

ICISE Web Seminar

October 7th, 2021



**Diffuse Supernova Neutrino Background Search
at Super-Kamiokande**

[arXiv:2109.11174](https://arxiv.org/abs/2109.11174)

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in corporation with S. El Hedri & A. Giampaolo (Ecole Polytechnique)



2015

2016

2017



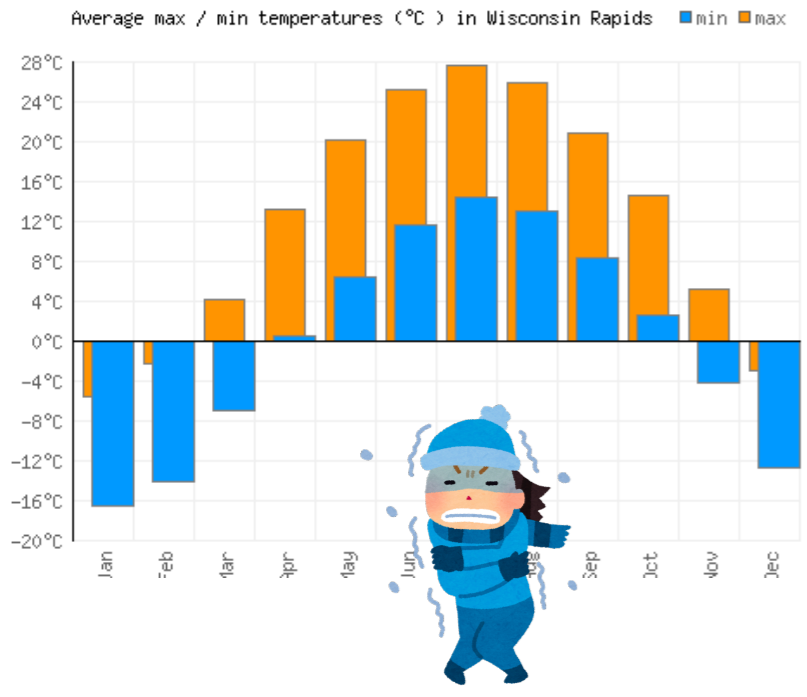
2018

2019

Got Ph.D in Kyoto!

2020





2015

2016

2017



2019

2020

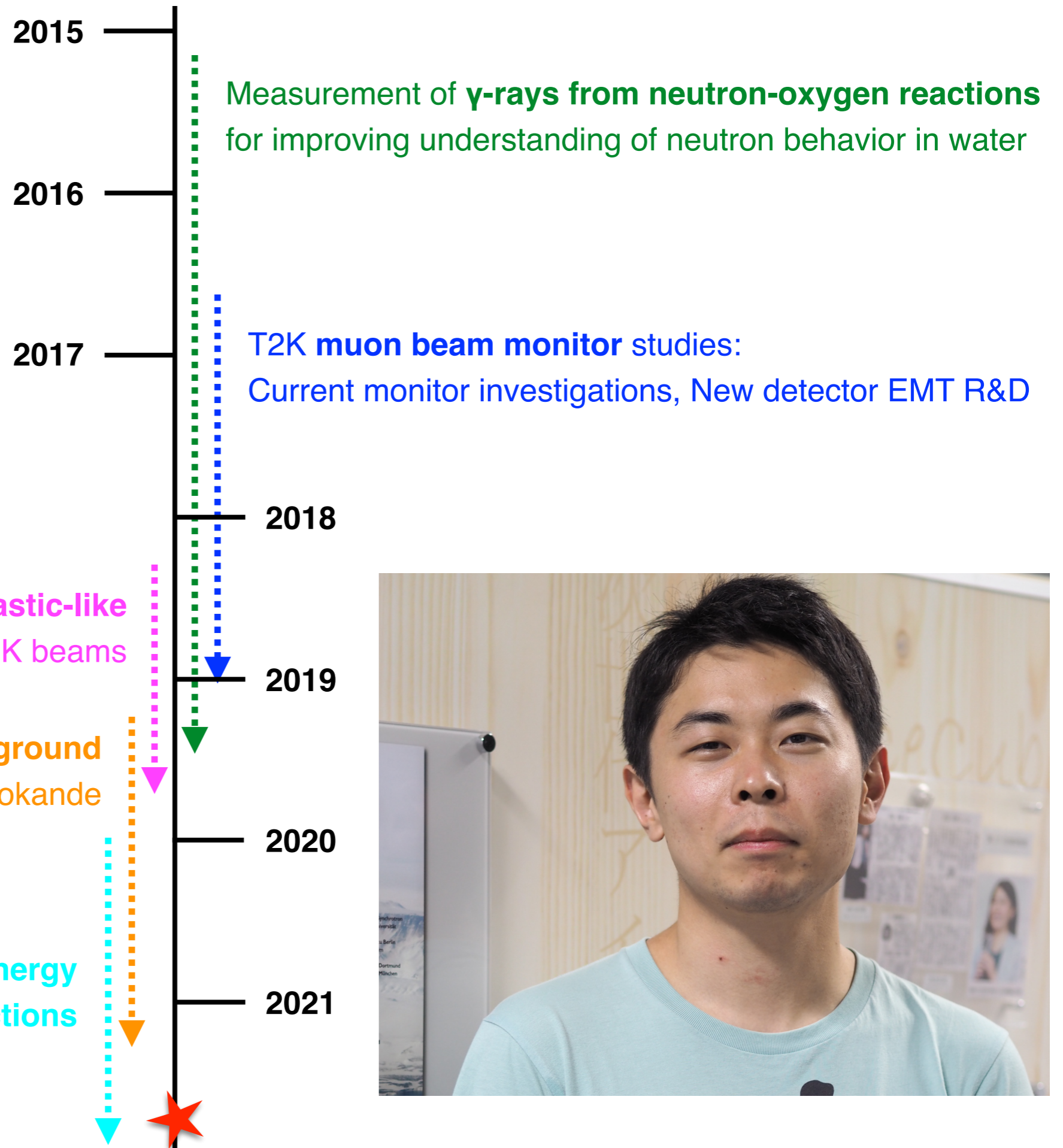
2021



Moved to Madison, Wisconsin!



