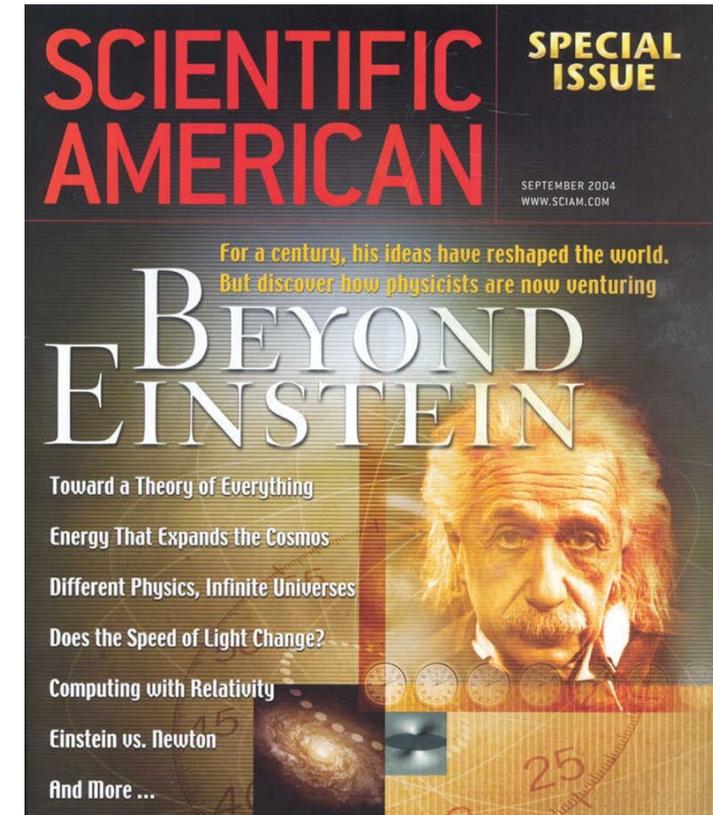


Tests of Spacetime Symmetry with Neutrinos

outline

1. Introduction
2. Tests of Lorentz violation with neutrinos
3. Tests of Lorentz violation with astrophysical neutrinos
4. Conclusion



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Neutrino Conference 2025, ICISE, Quy Nhon, Vietnam, July 23, 2025

Introduction

Theory of Special Relativity

Einstein and Lorentz



Special relativity is a basis of both quantum field theory and general relativity

Special relativity is based on Lorentz symmetry

Lorentz symmetry is isotropy of spacetime

If the universe has a special direction, space doesn't have Lorentz symmetry and Lorentz transformation is violated

→ Lorentz violation

All fundamental physics phenomena must be experimentally tested including Lorentz symmetry

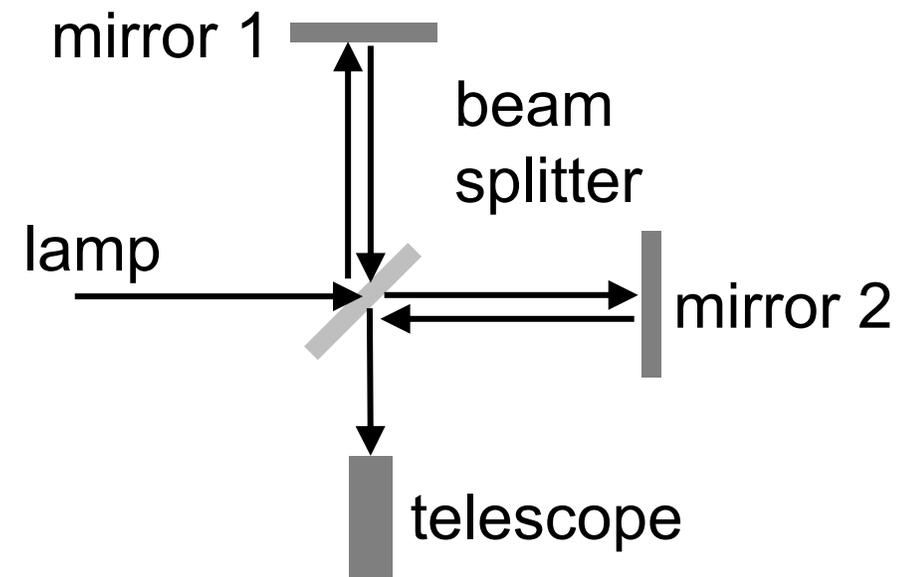
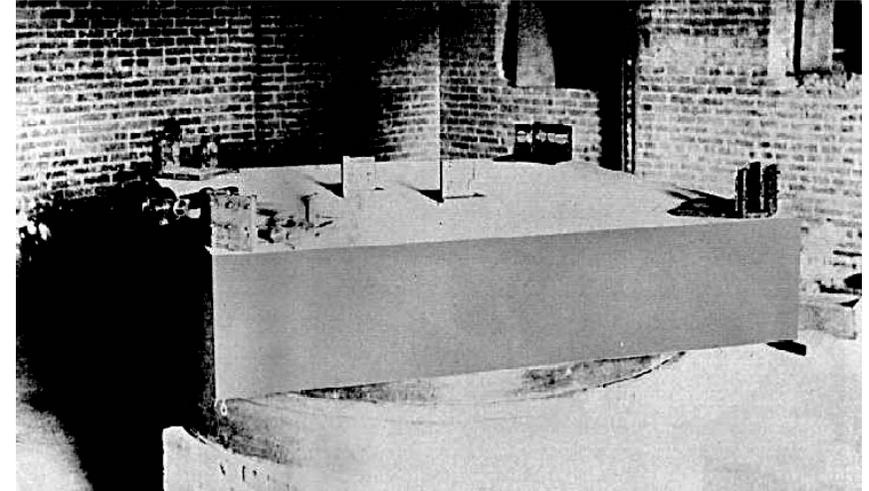
Michelson-Morley experiment

The experiment tried to measure the motion of the Earth relative to æther.

The experiment shows the speed of light is constant regardless the motion of the Earth.

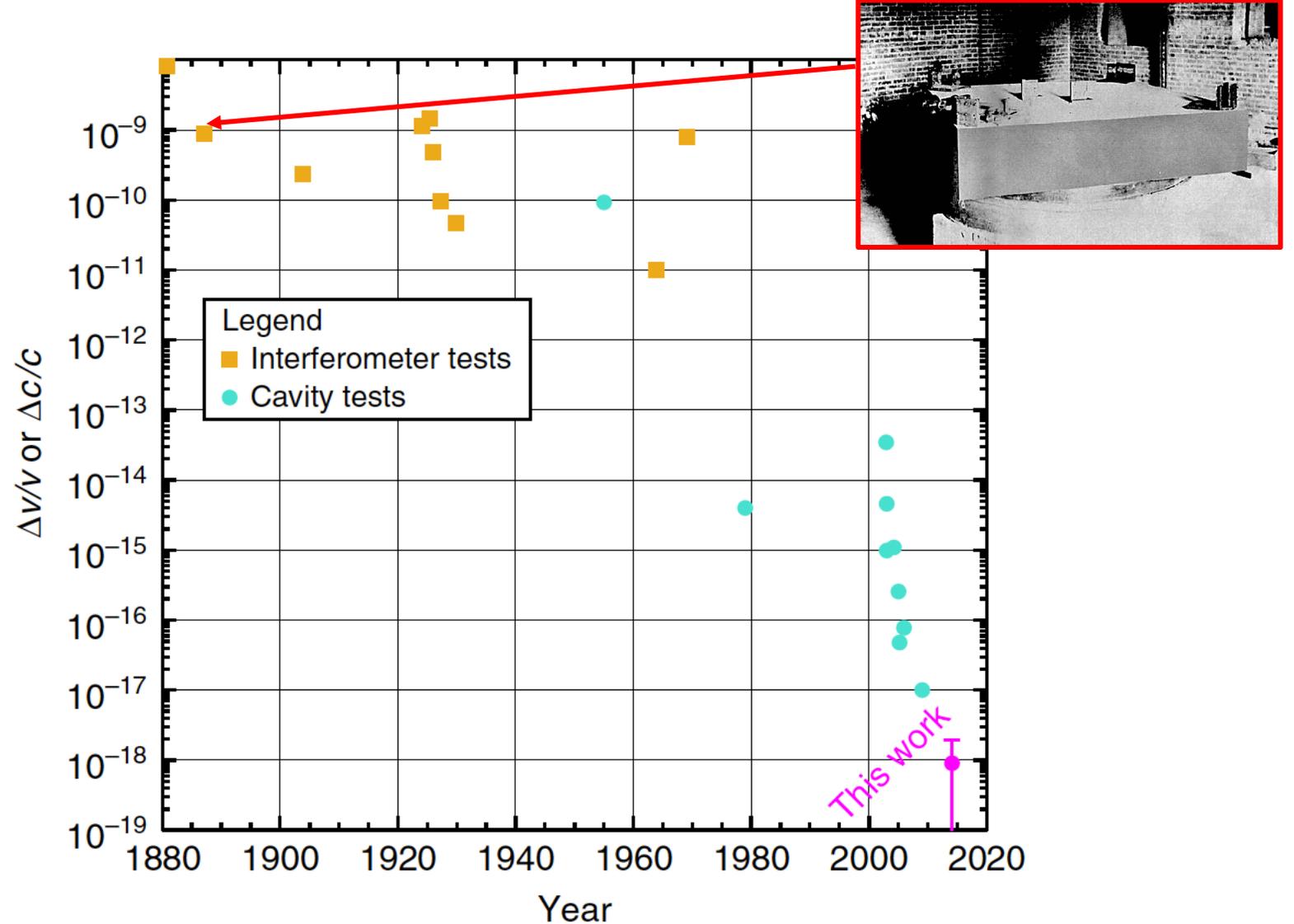
This result suggests the isotropy of spacetime, and Lorentz symmetry.

Lorentz symmetry is valid down to $\Delta c/c < 10^{-9}$



Michelson-Morley experiment

The experiment has been improved over 100 years.



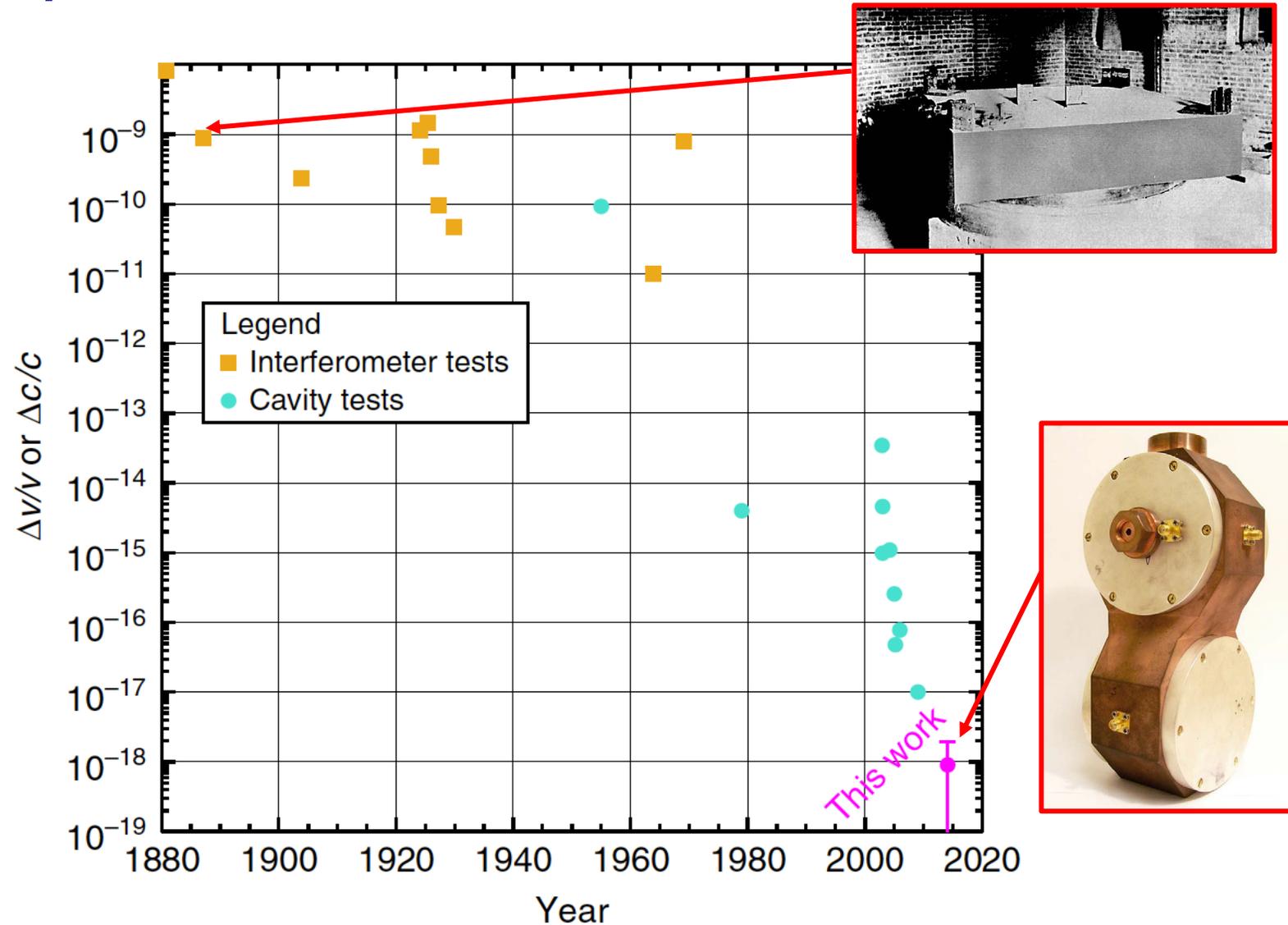
Michelson-Morley experiment

The experiment has been improved over 100 years.

Technology shift
(interferometer \rightarrow optical cavity) and $\Delta c/c < 10^{-18}$
(1 billion higher precision than M-M experiment)

Why we keep testing this?

Why do we expect Lorentz violation?



