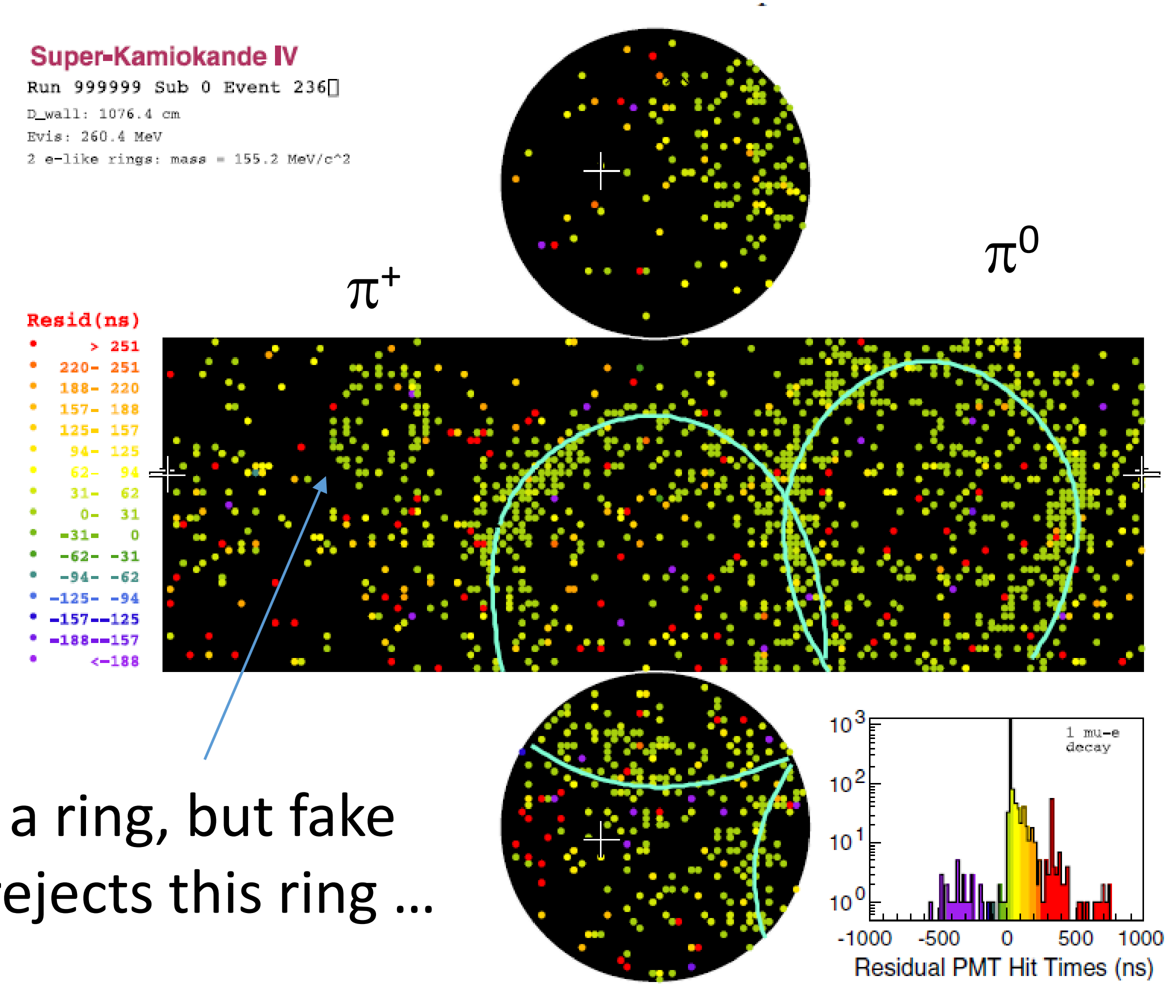


3-3. Search for p→νK^+, $K^+ \to \pi^+\pi^0$



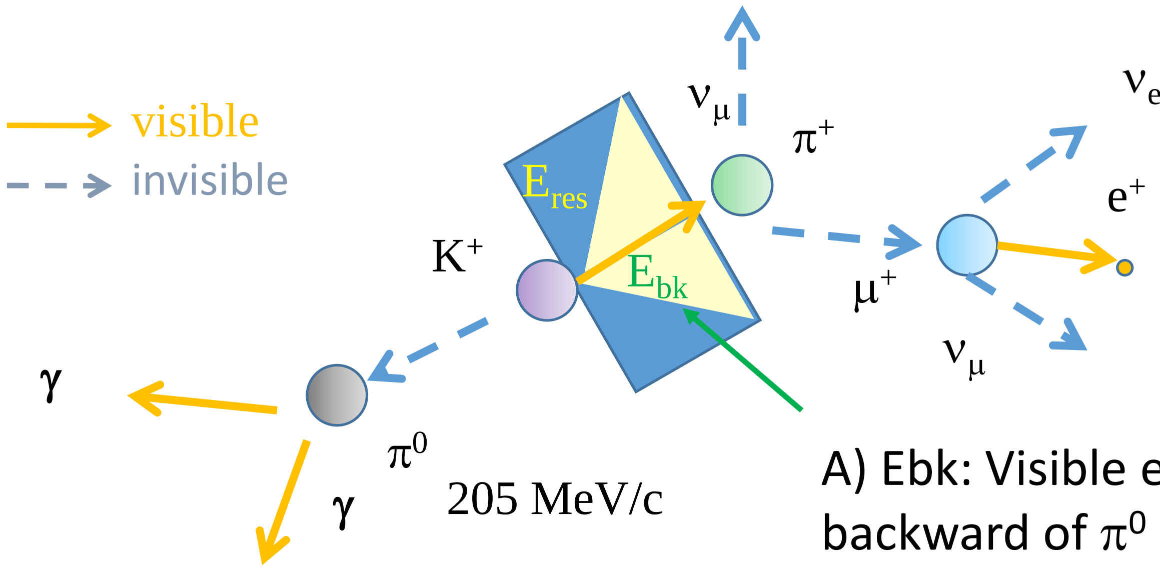
- Both π^+ and π^0 has 205 MeV/c in momentum. This is just above Cherenkov threshold for π^+, thus it is not identified as a ring in most of case.
- π^+ decays into μ (invisible) and ν, μ decays into $e\nu_e\nu_\mu$.
- π^0 decays into 2 γs.
- Search for 206 MeV/c π^0 with Michel electron.