T2K
↓
Super-Kamiokande
↓
IceCube



Supernova Explosion

- A Star which is more than ~8 times heavier than the Sun ends its life by an explosion.
 - kinetic energy: $\sim 10^{51}$ erg (1 erg = 1×10^{-7} J = 6.2×10^{11} eV)
 - luminosity: \sim galaxy
 - rate: 1–3/century/galaxy

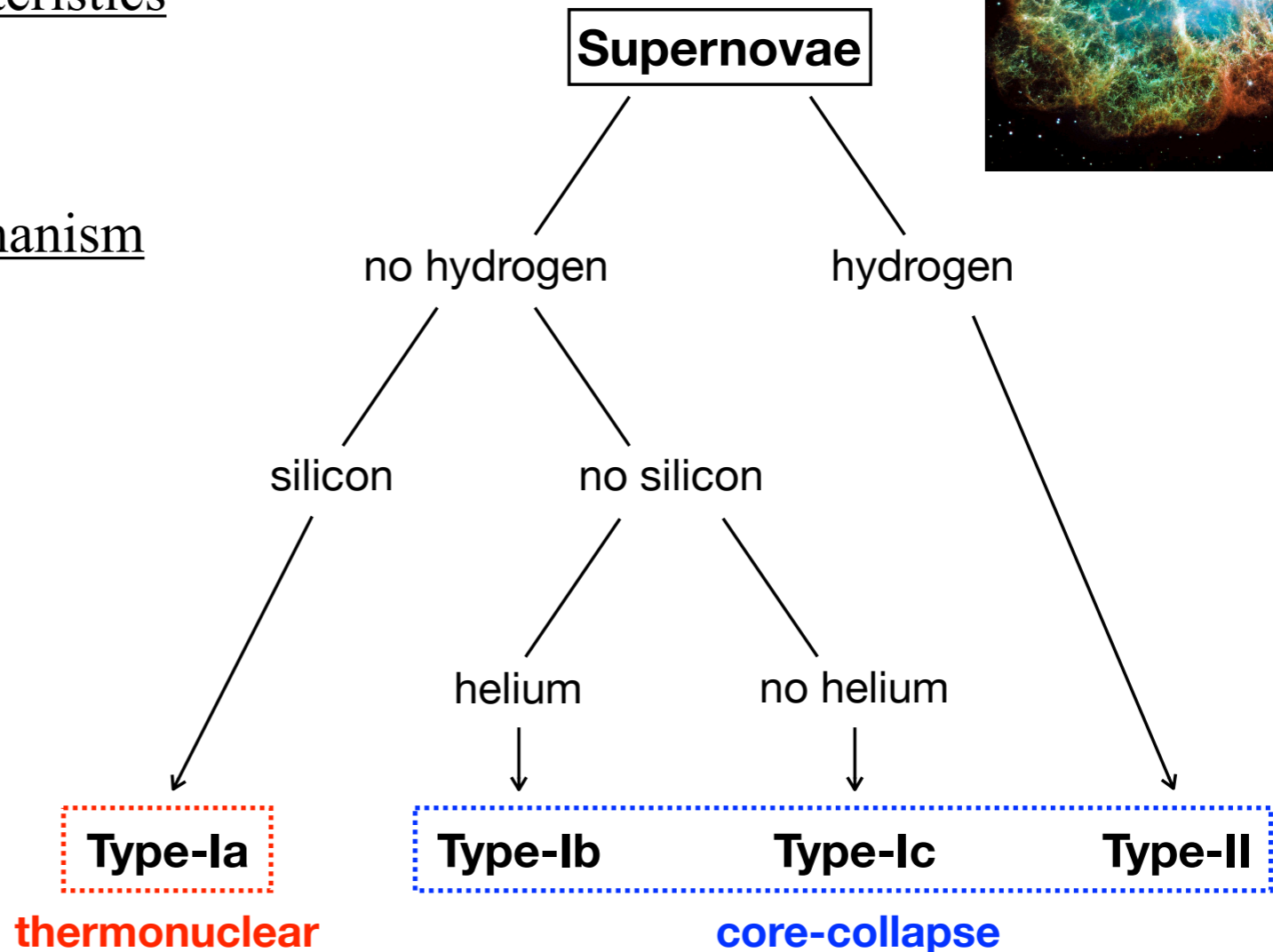
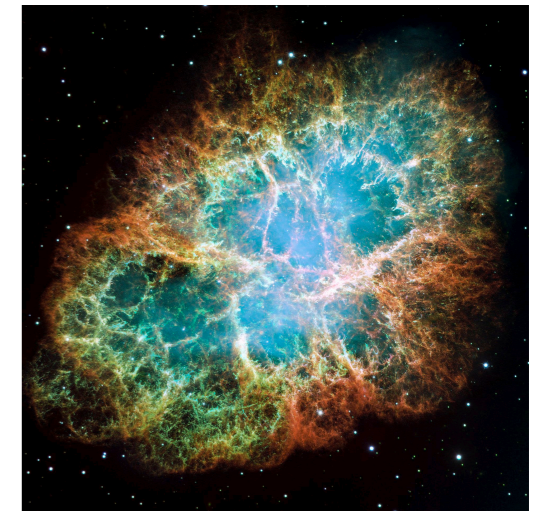
- Classification by spectral characteristics