Quantum gravity

Searching Lorentz violation is well motivated

Lorentz violation in Planck scale theories

- string theory
- noncommutative field theory
- quantum loop gravity

etc

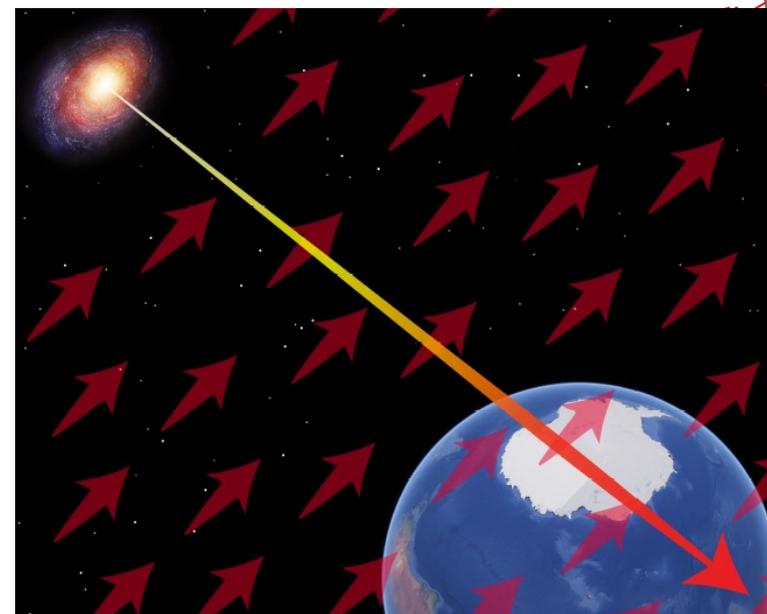
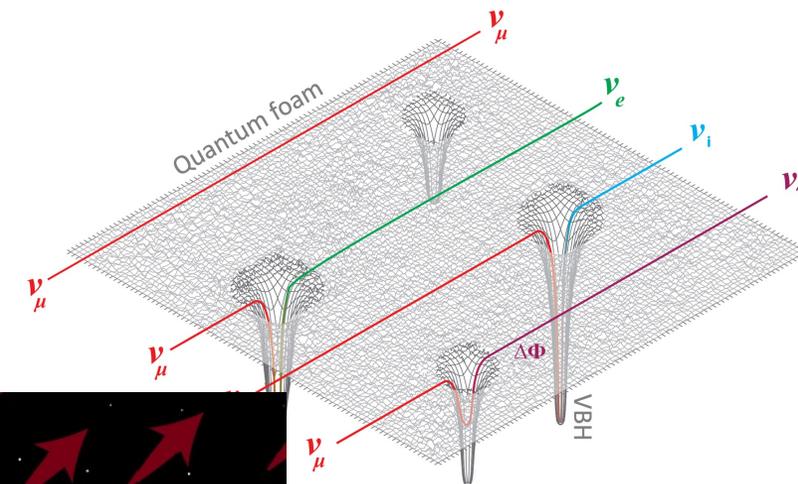
Lorentz violation is seen as

- spacetime fluctuation (Lindblad eqn.)
- background field in vacuum (SME)

etc

Quantum foam

- quantum fluctuation of space-time



Lorentz violating field

- background field of the universe (æther)

Standard-Model Extension (SME)

Search of Lorentz violation is to find anomalous effects due to the couplings of background fields and ordinary fields (electrons, muons, neutrinos, etc)

SME is an effective field theory (EFT) framework to look for Lorentz violation

e.g.) vacuum Lagrangian for fermion

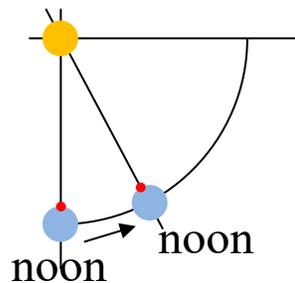
$$\mathcal{L} = \underbrace{i\bar{\psi}\gamma_{\mu}\partial^{\mu}\psi - m\bar{\psi}\psi}_{\text{Standard Model}} + \underbrace{i\bar{\psi}\gamma_{\mu}a^{\mu}\psi + \bar{\psi}\gamma_{\mu}c^{\mu\nu}\psi}_{\text{couplings with background fields}} \dots$$

Physics of Lorentz violation

- Spectrum distortion,
- **Sidereal time dependence**, etc...

24h 00min 00sec: Solar day

23h 56min 4.1sec: Sidereal day



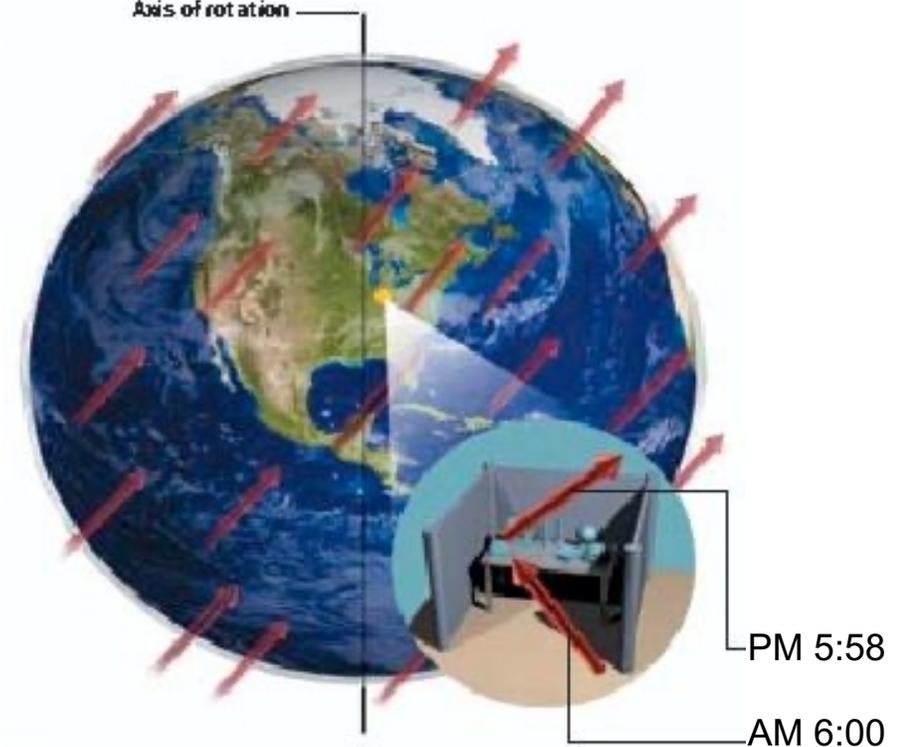
tkatori@cern.ch

Alan Kostelecky, Indiana University

2025 recipient, Norman F. Ramsey Prize

For the development of the Standard Model Extension and for its application to, and inspiration for, a broad set of precision measurement tests across various physical systems, some of which have reached Planck-scale sensitivity.

Scientific American (Sept. 2004)



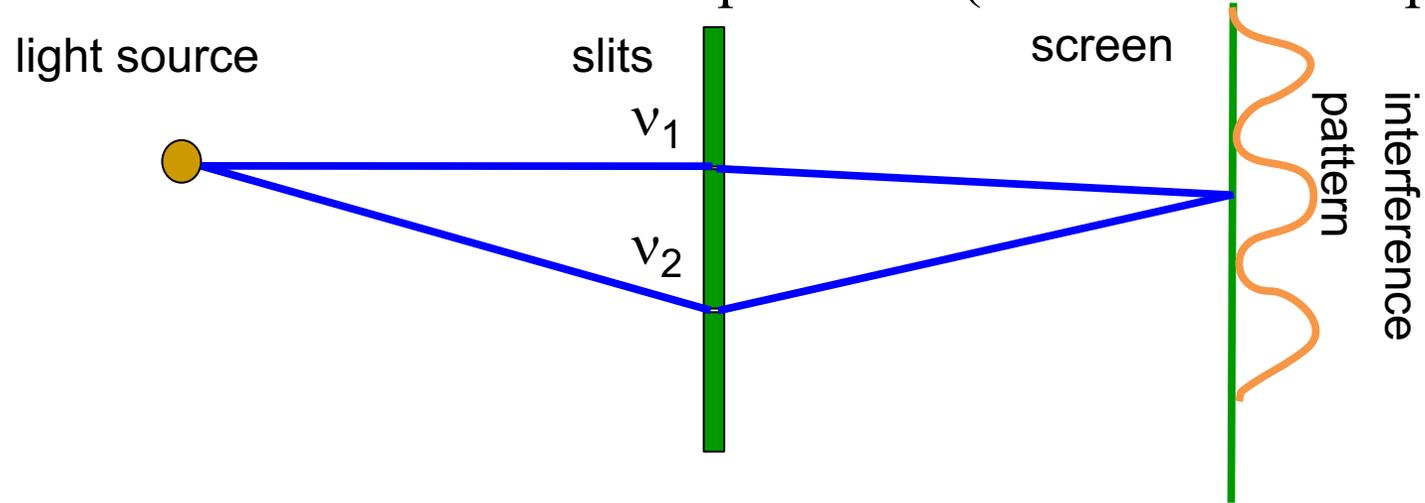
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8

Tests of Lorentz Violation with Neutrinos

Neutrino oscillation experiments

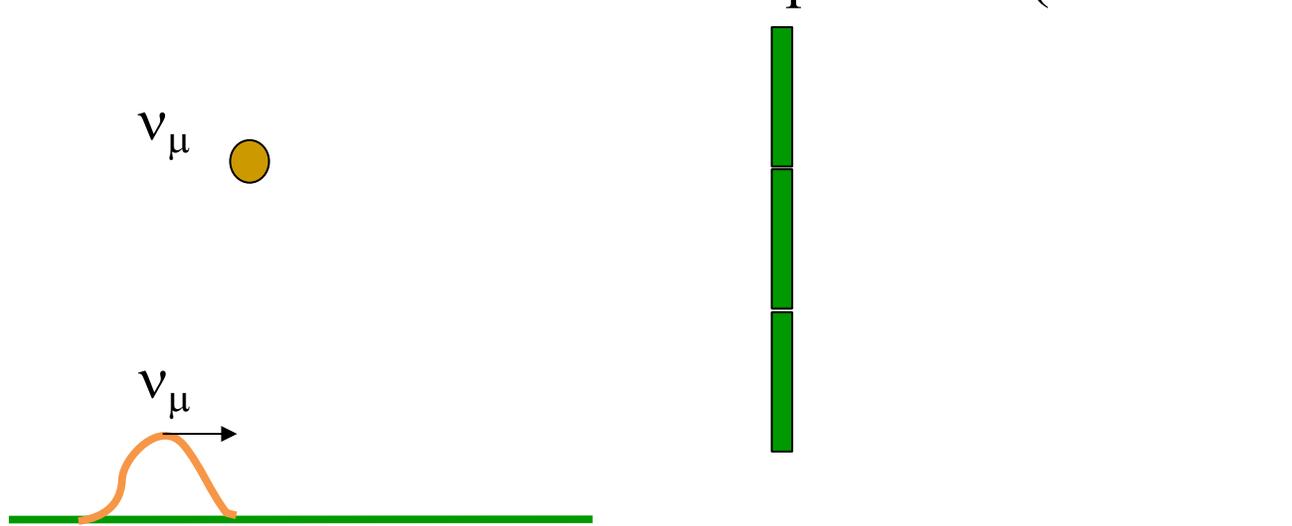
Neutrino oscillation is an interference experiment (cf. double slit experiment)



For double slit experiment, if path v_1 and path v_2 have different length, they have different phases and it causes interference.

Neutrino oscillation experiments

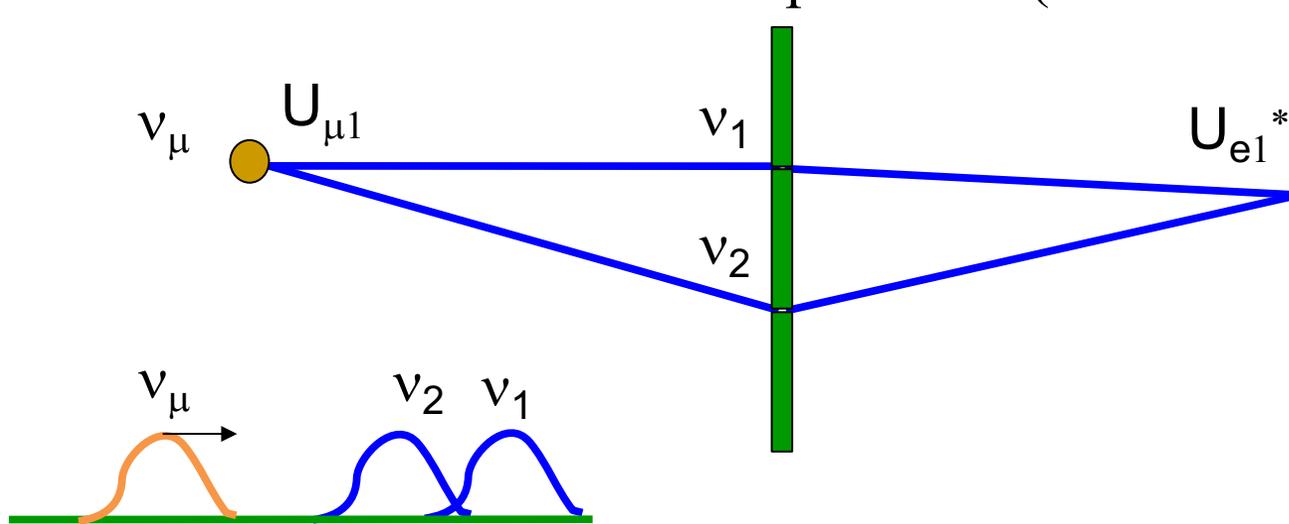
Neutrino oscillation is an interference experiment (cf. double slit experiment)



Neutrino flavour eigenstates are super-position of Hamiltonian eigenstates ν_1 and ν_2

Neutrino oscillation experiments

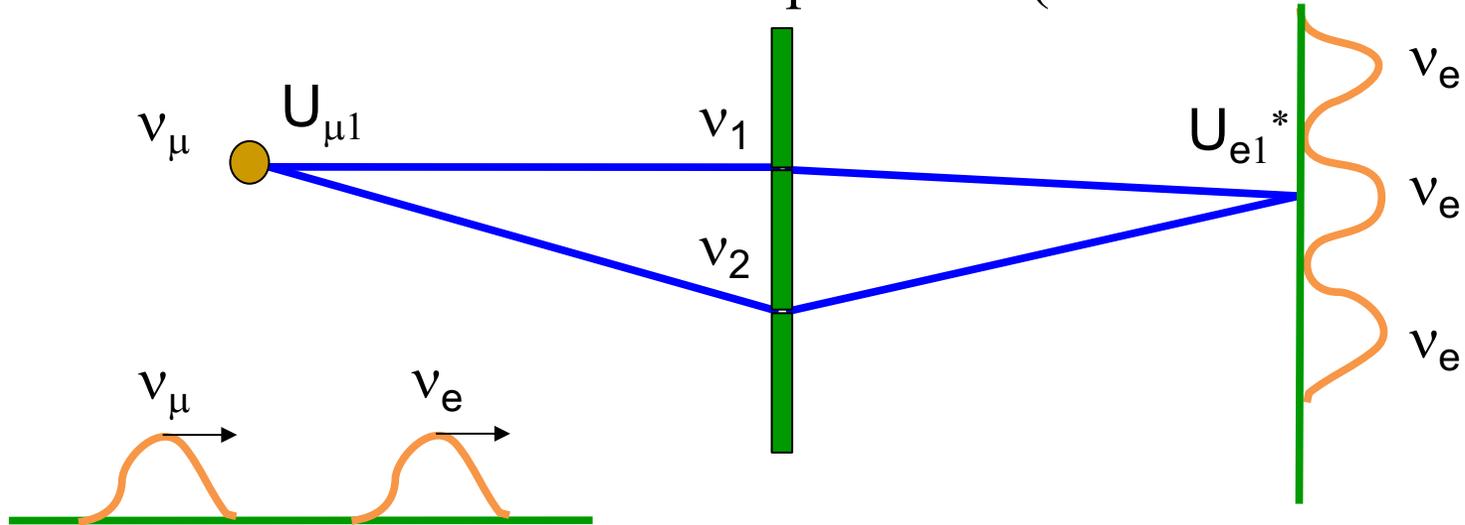
Neutrino oscillation is an interference experiment (cf. double slit experiment)



Neutrino flavour eigenstates are super-position of Hamiltonian eigenstates ν_1 and ν_2
Difference in velocities cause quantum interference

Neutrino oscillation experiments

Neutrino oscillation is an interference experiment (cf. double slit experiment)