Example of p→νK$^+$, K$^+$→$\pi^+\pi^0$



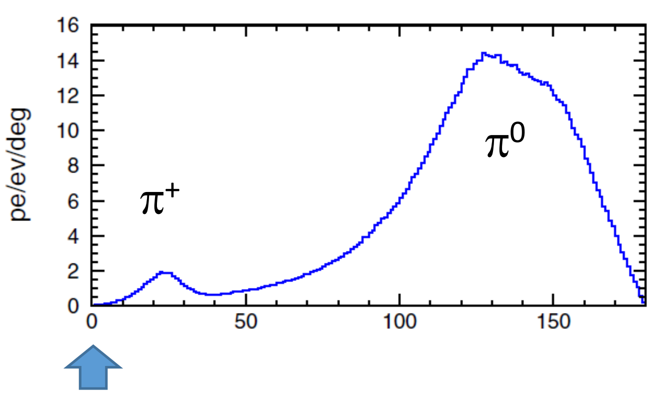
Look like a ring, but fake ring cut rejects this ring …

Use π^+ information to select events



A) Ebk: Visible energy sum in backward of π^0 direction (140°-180°)

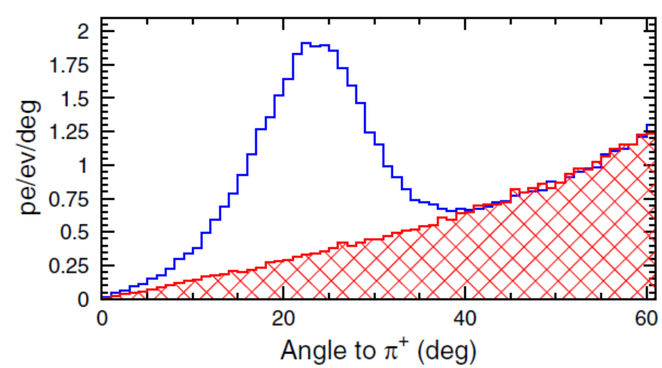
Charge distribution



π^+ direction

Zoom

B) Make likelihood for hit pattern.