- Ia, Ib, Ic, II

- Classification by explosion mechanism

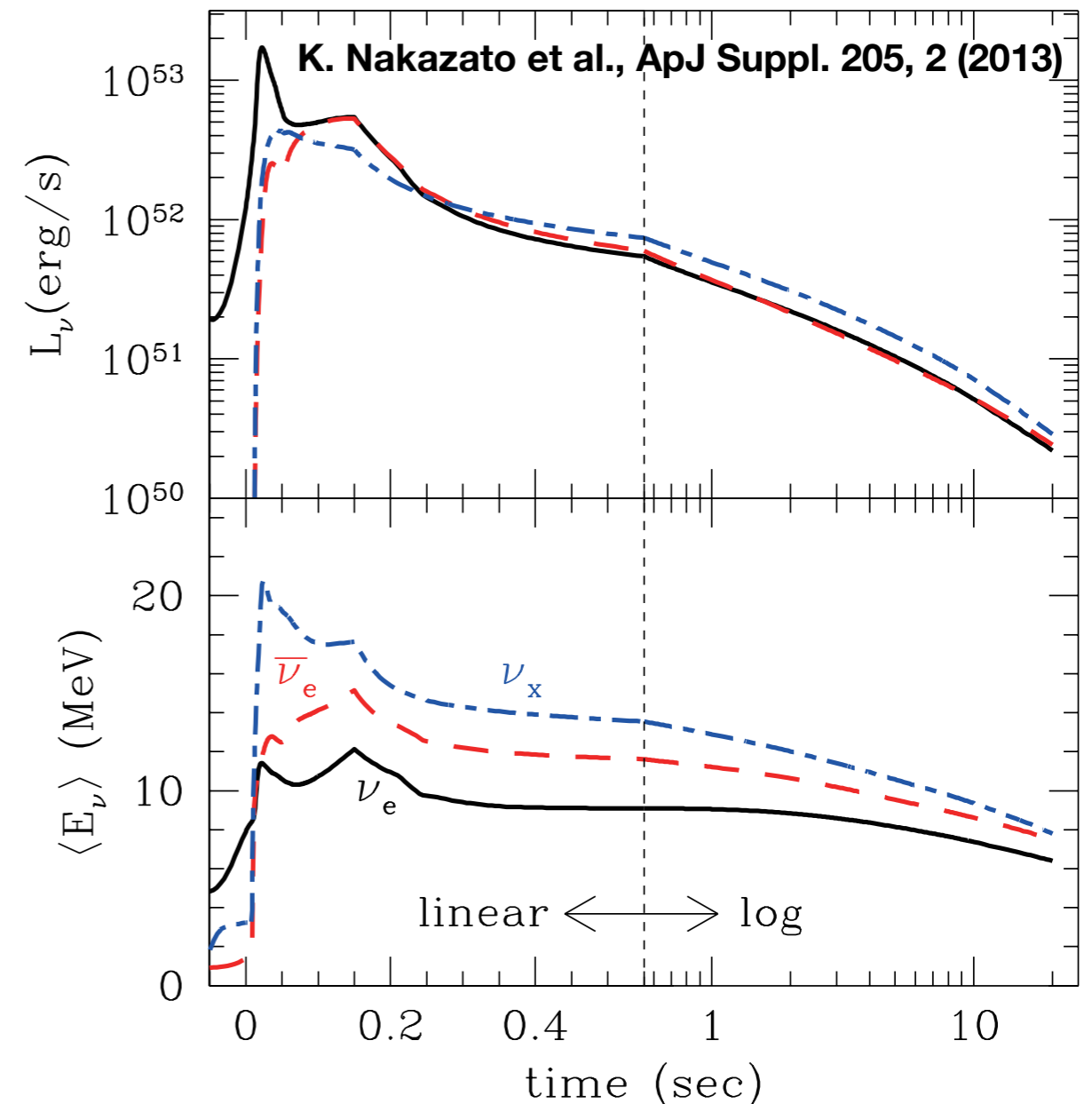
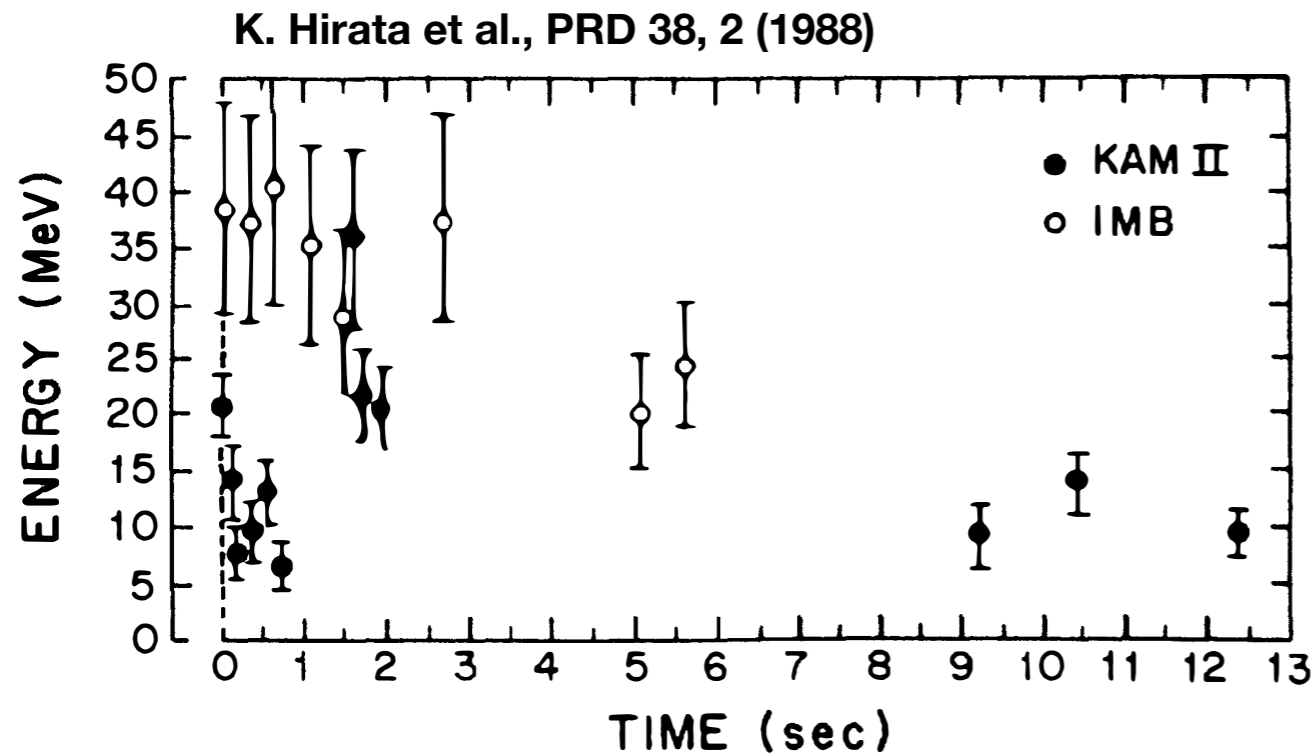
- thermonuclear (= Ia)
- **core-collapse** (= Ib, Ic, II)
 - **neutrino emission**

Crab Nebula by NASA



Neutrinos from Core-Collapse Supernovae

- **Experiment** There is only one observation of neutrinos from a supernova (“SN1987A” in the Large Magellanic Cloud).
- **Theory** There are many numerical simulations about CCSNe, but **the explosion mechanism is not completely revealed.**