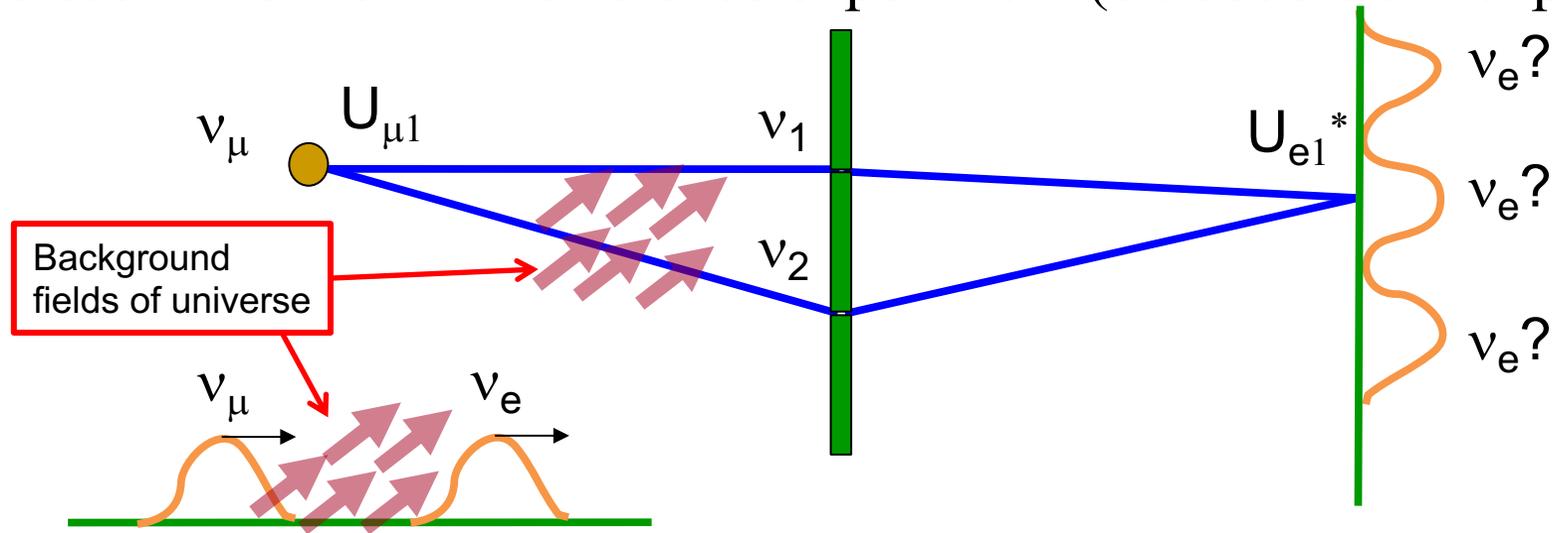
Neutrino flavour eigenstates are super-position of Hamiltonian eigenstates ν_1 and ν_2

Difference in velocities cause quantum interference

The detection may be different flavour (neutrino oscillations)

Neutrino oscillation experiments

Neutrino oscillation is an interference experiment (cf. double slit experiment)



Neutrino flavour eigenstates are super-position of Hamiltonian eigenstates ν_1 and ν_2

Difference in velocities cause quantum interference

The detection may be different flavour (neutrino oscillations)

Neutrino propagation may be affected by background fields

→ anomalous neutrino oscillation results

MiniBooNE ν_e appearance candidate data

Anomalous ν_e candidate low-energy excess

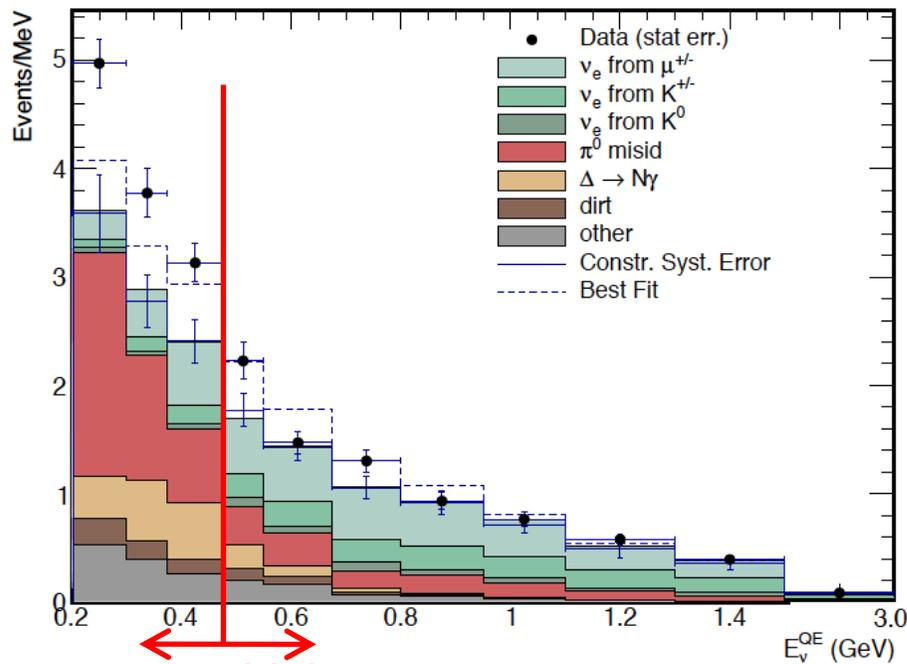
- Can that be Lorentz violation?

→ no sidereal time dependent modulation, unlikely Lorentz violation

	ν -mode BF	2σ limit	$\bar{\nu}$ -mode BF	2σ limit
$ (C)_{e\mu} $	$3.1 \pm 0.6 \pm 0.9$	< 4.2	$0.1 \pm 0.8 \pm 0.1$	< 2.6
$ (A_S)_{e\mu} $	$0.6 \pm 0.9 \pm 0.3$	< 3.3	$2.4 \pm 1.3 \pm 0.5$	< 3.9
$ (A_C)_{e\mu} $	$0.4 \pm 0.9 \pm 0.4$	< 4.0	$2.1 \pm 1.2 \pm 0.4$	< 3.7

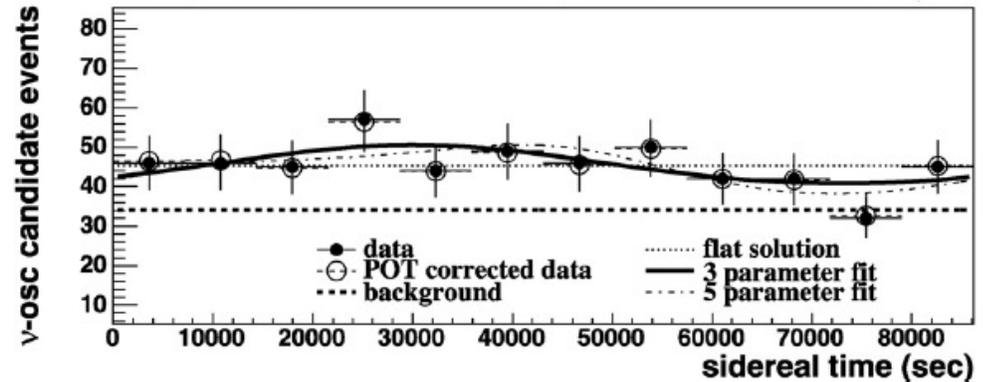
SME coefficients combination (unit 10^{-20} GeV)	
$ (C)_{e\mu} $	$\pm[(a_L)_{e\mu}^T + 0.75(a_L)_{e\mu}^Z] - (E)[1.22(c_L)_{e\mu}^{TT} + 1.50(c_L)_{e\mu}^{TZ} + 0.34(c_L)_{e\mu}^{ZZ}]$
$ (A_S)_{e\mu} $	$\pm[0.66(a_L)_{e\mu}^Y] - (E)[1.33(c_L)_{e\mu}^{TY} + 0.99(c_L)_{e\mu}^{TZ}]$
$ (A_C)_{e\mu} $	$\pm[0.66(a_L)_{e\mu}^X] - (E)[1.33(c_L)_{e\mu}^{TX} + 0.99(c_L)_{e\mu}^{XZ}]$

MiniBooNE low E ν_e excess

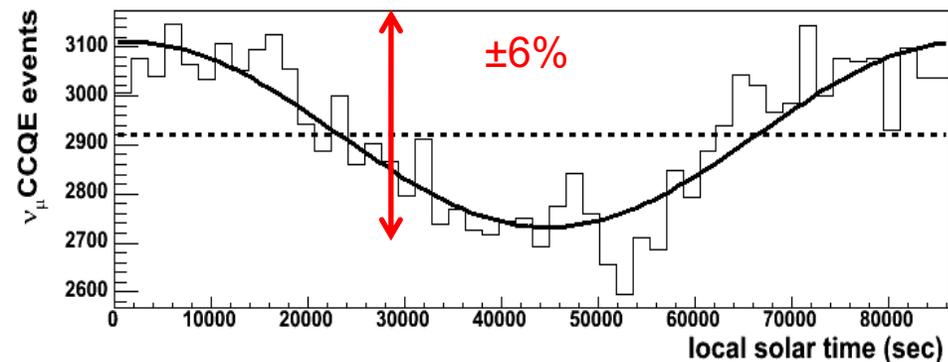


low energy high energy

Neutrino mode ν_e candidate data sidereal time distribution



ν_μ CCQE events day-night distribution



Lorentz violation tests with neutrinos – Summary

Limits of all SME parameters are summarized in tables [ArXiv:0801.0287v17](https://arxiv.org/abs/0801.0287v17)

So far, there is no compelling evidence of Lorentz violation

When do we find it???

28-page limits only in neutrino sector...

Table D31. Neutrino sector, $d=3$ (part 4 of 6)

Combination	Result	System	Ref.
$c_{\mu\mu}^{\mu}$	$(-0.3 \pm 3.0) \times 10^{-30}$ GeV	T2K	[200]
$(A_{\mu\nu})_{\mu}$	$(0.4 \pm 3.0) \times 10^{-30}$ GeV	"	[200]
$(A_{\mu\nu})_{\nu}$	$(0.4 \pm 3.8) \times 10^{-30}$ GeV	"	[200]
$(B_{\mu\nu})_{\mu}$	$(-1.2 \pm 2.6) \times 10^{-30}$ GeV	"	[200]
$(B_{\mu\nu})_{\nu}$	$(2.0 \pm 3.1) \times 10^{-30}$ GeV	"	[200]
$(C_{\mu\nu})_{\mu}^2$	$(10.7 \pm 2.6 \pm 1.3) \times (10^{-19} \text{ GeV})^2$	LSND	[201]
$(C_{\mu\nu})_{\nu}^2 + \frac{1}{2}(A_{\mu\nu})_{\mu}^2 + \frac{1}{2}(A_{\mu\nu})_{\nu}^2$	$(0.9 \pm 2.3 \pm 1.4) \times (10^{-19} \text{ GeV})^2$	"	[201]
$(C_{\mu\nu})_{\mu\nu}^2 + \frac{1}{2}(A_{\mu\nu})_{\mu}^2 + \frac{1}{2}(A_{\mu\nu})_{\nu}^2 + \frac{1}{2}(B_{\mu\nu})_{\mu}^2 + \frac{1}{2}(B_{\mu\nu})_{\nu}^2$	$(10.5 \pm 2.4 \pm 1.4) \times (10^{-19} \text{ GeV})^2$	"	[201]
$ (a_{\mu\nu}^{\mu})_{\mu} $	$< 6.5 \times 10^{-30}$ GeV	SNO	[251]
$ (a_{\mu\nu}^{\mu})_{\nu} $	$< 2.8 \times 10^{-31}$ GeV	"	[251]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} $	$< 1.5 \times 10^{-30}$ GeV	"	[251]
$ \text{Im}(a_{\mu\nu}^{\mu})_{\mu} $	$< 1.7 \times 10^{-31}$ GeV	"	[251]
$(a_{\mu\nu}^{\mu})_{\nu}$	$(-5.6 \pm 8.0) \times 10^{-30}$ GeV	Daya Bay	[252]
$(a_{\mu\nu}^{\mu})_{\mu}$	$(-0.9 \pm 8.0) \times 10^{-30}$ GeV	"	[252]
$\text{Re}(a_{\mu\nu}^{\mu})_{\nu}$	$< 4.1 \times 10^{-30}$ GeV	Super-Kamiokande	[253]
$\text{Im}(a_{\mu\nu}^{\mu})_{\nu}$	$< 2.8 \times 10^{-30}$ GeV	"	[253]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} $	$< 7.8 \times 10^{-30}$ GeV	Double Chooz	[256]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} $	$< 4.4 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} $	$< 9.0 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} $	$< 2.7 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} $	$< 7.8 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 6.6 \times 10^{-30}$ GeV	"	[258]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 7.0 \times 10^{-30}$ GeV	"	[258]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 5.4 \times 10^{-30}$ GeV	"	[258]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 5.4 \times 10^{-30}$ GeV	"	[258]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 2 \times 10^{-7}$ GeV	Leptons, SU(2) _L invariance	[239]*
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 4 \times 10^{-30}$ GeV	"	[239]*
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 8.2 \times 10^{-30}$ GeV	SNO	[251]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 8.4 \times 10^{-31}$ GeV	"	[251]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 2.9 \times 10^{-31}$ GeV	"	[251]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 3.2 \times 10^{-31}$ GeV	"	[251]
$(a_{\mu\nu}^{\mu})_{\nu}$	$(0 \pm 4.5) \times 10^{-30}$ GeV	Daya Bay	[252]
$(a_{\mu\nu}^{\mu})_{\mu}$	$(-0 \pm 4.0) \times 10^{-30}$ GeV	"	[252]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 1.9 \times 10^{-30}$ GeV	Super-Kamiokande	[202]*
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 4.8 \times 10^{-30}$ GeV	T2K	[203]
$ \text{Re}(a_{\mu\nu}^{\mu})_{\mu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu} , \text{Re}(a_{\mu\nu}^{\mu})_{\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Re}(a_{\mu\nu}^{\mu})_{\mu\nu} , \text{Im}(a_{\mu\nu}^{\mu})_{\mu\nu} $	$< 6.3 \times 10^{-30}$ GeV	Super-Kamiokande	[204]*

Spectral distortion



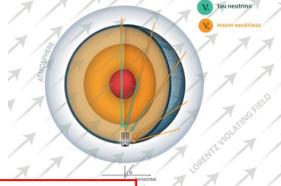
Super-Kamiokande
PRD91(2015)052003



Daya Bay
PRD98(2018)092013

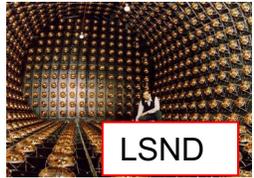


AMANDA
PRD79(2009)102005



IceCube
Nature Physics
14(2018)961

Sidereal variation



LSND
PRD72(2005)076004



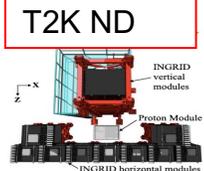
MiniBooNE
PLB718(2013)1303



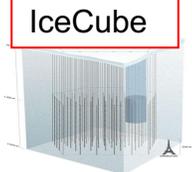
MINOS ND
PRL101(2008)151601



MINOS FD
PRL105(2010)151601



T2K ND
PRD95(2017)111101

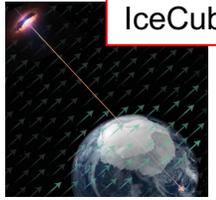


IceCube
PRD82(2010)112003



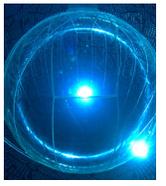
Double Chooz
PRD86(2013)112009

Flavor ratio



IceCube
Nature Physics, 18(2022)1287

Seasonal variation



SNO
PRD98(2018)112013

When do we find Lorentz violation???

Lorentz violation is motivated by Planck scale theories, so it is suppressed with the power of Planck mass ($\sim 10^{19} \text{ GeV}$)

$$\sim \frac{1}{M_{Pl}}, \left(\frac{1}{M_{Pl}}\right)^2, \text{ etc}$$

In effective field theory, **non-renormalizable operators** are the signature of new physics, dimension analysis guides target sensitivity to look for Lorentz violation.

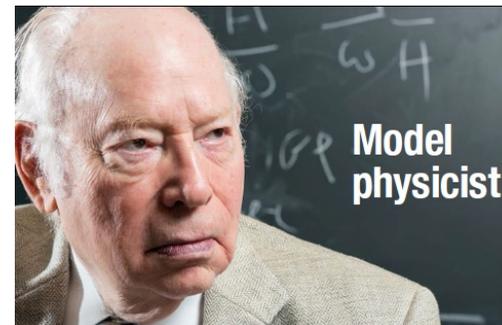
dimension-5 LV operator, $a^{(5)} < 10^{-19} \text{ GeV}^{-1}$

dimension-6 LV operator, $c^{(6)} < 10^{-38} \text{ GeV}^{-2}$

etc

These numbers can be used as a guidance to design new experiments

Steven Weinberg
([CERN Courier Nov. 2017](#))



“We don’t know anything about non-renormalizable interaction terms, but I’ll swear they are there!”