Selection criteria for $p \rightarrow \nu K^+$, $K^+ \rightarrow \pi^+\pi^0$

- 1 or 2 e-like rings with decay-e.
- $85 < M\pi^0 < 185$ MeV.
- $175 < P\pi^0 < 250$ MeV/c.
- E_{bk}: visible energy sum in 140-180 deg. of π^0 dir,
  E_{res}: in 90-140 deg,
  L_{shape}: Likelihood based on charge profile
  $10 < E_{bk} < 50$ MeV
  $E_{res} < 12$ MeV (20 MeV for 1ring)
  $L_{shape} > 2.0$ (3.0 for 1ring)
- No neutrons
- Selection efficiency: 10 % ($Br(K^+ \rightarrow \pi^+\pi^0)$=21 %)

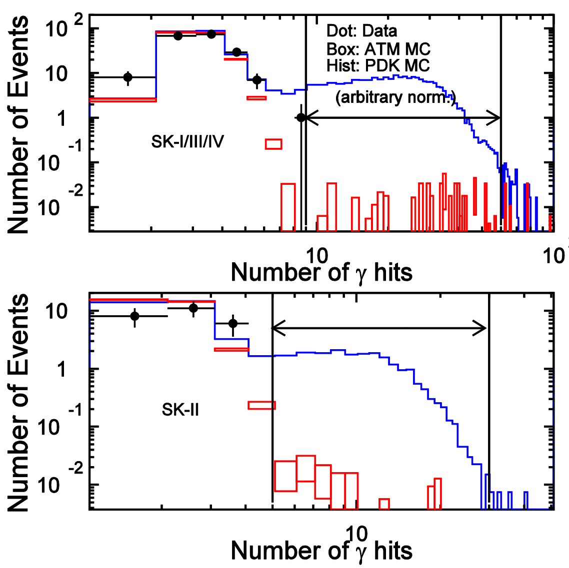
Background for $p \rightarrow \nu K^+$

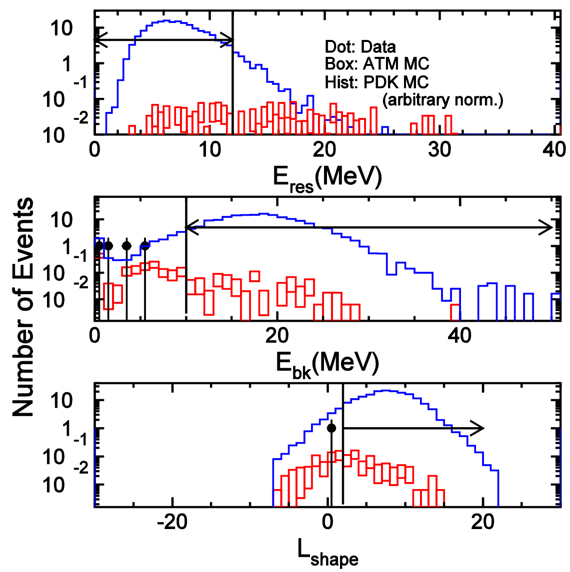
- Dominant background is K^+ production by neutrino interactions.
  - $\nu p \rightarrow \nu \Lambda K^+$, $\Lambda \rightarrow p\pi^-$ (BR:64 %, mostly invisible in WCD)
  - Emit nuclear γ as same as the signal.
- It is also rare interaction and we had poor information from very old bubble chamber. Large uncertainty.
- Recently MINERvA measures K^+ production. It is very useful information for this analysis.