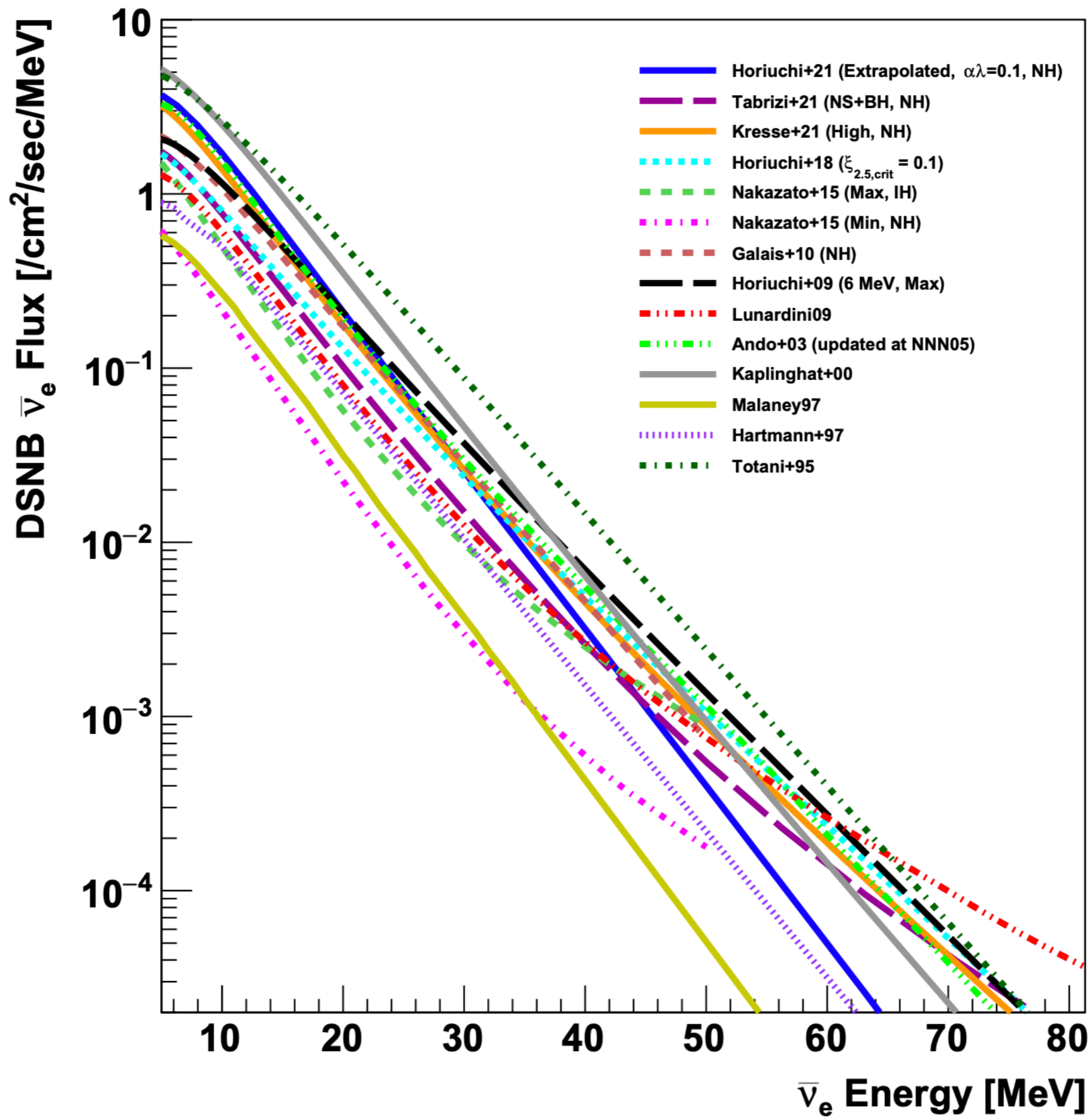
Diffuse Supernova Neutrino Background

- Neutrinos from all past CCSNe are accumulated to form an integrated flux.
= **Diffuse Supernova Neutrino Background (DSNB)** or **Supernova Relic Neutrinos (SRNs)**
- Various factors affect the DSNB flux on Earth.
 - Neutrino oscillation (mass ordering)
 - Galactic evolution (star formation rate, initial mass function, binary interactions, etc)
 - Black hole formation rate (metallicity, equation-of-state, etc)
 - etc

DSNB flux

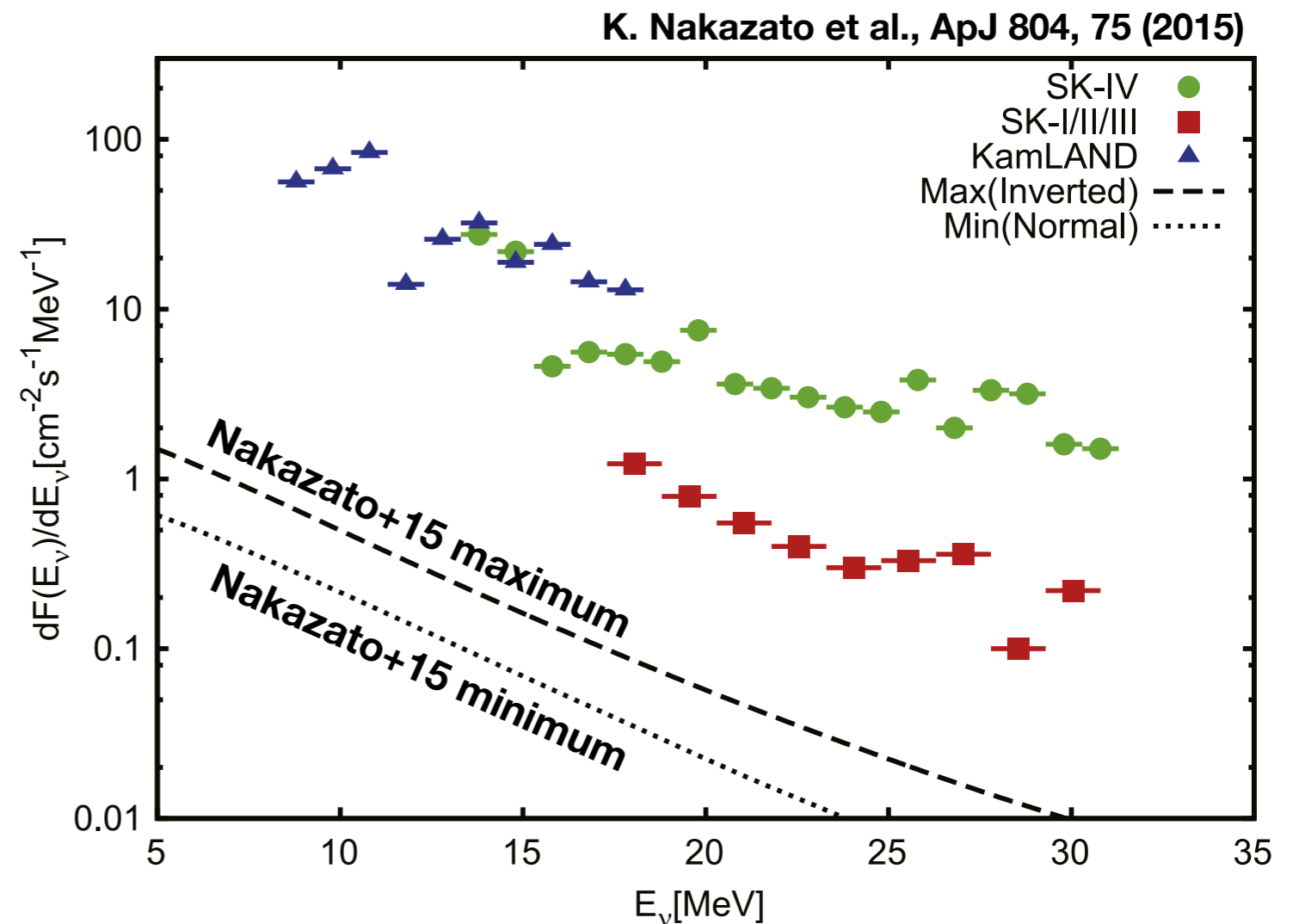
$$\frac{d\Phi(E_\nu)}{dE_\nu} = c \int_0^\infty \frac{dz}{H_0 \sqrt{\Omega_m (1+z)^3 + \Omega_\Lambda}} \times \left[R_{\text{CCSN}}(z) \int_0^{Z_{\text{max}}} \Psi_{\text{ZF}}(z, Z) \left\{ \int_{M_{\text{min}}}^{M_{\text{max}}} \Psi_{\text{IMF}}(M) \frac{dN(M, Z, E'_\nu)}{dE'_\nu} dM \right\} dZ \right].$$