Tests of Lorentz violation with astrophysical neutrinos

Terrestrial experiments

- controlled, high-precision

So far, no compelling evidence of Lorentz violation

Atmospheric, astrophysical, and cosmological experiments

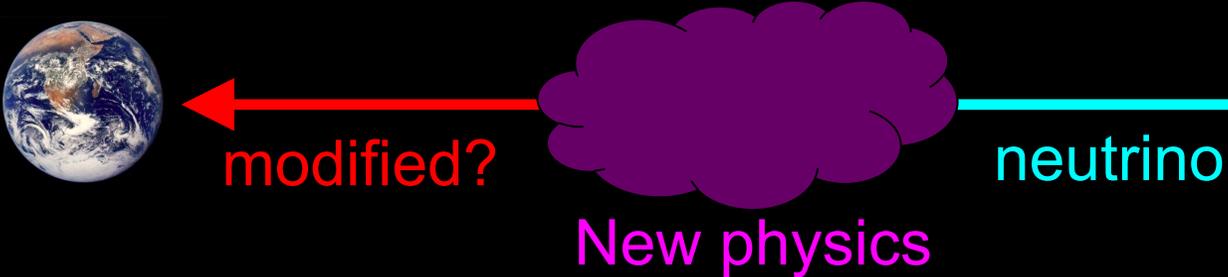
- not controlled, low-precision
- extreme systems (high energy, long propagation, etc)
- **more sensitive to nonrenormalizable operators**

Tests of Lorentz Violation with Astrophysical Neutrinos

Astrophysical neutrinos

Long, straight trajectory propagation in vacuum

- Astrophysical neutrinos are sensitive to tiny space-time effects

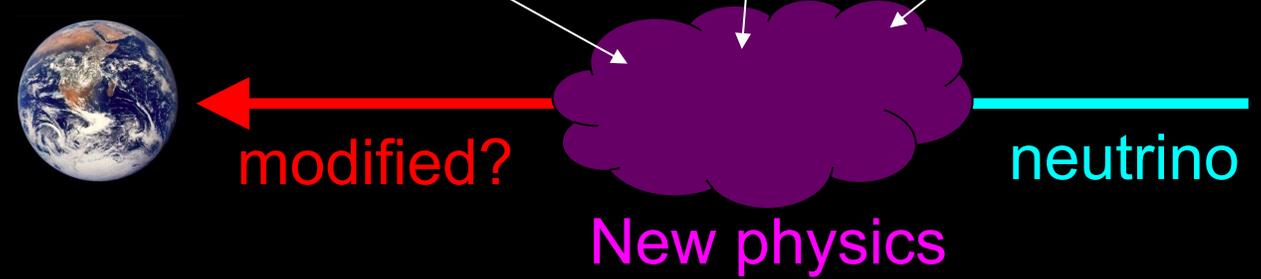
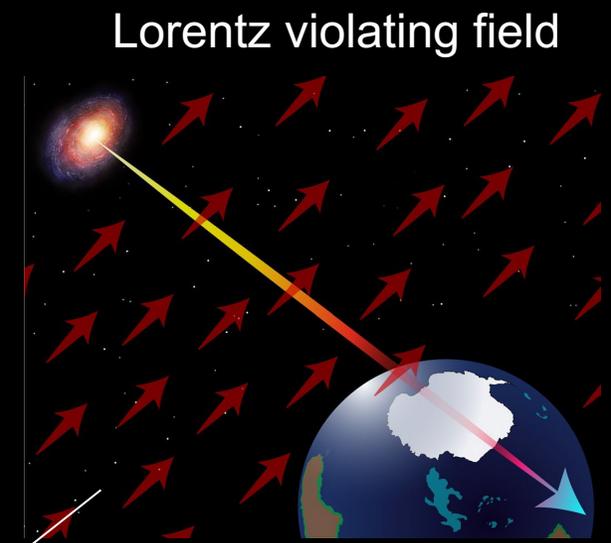
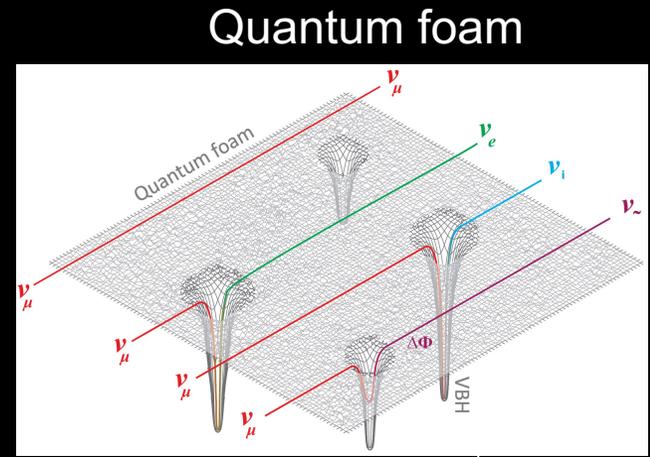


Astrophysical neutrinos

- Long, straight trajectory propagation in vacuum
- Astrophysical neutrinos are sensitive to tiny space-time effects

Long list of new models to affect astrophysical neutrino propagation

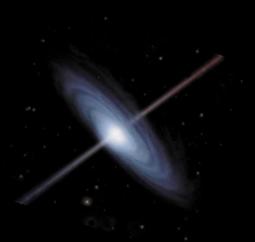
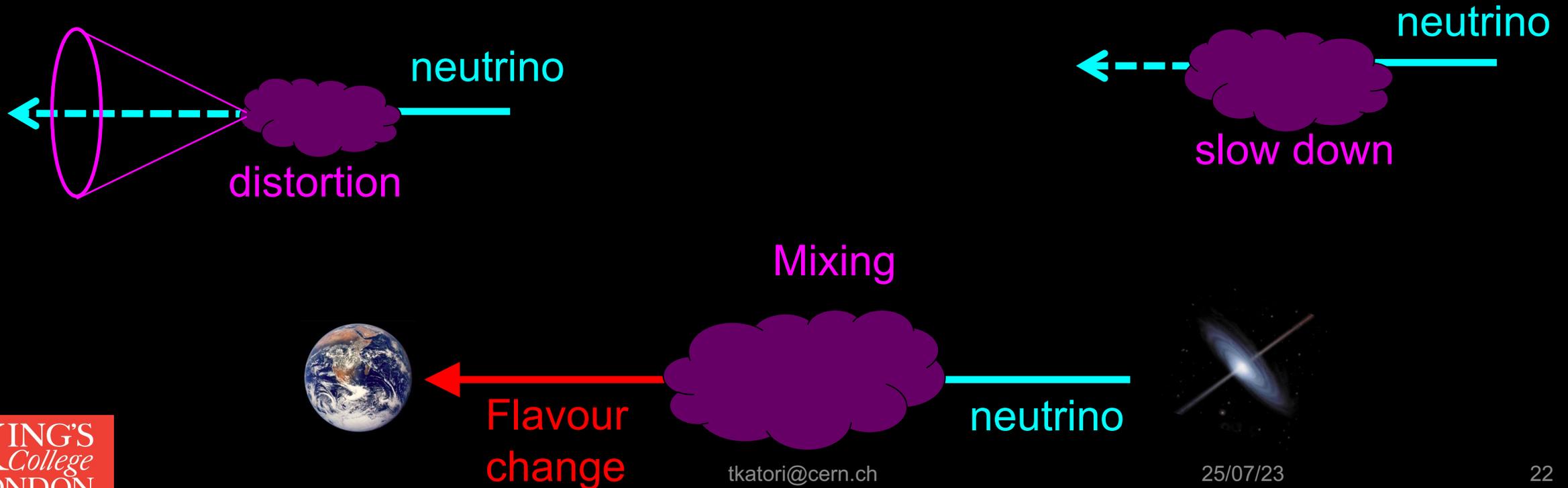
- Long range force
- Neutrino-dark matter coupling
- Neutrino-dark energy coupling
- etc



Test of Spacetime properties with Astrophysical neutrinos

Lorentz violation = Media in vacuum

- Spectrum distortion (energy)
- Time of Flight (time)
- Anomalous mixing (flavour)



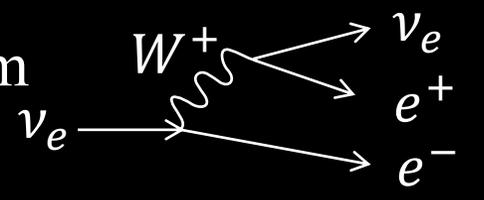
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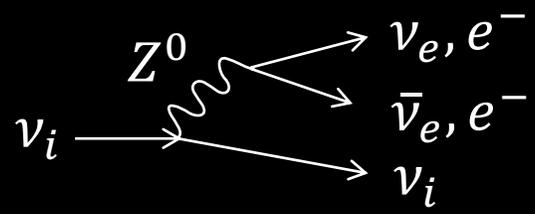
Test of Spacetime properties with Astrophysical neutrinos

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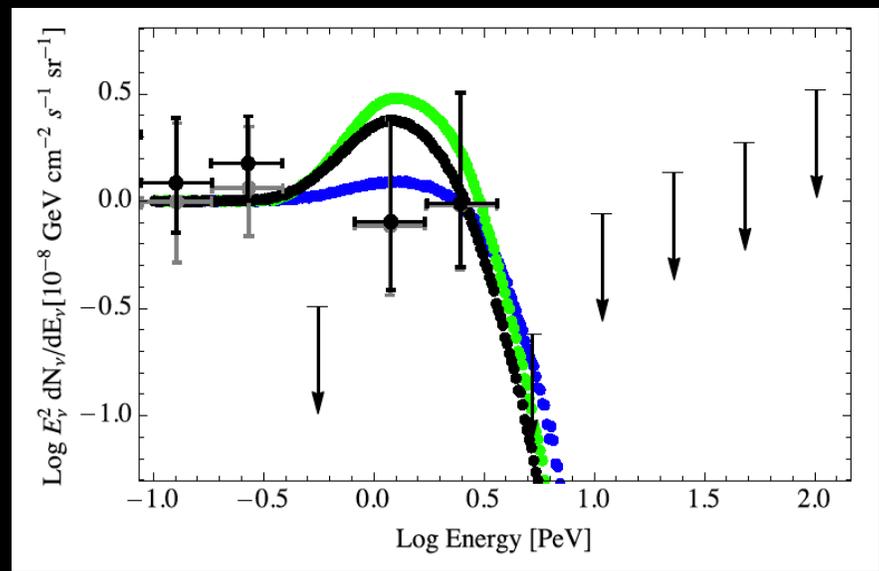


Vacuum pair emission



Neutrino splitting

Diffuse neutrino spectrum distortion



Lorentz violating field cause radiation in vacuum

- High-energy neutrinos are attenuated
- KM3NeT 220 PeV neutrino (KM3-230213A)

$$\delta \equiv c_\nu^2 - 1 < 4 \times 10^{-22}$$



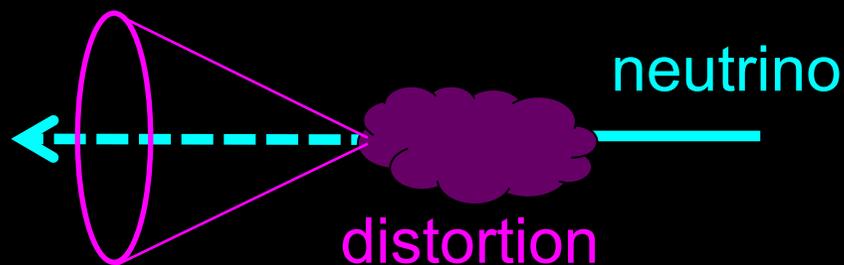
Test of Spacetime properties with Astrophysical neutrinos

Lorentz violation = Media in vacuum

- Spectrum distortion (energy)
- Time of Flight (time)
- Anomalous mixing (flavour)

Spectrum distortion happen by other scenarios

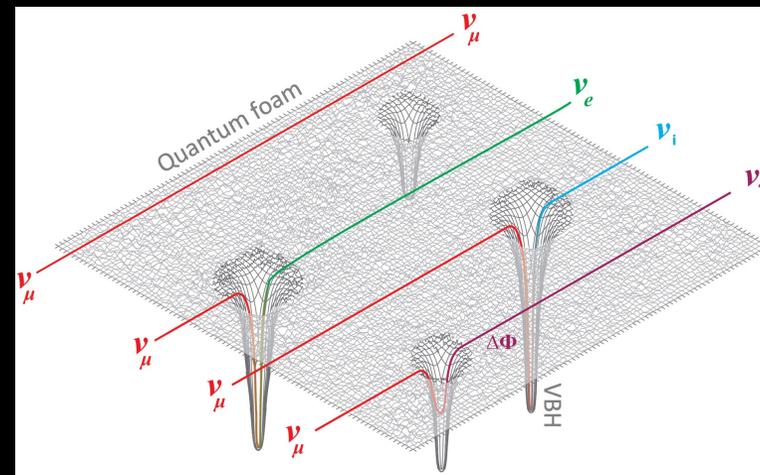
- “missing” neutrinos by micro black-hole (neutrino-loss quantum decoherence)
- Strong limits from SN1987A (cf. neutrino decay)



Lorentz violating field cause radiation in vacuum

- High-energy neutrinos are attenuated
- KM3NeT 220 PeV neutrino (KM3-230213A)

$$\delta \equiv c_v^2 - 1 < 4 \times 10^{-22}$$



Test of Spacetime properties with Astrophysical neutrinos

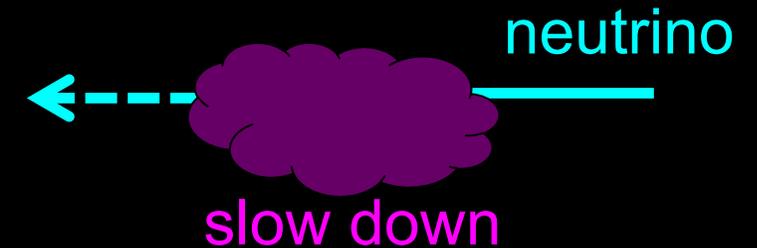
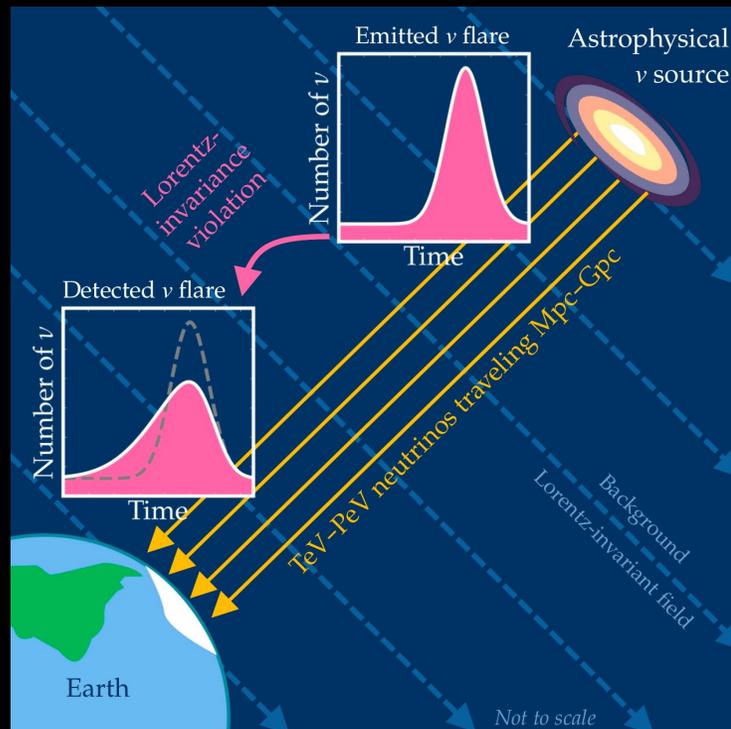
New physics search