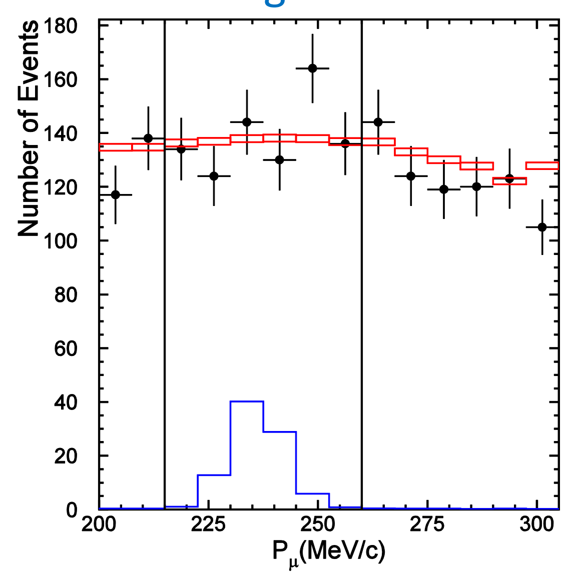
3-4. SK results (So far)

- Exposure: 365 kton・year
- Expected background: 0.3 events for $K^+ \rightarrow \nu\mu$ with nuclear γ, 0.6 events for $K^+ \rightarrow \pi^+\pi^0$.
- No candidates observed and no excess in momentum distribution.
- Lower lifetime limit: > 0.8×10^{34} year

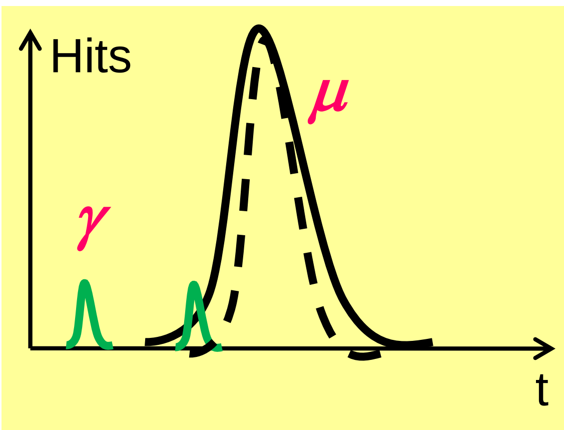
Black: Data
Red: Atm.n MC
Blue: Signal MC



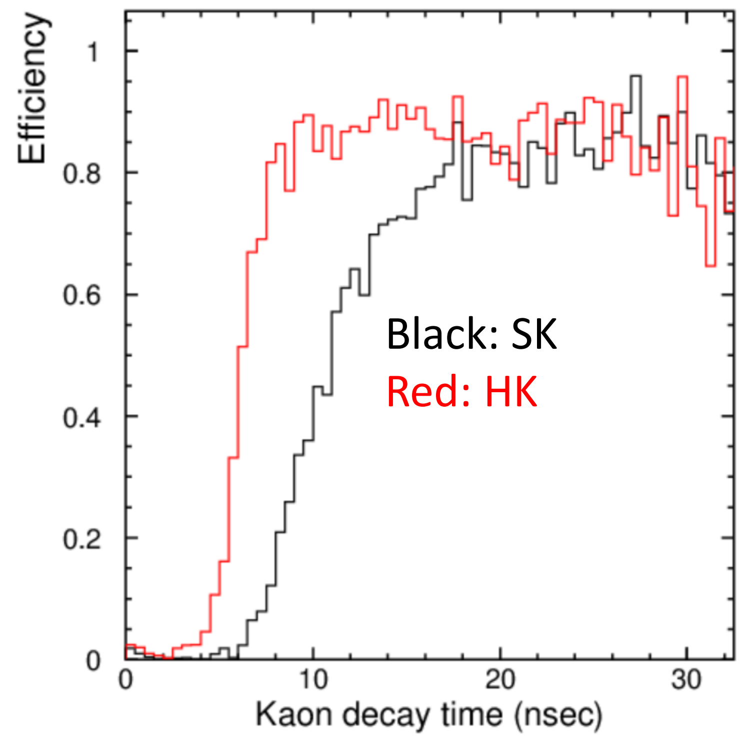




Faster PMT response improves nuclear γ tagging in p→νK⁺



γ tagging efficiency



- Time resolution: 2.2nsec (SK) →1.1 nsec (HK).
- Sharper time distribution of μ → γ close to μ cab be identified !

(Better photon counting also contributes improvement)