cosmological parameters
neutrino number spectrum per CCSN
CCSN rate
metallicity distribution of progenitors
initial mass function of progenitors

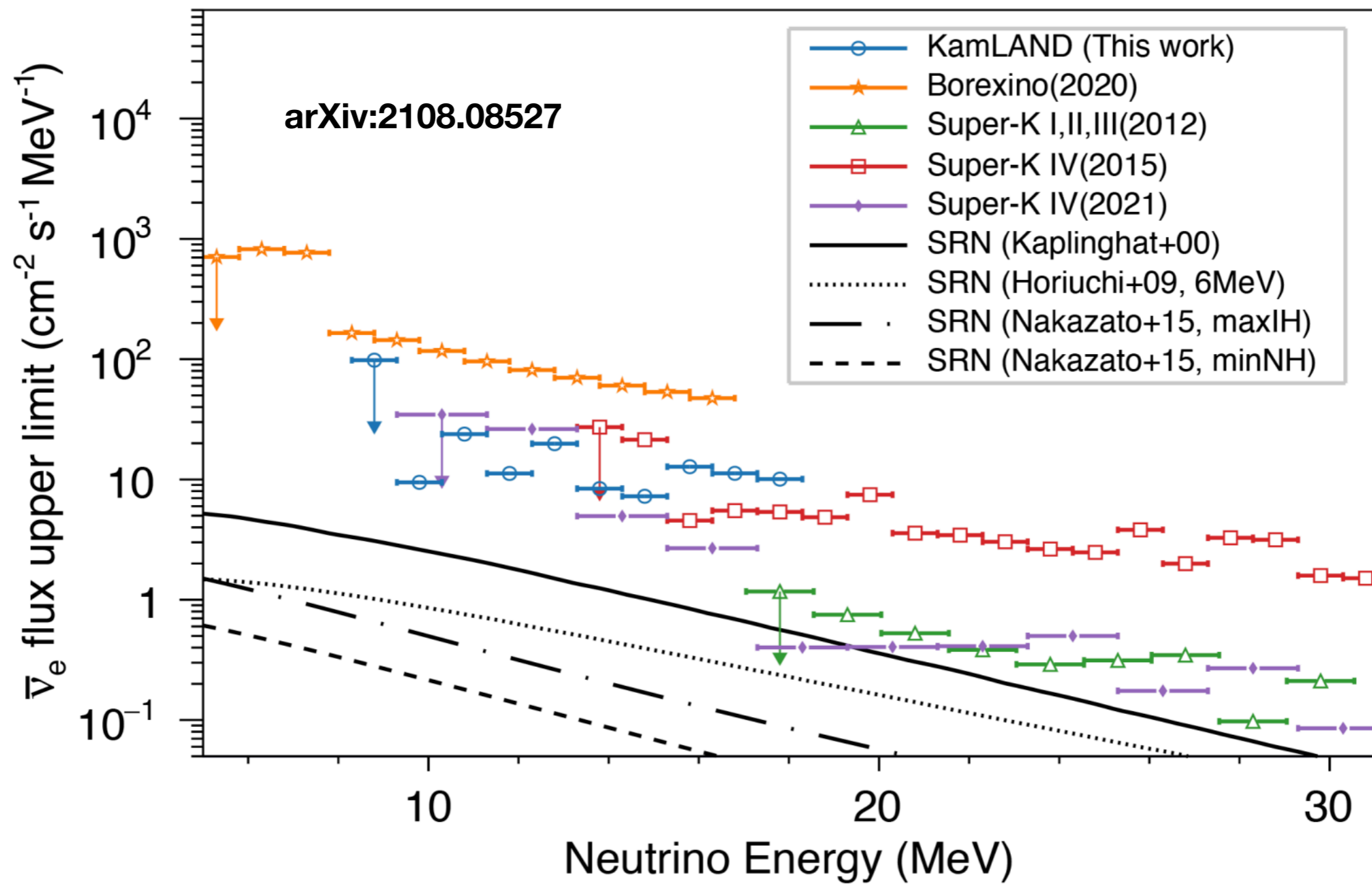


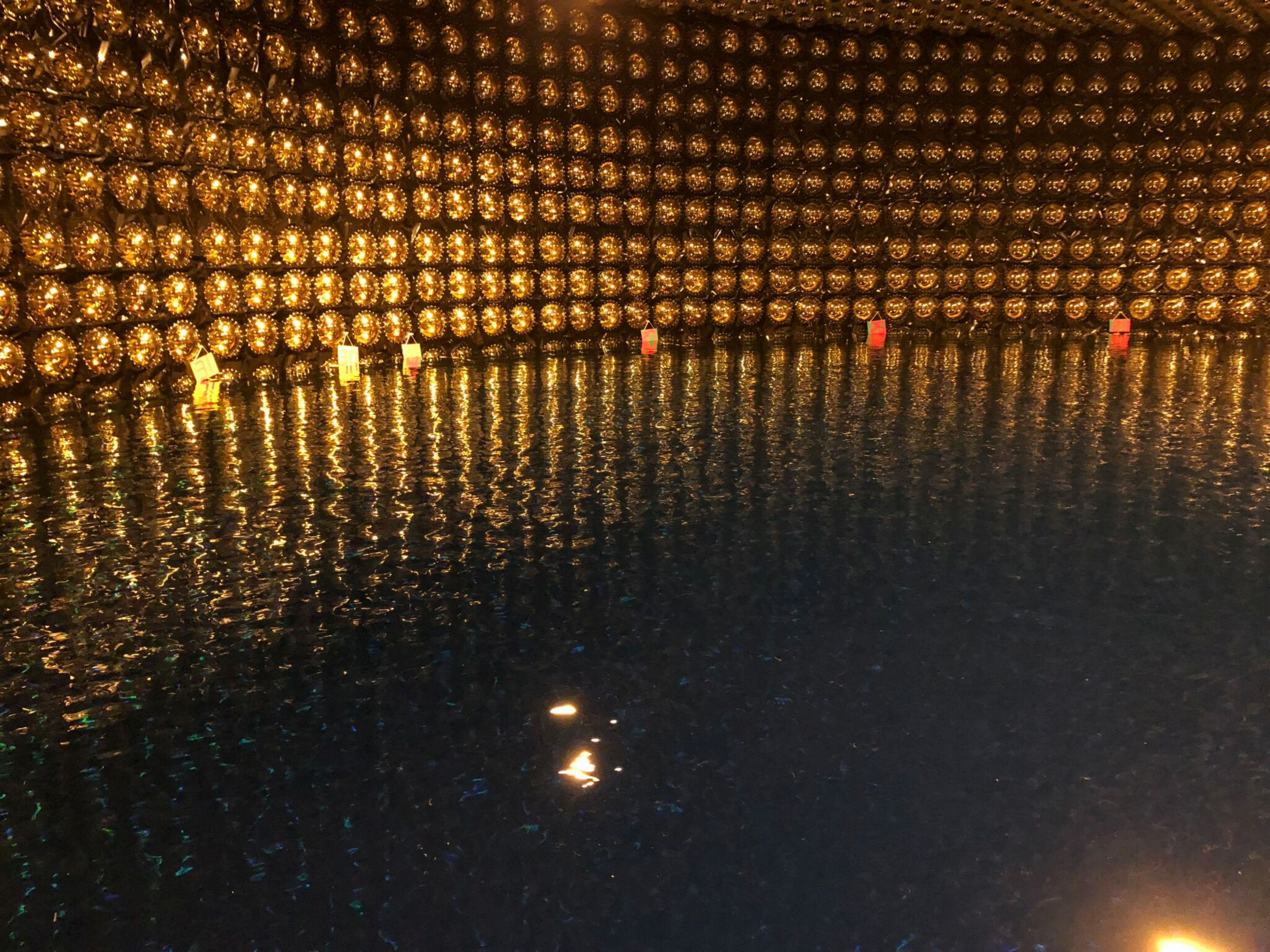
Experimental Searches

- **Signal in experimental searches** = inverse beta decay ($\bar{\nu}_e + p \rightarrow e^+ + n$)
- Most sensitive searches have been performed at **Super-Kamiokande** and **KamLAND**.
- Search at SK (water)
 - SK-I/II/III (spectral fitting analysis): fitting by atmospheric spectra for $E_\nu > 17.3$ MeV
 - SK-IV (neutron tagging analysis): low energy threshold, tagging efficiency $\sim 20\%$
- Search at KamLAND (oil)
 - very low energy threshold, tagging efficiency $\sim 100\%$