- Spectrum distortion (energy)
- **Time of Flight (time)**
- Anomalous mixing (flavour)

Modified dispersion due to quantum foam
cause unexpected delay/advance for neutrinos

- Neutrino time-of-flight ($a^{(5)}$ =CPT odd)

$$\delta v \sim E a^{(5)} + E^2 c^{(6)} + \dots$$



Time distribution is modified due to
Lorentz violation (energy-dependent)

Test of Spacetime properties with Astrophysical neutrinos

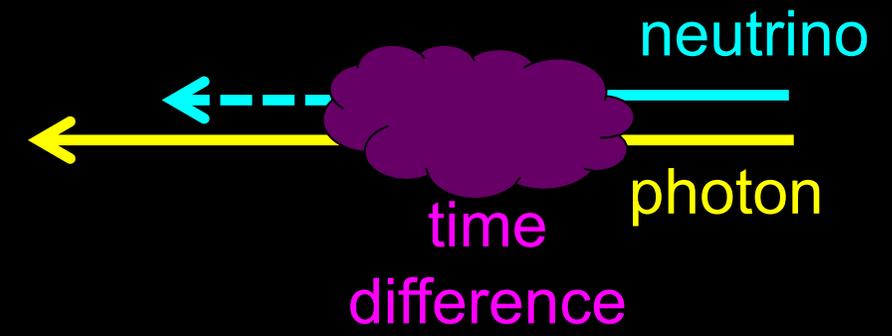
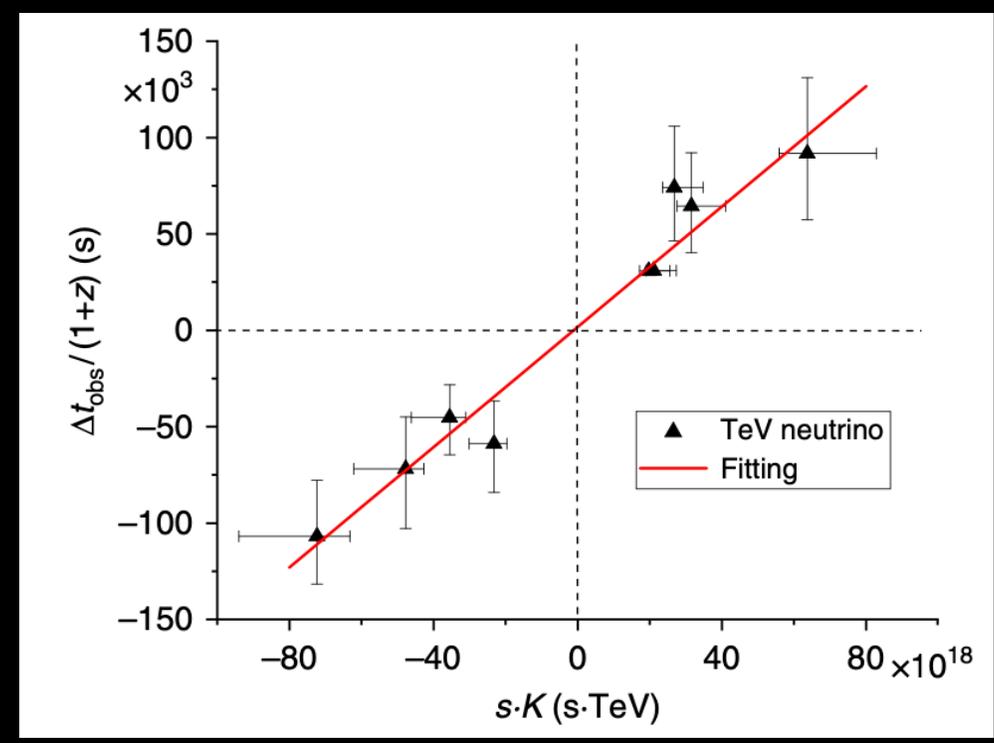
New physics search

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Neutrinos and gamma-ray bursts may have coincidence with Lorentz violation

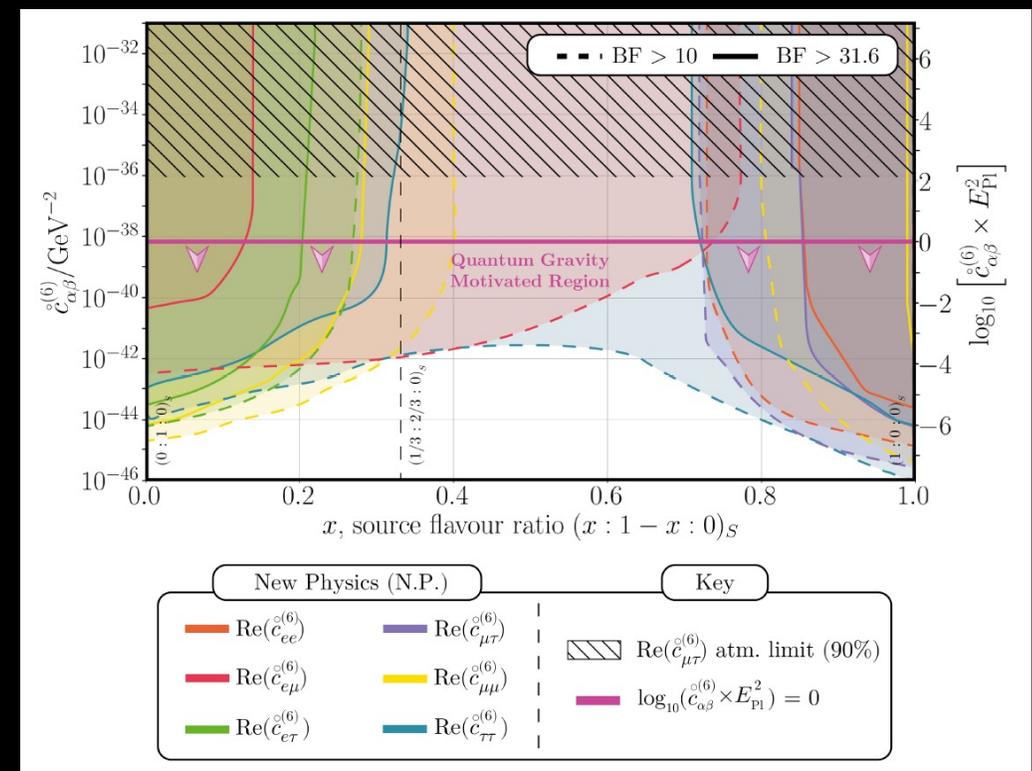
Test of Spacetime properties with Astrophysical neutrinos

New physics search

- Spectrum distortion (energy)
- Time of Flight (time)
- **Anomalous mixing (flavour)**

Flavour effect

- Macroscopic quantum effect and sensitive to small effects
- Sensitive to the target signal region of Lorentz violation ($< 10^{-38} \text{ GeV}^{-2}$ for dim-6 operators)



← **Flavour change**



Mixing

→ **Neutrino**



Lorentz violation limits from tabletop to cosmology



Physics MMA

Lower dimension operators \rightarrow searches by tabletop experiments
 Higher dimension operators \rightarrow searches by astrophysical observations

$$H \sim \frac{m^2}{2E} + a^{(3)} - E \cdot c^{(4)} + E^2 \cdot a^{(5)} - E^3 \cdot c^{(6)} \dots$$



torsion pendulum



optical resonator



comagnetometer



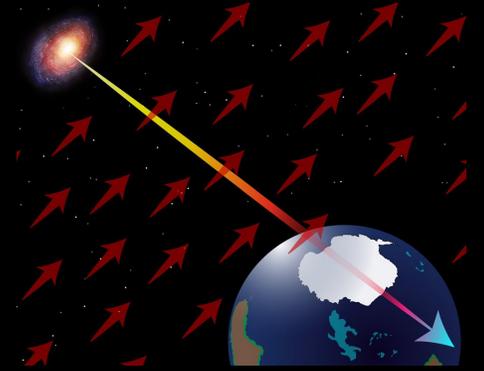
vacuum birefringence



UHECRs

dim.	method	type	sector	limits	ref.
$\hat{a}^{(3)}$	CMB polarization	astrophysical	photon	$\sim 10^{-43}$ GeV	[2]
	He-Xe comagnetometer	tabletop	neutron	$\sim 10^{-34}$ GeV	[3]
	torsion pendulum	tabletop	electron	$\sim 10^{-31}$ GeV	[4]
	muon g-2	accelerator	muon	$\sim 10^{-24}$ GeV	[5]
	neutrino mixing	astrophysical	neutrino	$\sim 10^{-26}$ GeV	[1]
$\hat{c}^{(4)}$	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-38}$	[6]
	Laser interferometer	LIGO	photon	$\sim 10^{-22}$	[7]
	Sapphire cavity oscillator	tabletop	photon	$\sim 10^{-18}$	[8]
	Ne-Rb-K comagnetometer	tabletop	neutron	$\sim 10^{-29}$	[9]
	trapped Ca^+ ion	tabletop	electron	$\sim 10^{-19}$	[10]
	neutrino mixing	astrophysical	neutrino	$\sim 10^{-31}$	[1]
$\hat{a}^{(5)}$	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-34}$ GeV $^{-1}$	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-22}$ to 10^{-18} GeV $^{-1}$	[11]
	neutrino mixing	astrophysical	neutrino	$\sim 10^{-37}$ GeV $^{-1}$	[1]
$\hat{c}^{(6)}$	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-31}$ GeV $^{-2}$	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-42}$ to 10^{-35} GeV $^{-2}$	[11]
	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-31}$ GeV $^{-2}$	[12]
	neutrino mixing	astrophysical	neutrino	$\sim 10^{-42}$ GeV $^{-2}$	[1]

Astrophysical neutrino flavour Lorentz violation limits



Weak interaction
 + Small mass
 + Quantum mixing
 = macroscopic quantum system you cannot disturb

Tests of Lorentz Violation with Astrophysical Neutrinos – Summary

Astrophysical neutrinos have high potential to look for Lorentz violation. But there are many unknowns;

- Energy spectrum
- Production time
- Source information
- Foreground

etc

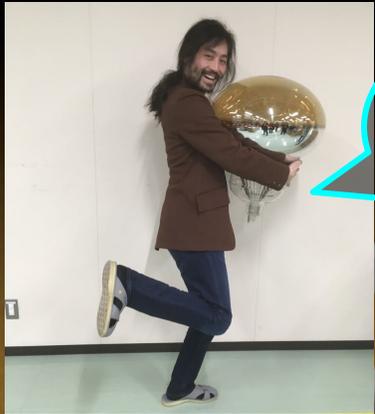
So far, astrophysical neutrino data are low statistics, and further data are needed to search Lorentz violation...

Hyper-Kamiokande and IceCube-Gen2

Summer
2024-2045
IceCube team



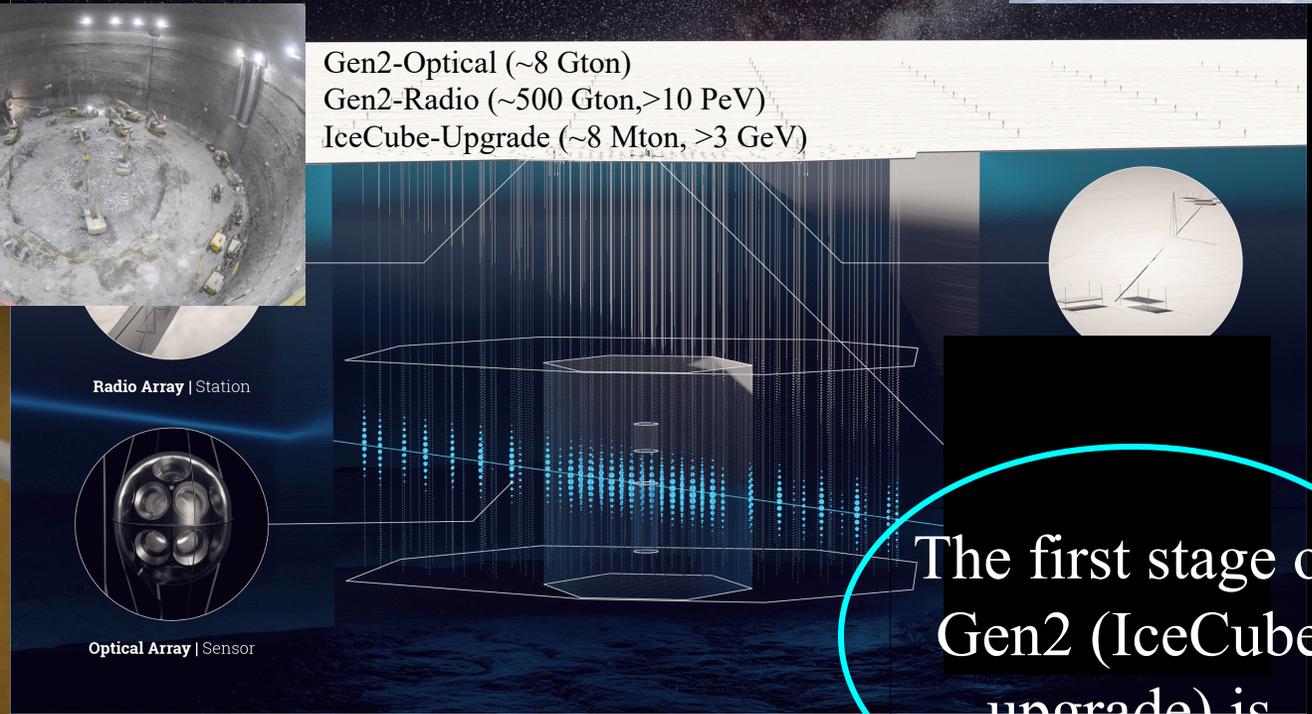
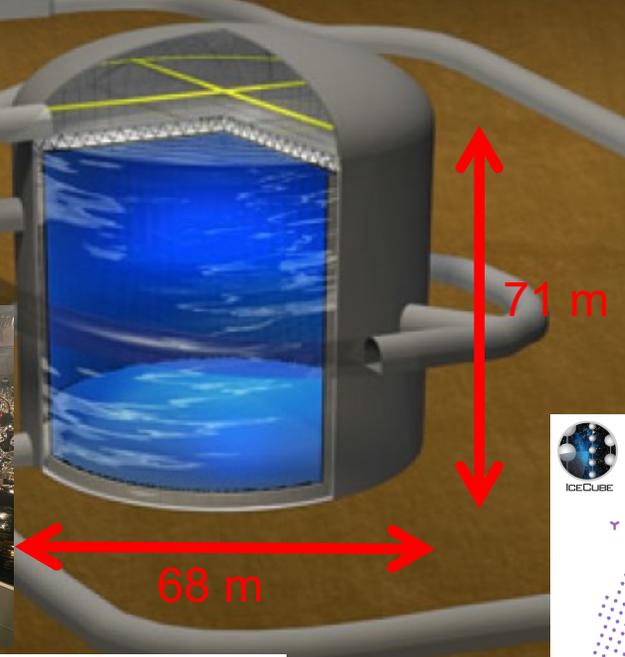
New international neutrino astronomy projects around the world



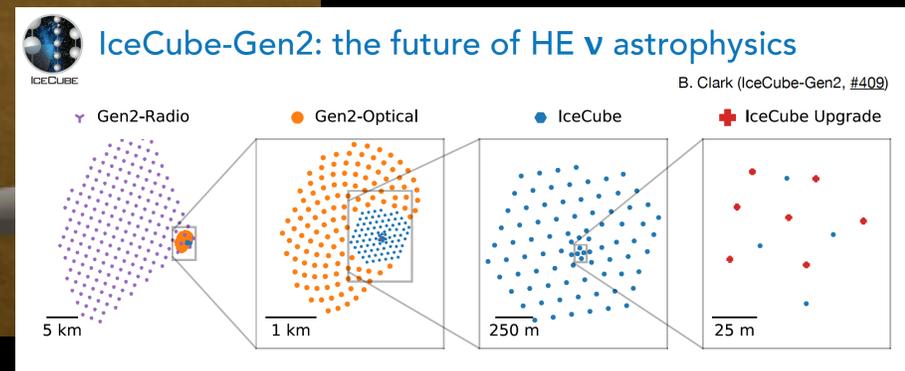
Hyper-K
construction
is ongoing



Gen2-Optical (~8 Gton)
Gen2-Radio (~500 Gton, >10 PeV)
IceCube-Upgrade (~8 Mton, >3 GeV)



The first stage of
Gen2 (IceCube
upgrade) is
ongoing



Conclusion

Lorentz violation is motivated from Planck-scale theories

There is a worldwide effort to look for Lorentz violation, using various state-of-the-art techniques including neutrinos, but so far, no compelling evidence of Lorentz violation

Astrophysical neutrinos are powerful tools to look for Lorentz violation

Thank you for your attention!