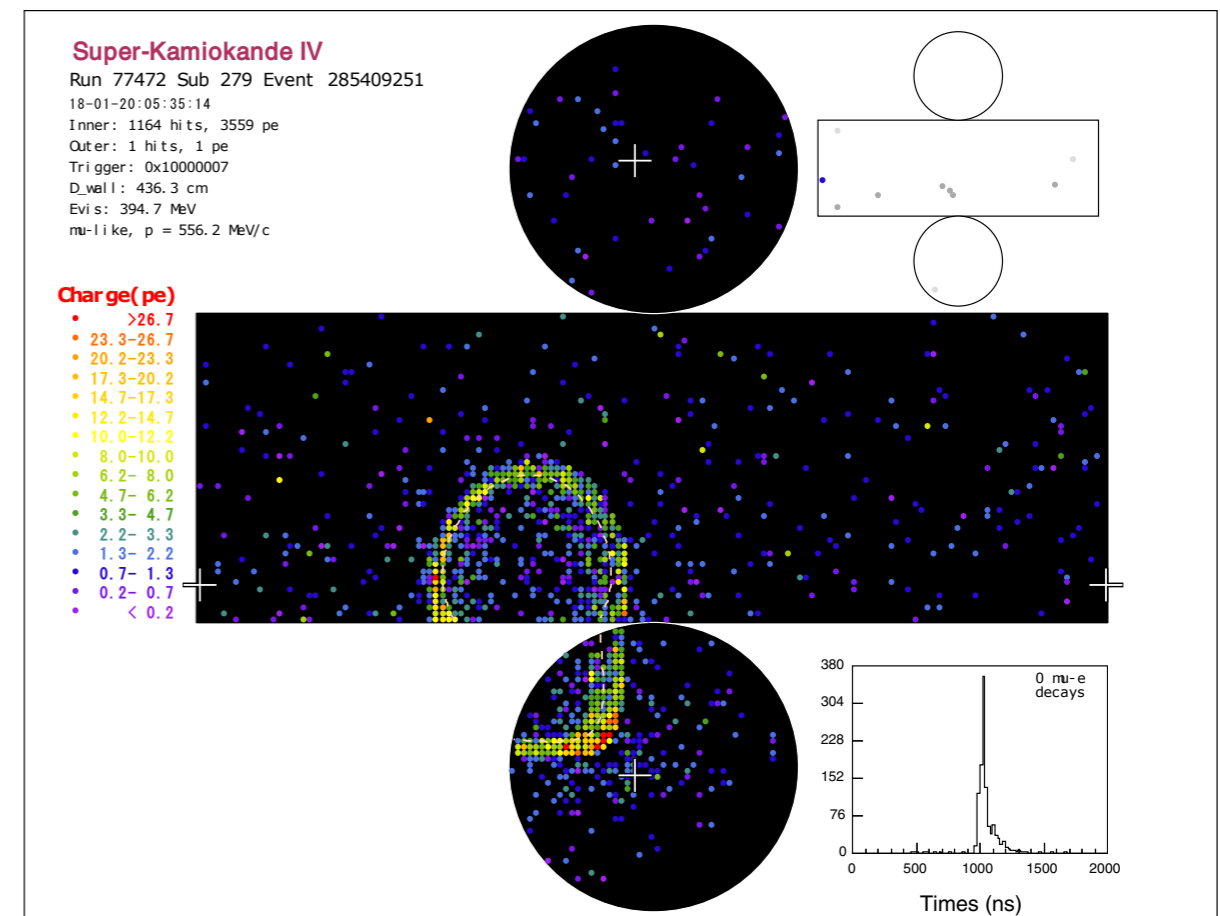
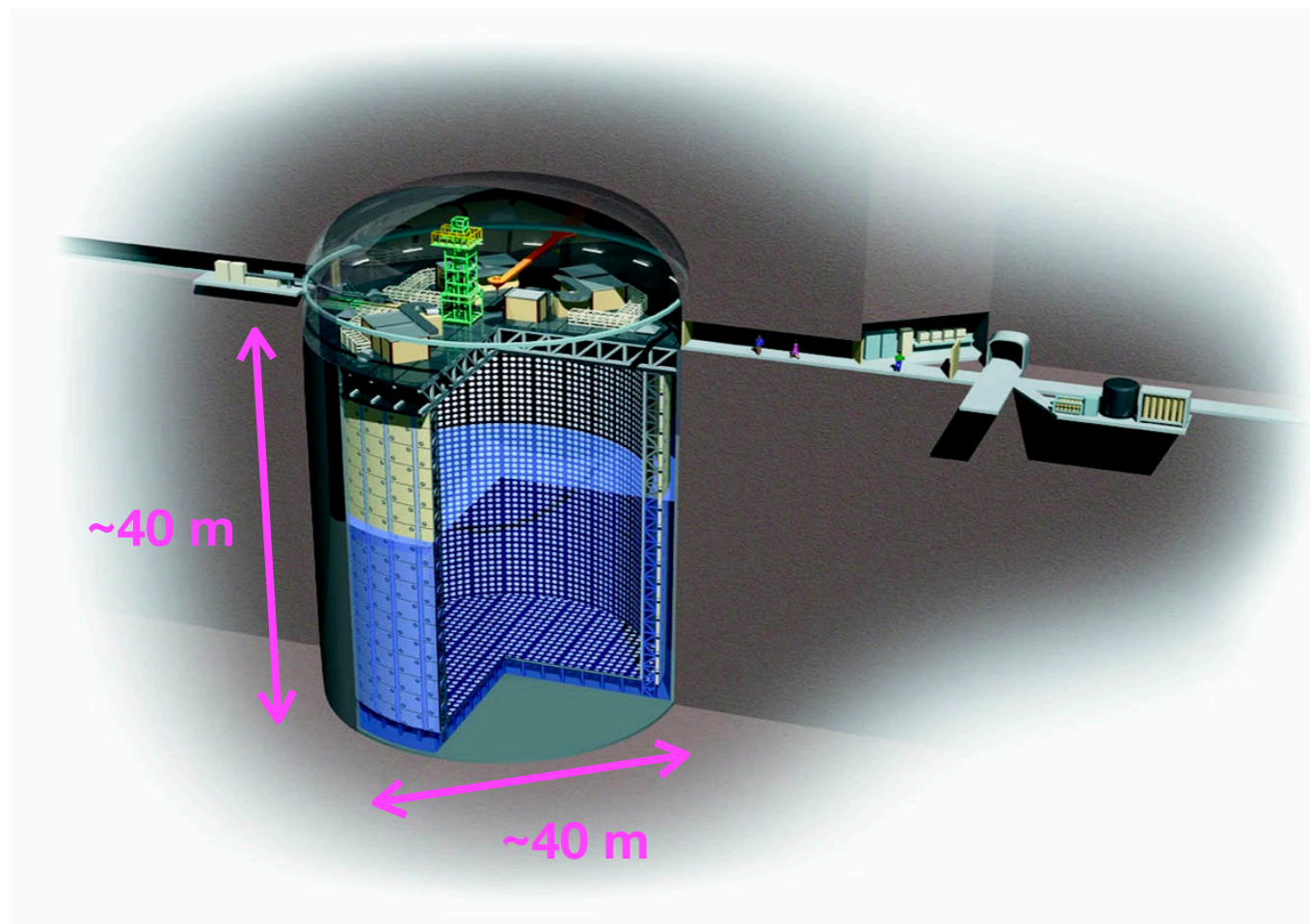
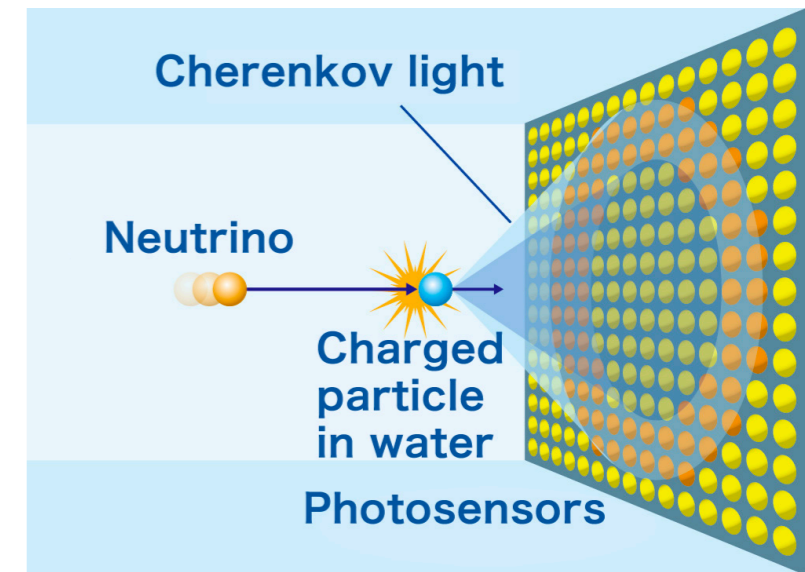
Recent Result from KamLAND