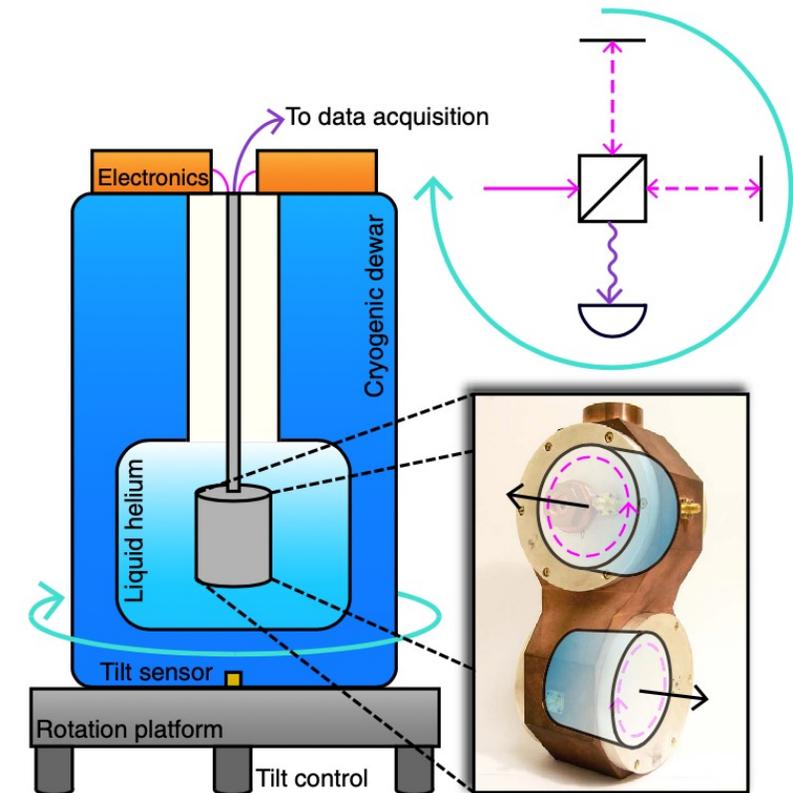
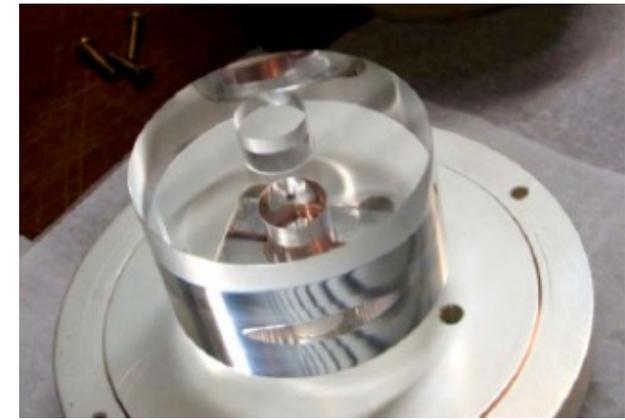
Backup

Optical cavity experiment

Modern Michelson-Morley experiment

- Sapphire crystal resonator
- Whispering gallery mode
- Vacuum insulation, liquid helium cooling to 4K
- Turntable to actively rotate

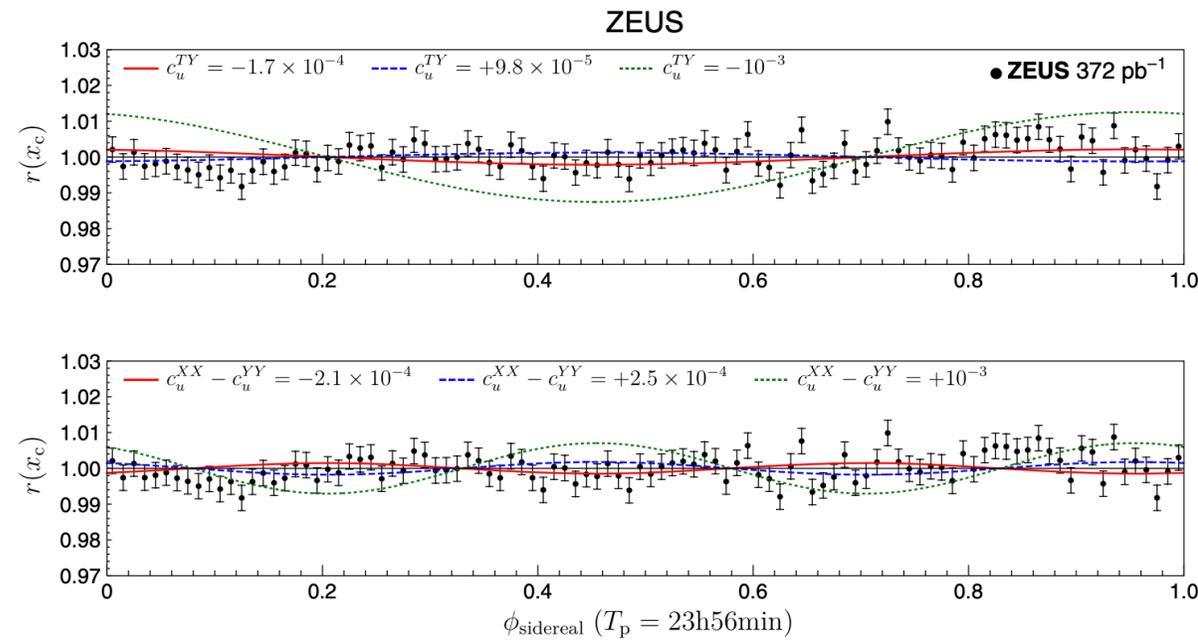
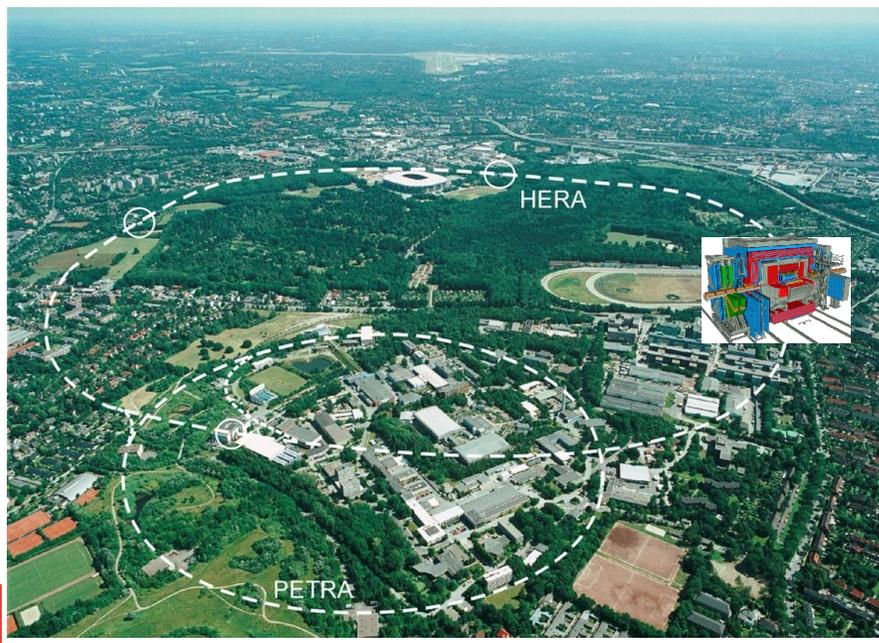
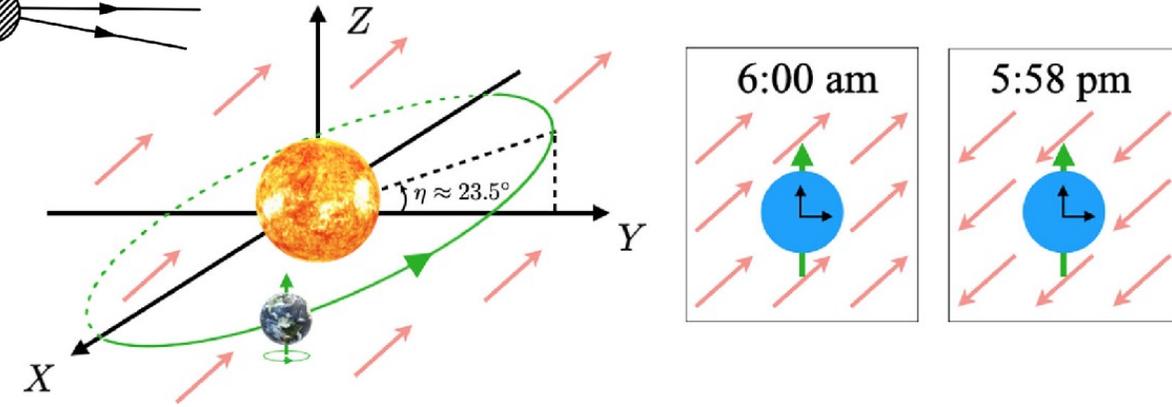
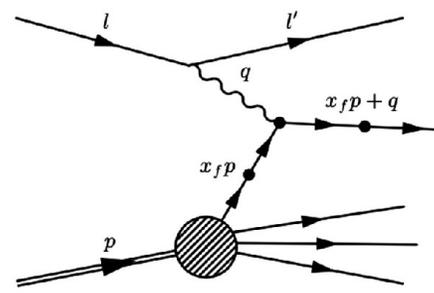
This experiment is sensitive to the anisotropy of speed of light down to $\Delta c/c \sim 10^{-18}$



Collider physics (quarks)

HERA p-e⁻ collider

- ZEUS deep-inelastic scattering data
- Monitor sidereal time dependence
- LV tests of quarks



Models of Lorentz violation

String theory, [Kostelecký and Samuel, PRD39 \(1989\) 683](#)

Ultra-light dark matter, [Graham and Rajendran, PRD88 \(2013\) 035023](#)

Quintessence, [Ando, Kamionkowski, and Mocioiu, PRD80 \(2009\) 123522](#)

Loop quantum gravity, [Gambini and Pullin, PRD59 \(1999\) 124021](#)

Non-commutative field theory, [Carroll, Harvey, Kostelecký, Lane, Okamoto, PRL87 \(2001\) 141601](#)

Hořava-Lifshitz gravity, [Pospelov and Shang, PRD85 \(2012\) 105001](#)

Lee-Wick theory, [Myers and Pospelov, PRL90 \(2003\) 211601](#)

and many more!

Effective Lorentz violation (spontaneous Lorentz symmetry breaking) is compatible with Riemann geometry, however, Intrinsic Lorentz Violation is not

Finsler geometry [Kostelecký and Li, PRD104 \(2021\) 044054](#) got lots of attention recently, to go beyond Riemann geometry

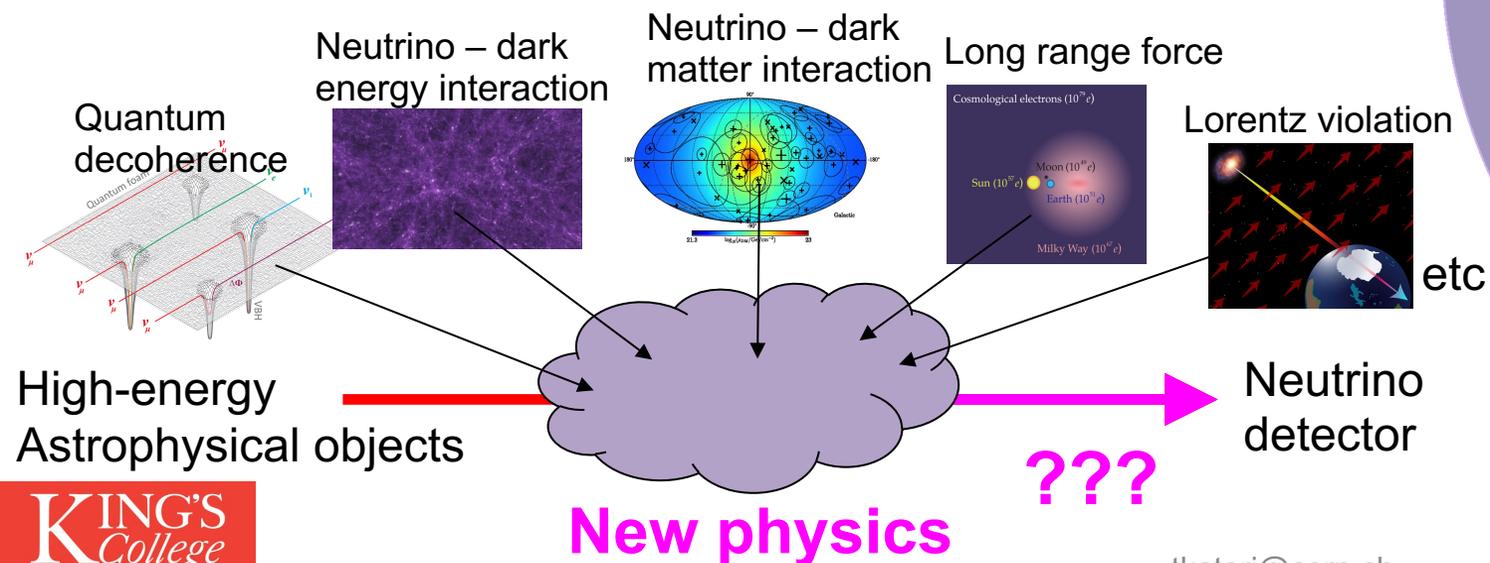
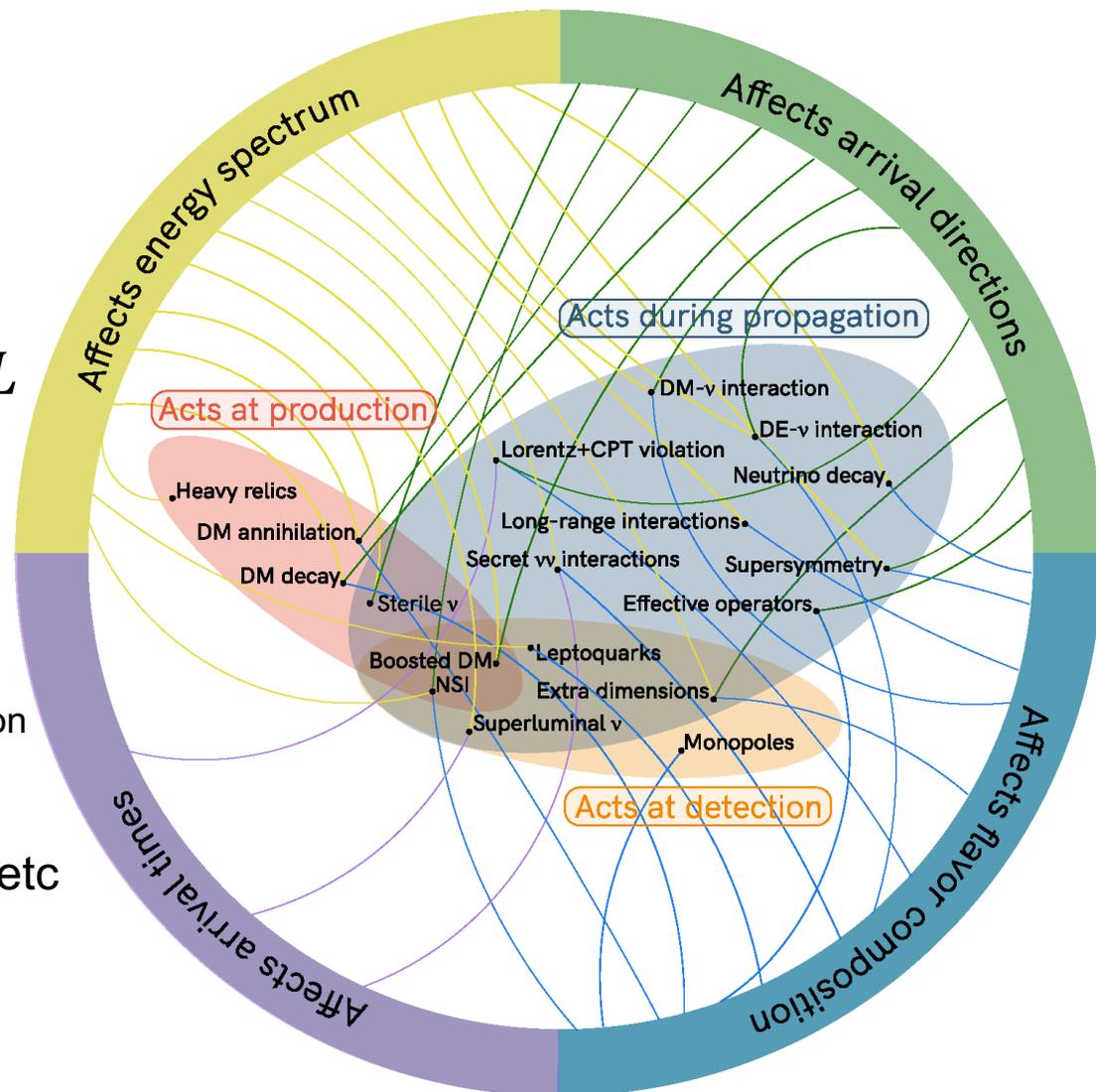
High-energy, long propagating neutrinos

High-energy astrophysical neutrinos

- Long baseline accumulates new physics effect
- High energy enhances new physics effect

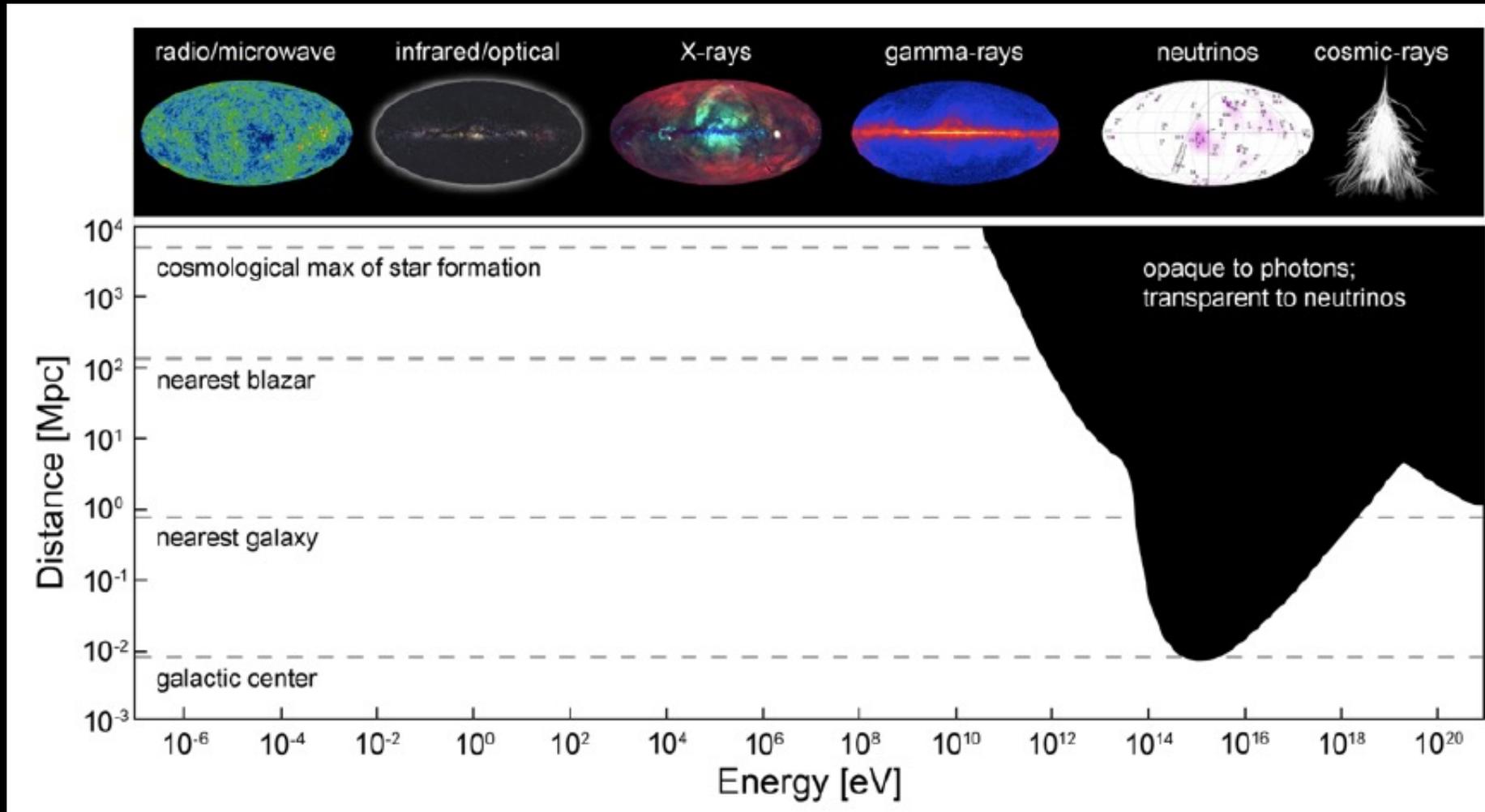
$$H \sim \frac{m^2}{2E} + V(\text{new physics}), P \sim V(\text{new physics}) \cdot L$$

- Energy spectrum, arrival time, **flavor** are affected by production, **propagation**, detection of neutrinos



High-energy astrophysical neutrinos

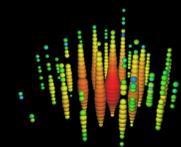
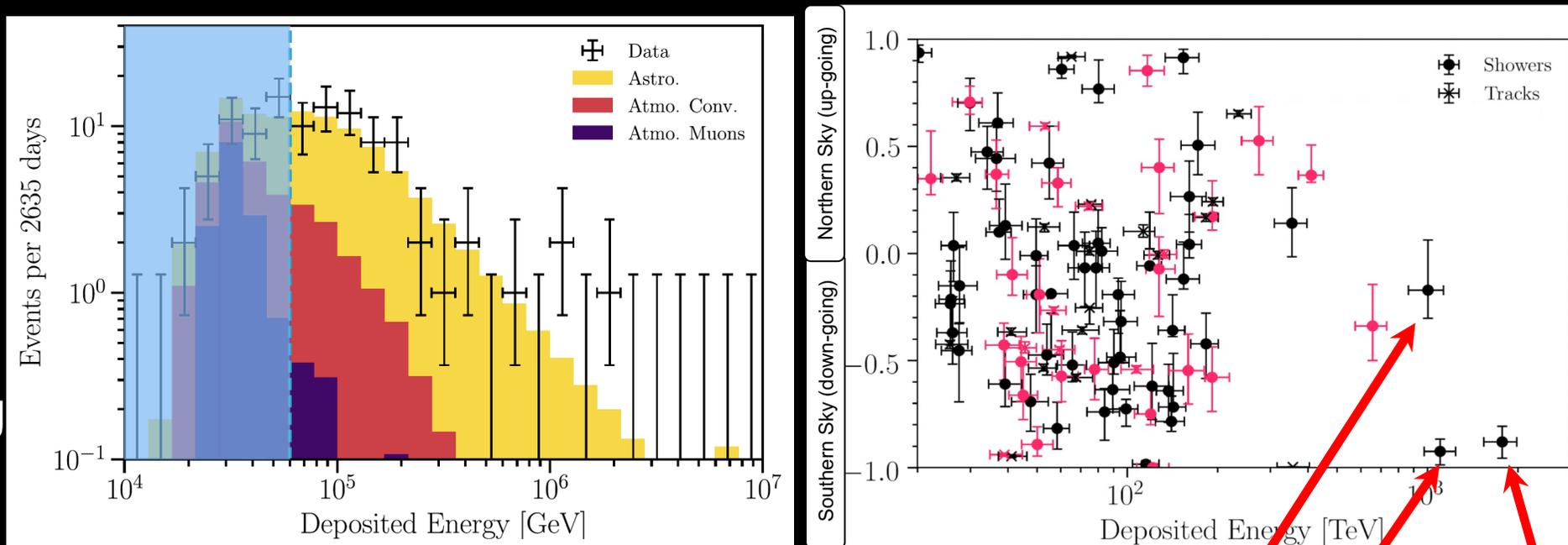
Above ~ 100 TeV, neutrinos are only particles pointing to their high-energy sources



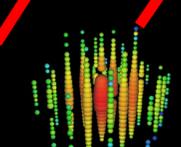
High-energy astrophysical neutrinos

60TeV- 2PeV astrophysical neutrinos are observed by IceCube Neutrino Observatory
 high-energy starting event (HESE) sample

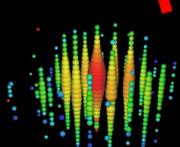
2. Hig



“Bert”
1.1 PeV



“Ernie”
1.0 PeV
25/07/23



“Big Bird”
2.0 PeV

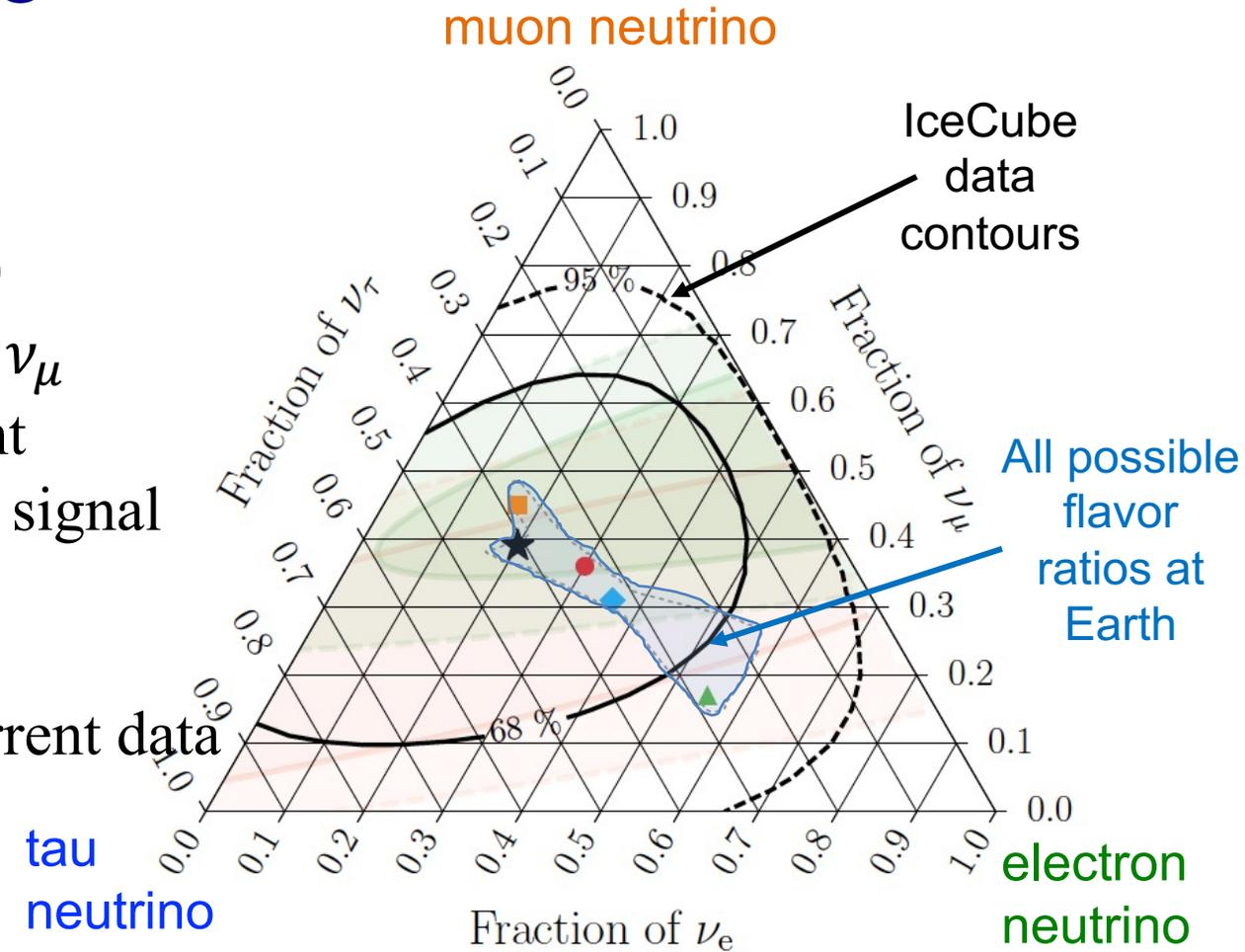
High-energy, long propagating neutrinos

Astrophysical neutrino flavor physics

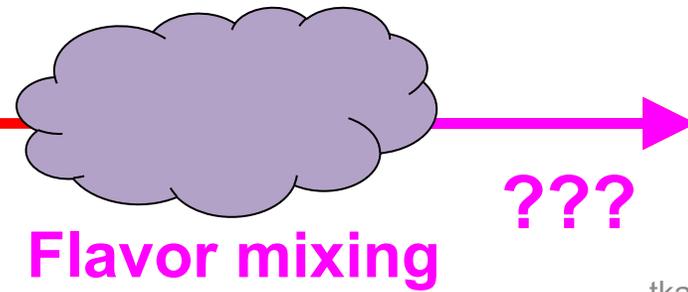
- Flavor triangle
- Spectrum integrated flavor ratio ($\nu_e : \nu_\mu : \nu_\tau$)
- Standard production models include ν_e and ν_μ
- Flavor ratio observables on Earth is different
- Deviation from this “island” is new physics signal

Data contour covers most of flavor triangle

- New physics cannot be discovered from current data
- Limits are set on vacuum operators



High-energy Astrophysical



—	HESE with ternary topology ID	$\nu_e : \nu_\mu : \nu_\tau$ at source \rightarrow on Earth:
★	Best fit: 0.20 : 0.39 : 0.42	■ 0:1:0 \rightarrow 0.17 : 0.45 : 0.37
■	Global Fit (IceCube, APJ 2015)	● 1:2:0 \rightarrow 0.30 : 0.36 : 0.34
■	Inelasticity (IceCube, PRD 2019)	▲ 1:0:0 \rightarrow 0.55 : 0.17 : 0.28
.....	3 ν -mixing 3 σ allowed region	

tkatori@cern.ch 25/07/23

HESE 7.5-yr flavor Lorentz violation search

dim-6 new physics operator limit

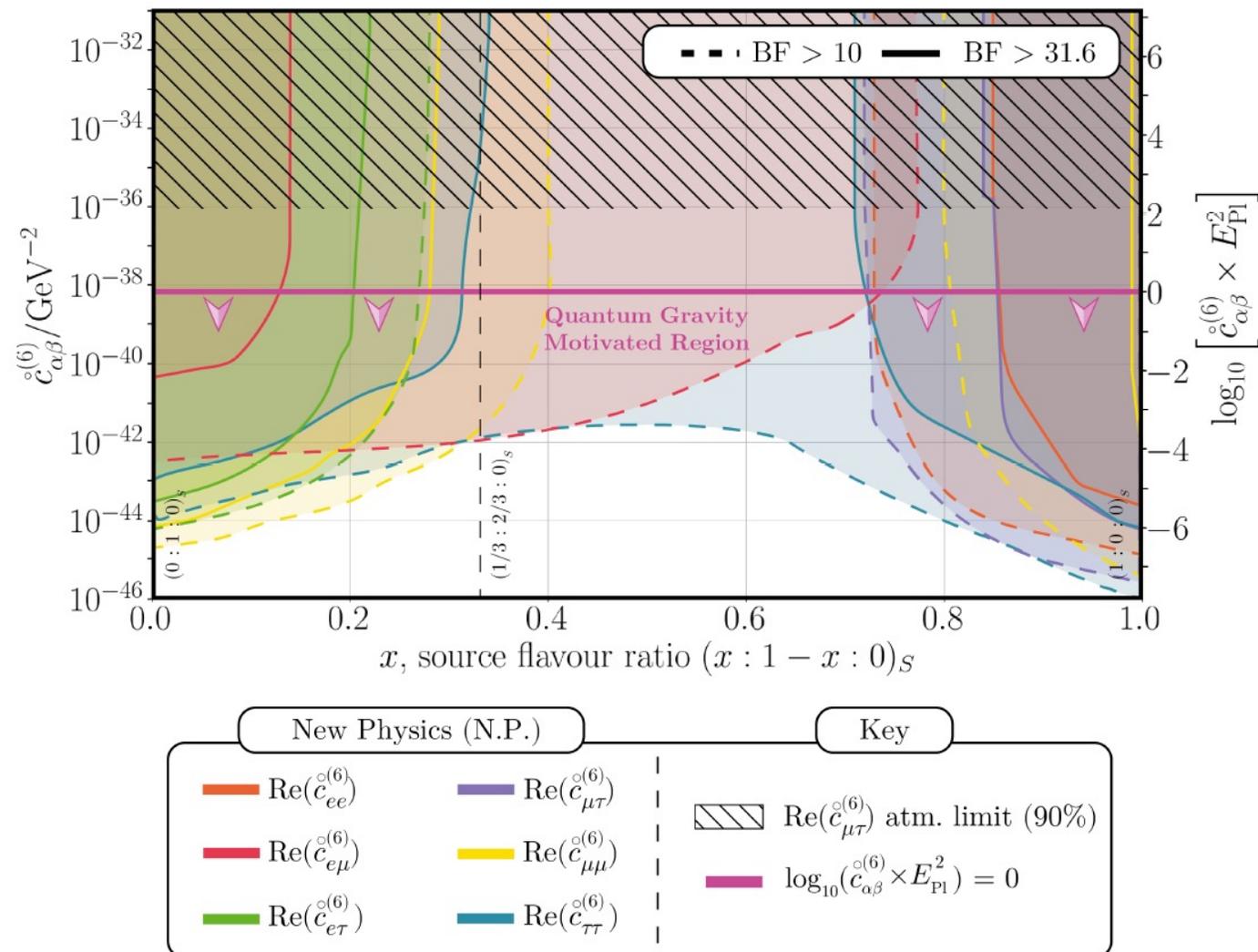
60 HESE events in 60 TeV – 2 PeV

IceCube data start to explore quantum gravity-motivated signal region for some parameters

$$c^{(6)} \leq \frac{1}{M_{Planck}^2} \sim 10^{-38} GeV^{-2}$$

dim coefficient limit (BF > 10.0)

3	$Re(\overset{\circ}{a}_{\tau\tau}^{(3)})$	$2 \times 10^{-26} GeV$
4	$Re(\overset{\circ}{c}_{\tau\tau}^{(4)})$	2×10^{-31}
5	$Re(\overset{\circ}{a}_{\tau\tau}^{(5)})$	$2 \times 10^{-37} GeV^{-1}$
6	$Re(\overset{\circ}{c}_{\tau\tau}^{(6)})$	$3 \times 10^{-42} GeV^{-2}$
7	$Re(\overset{\circ}{a}_{\tau\tau}^{(7)})$	$3 \times 10^{-47} GeV^{-3}$
8	$Re(\overset{\circ}{c}_{\tau\tau}^{(8)})$	$2 \times 10^{-52} GeV^{-4}$



Flavor new physics search with effective operators

Standard Model Extension (SME) is an effective field theory to look for Lorentz violation

$$L = i\bar{\psi}\gamma^\mu\partial_\mu\psi - m\bar{\psi}\psi + \bar{\psi}\gamma^\mu a_\mu\psi + \bar{\psi}\gamma^\mu c_{\mu\nu}\partial^\nu\psi \dots$$

Standard Model New physics

Effective Hamiltonian can be written from here

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + a_{\alpha\beta}^{(3)} - E c_{\alpha\beta}^{(4)} + E^2 a_{\alpha\beta}^{(5)} - E^3 c_{\alpha\beta}^{(6)} \dots$$

Standard Model New physics (renormalizable) higher dimension operator (non-renormalizable)

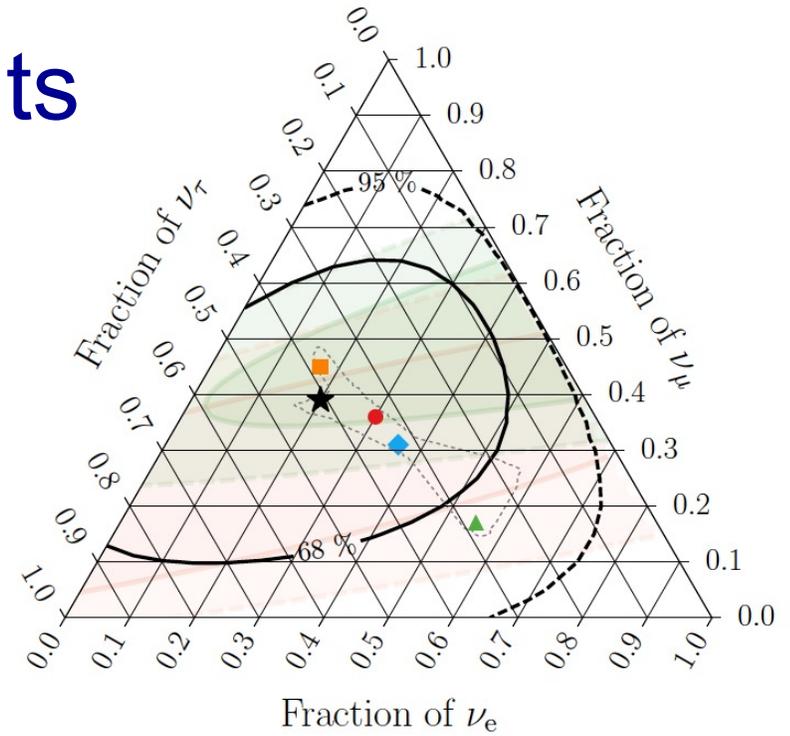
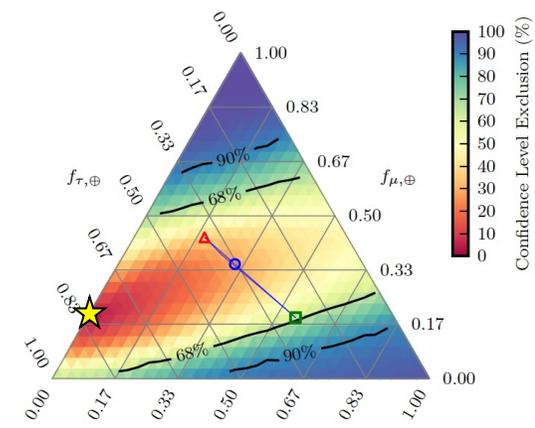
$$E^3 c_{\alpha\beta}^{(6)} = E^3 \begin{pmatrix} c_{ee}^{(6)} & c_{e\mu}^{(6)} & c_{\tau e}^{(6)} \\ c_{e\mu}^{(6)*} & c_{\mu\mu}^{(6)} & c_{\mu\tau}^{(6)} \\ c_{\tau e}^{(6)*} & c_{\mu\tau}^{(6)*} & c_{\tau\tau}^{(6)} \end{pmatrix}$$

IceCube is sensitive to higher dimension operators

dimension-6 operator natural scale: $c^{(6)} \sim \frac{1}{M_{Planck}^2} \sim 10^{-38} GeV^{-2}$

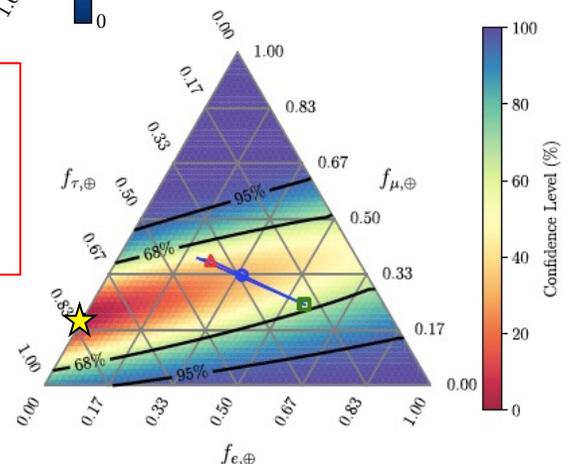
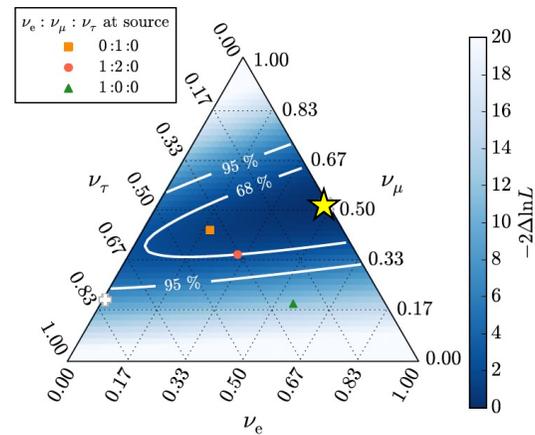
IceCube flavor ratio measurements

**IceCube
1st flavour ratio result
(0.0:0.2:0.8)**



- HESE with ternary topology ID
 - ★ Best fit: 0.20 : 0.39 : 0.42
 - Global Fit (IceCube, APJ 2015)
 - Inelasticity (IceCube, PRD 2019)
 - ⋯ 3ν-mixing 3σ allowed region
- | $\nu_e : \nu_\mu : \nu_\tau$ at source | → on Earth: |
|--|----------------------|
| 0:1:0 | → 0.17 : 0.45 : 0.37 |
| 1:2:0 | → 0.30 : 0.36 : 0.34 |
| 1:0:0 | → 0.55 : 0.17 : 0.28 |
| 1:1:0 | → 0.36 : 0.31 : 0.33 |

**IceCube
2nd flavour ratio result
(0.5:0.5:0.0)**



**IceCube
3rd flavour ratio result
(0.0:0.2:0.8)**

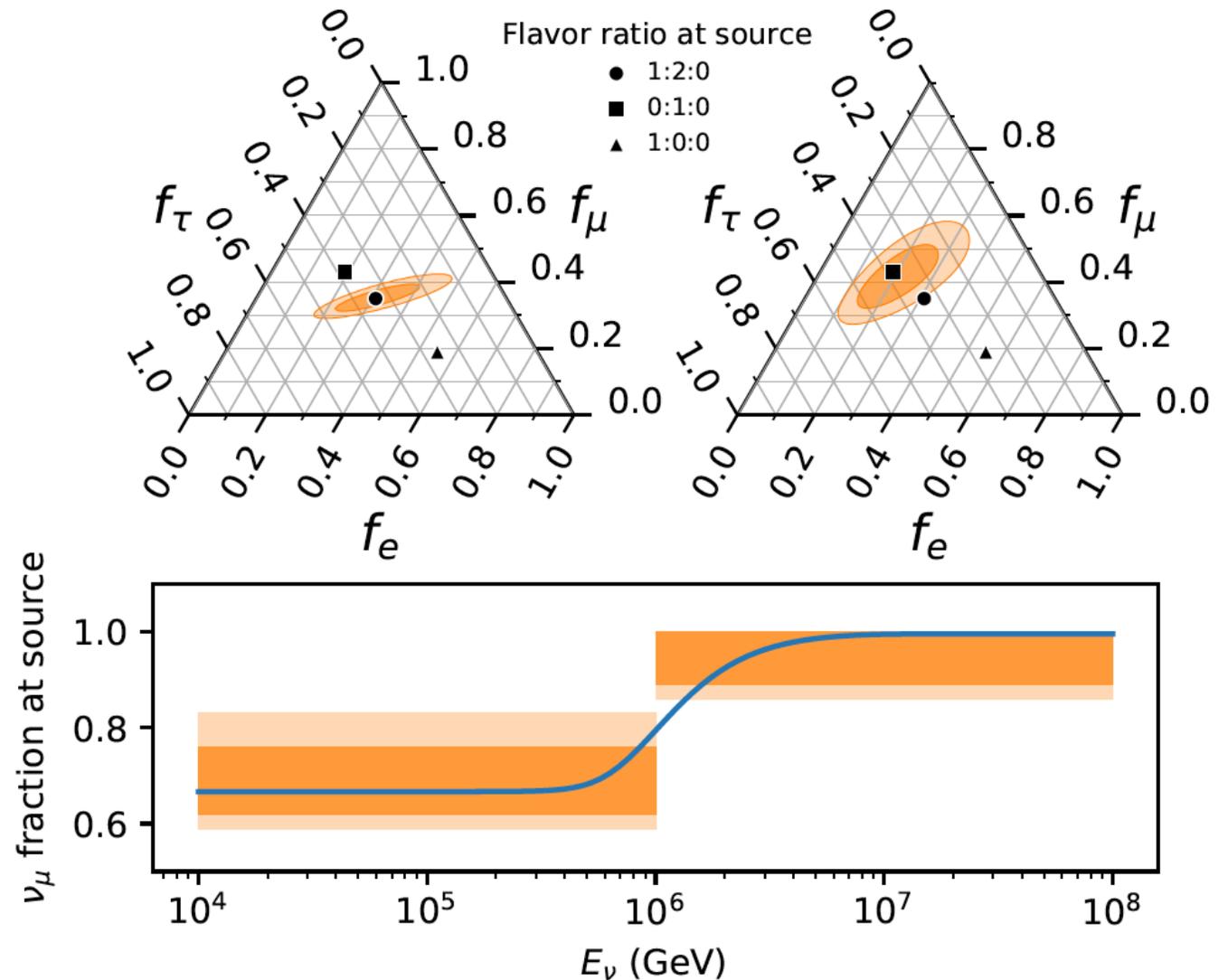
2018 flavour ratio measurement

- Likelihood is very shallow and fit often confuses between ν_e and ν_τ
- Flavour ratio result has some power to distinguish ν_e and ν_τ

Energy dependence of flavor ratio

Muon neutrino increases at higher energy

Future higher-statistics flavor measurement



New physics flavor ratio predictions

New physics models have different flavor ratios

Effective operator

- It includes Lorentz violation
- Assuming all possible standard production models, $(\nu_e:\nu_\mu:\nu_\tau) = (x:1-x:0)$, it covers 2/3 of the phase space.