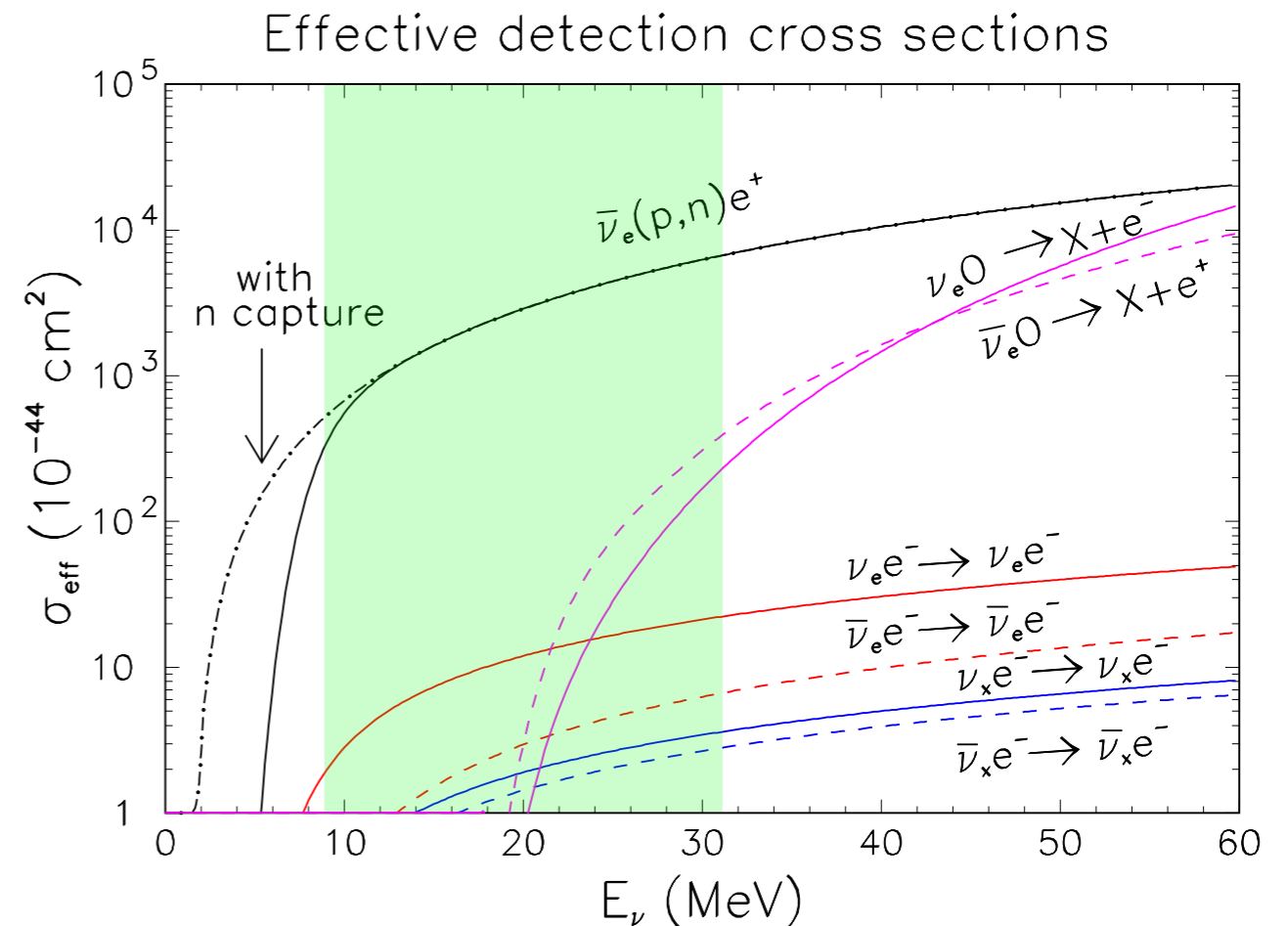
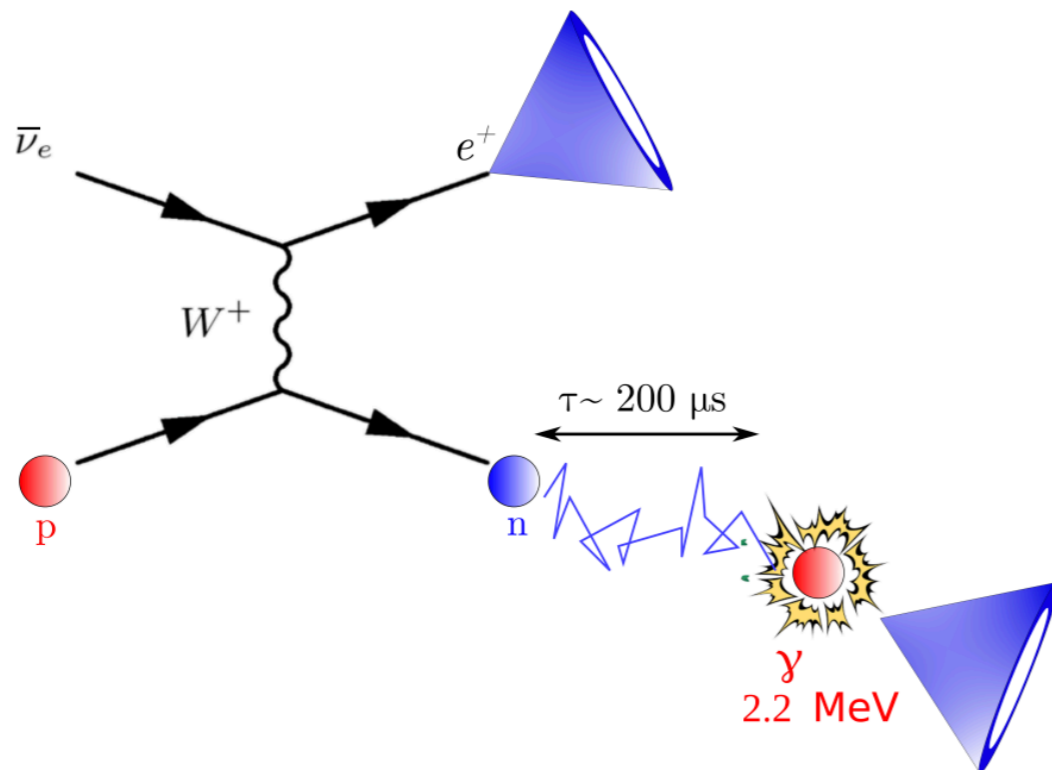


Super-Kamiokande

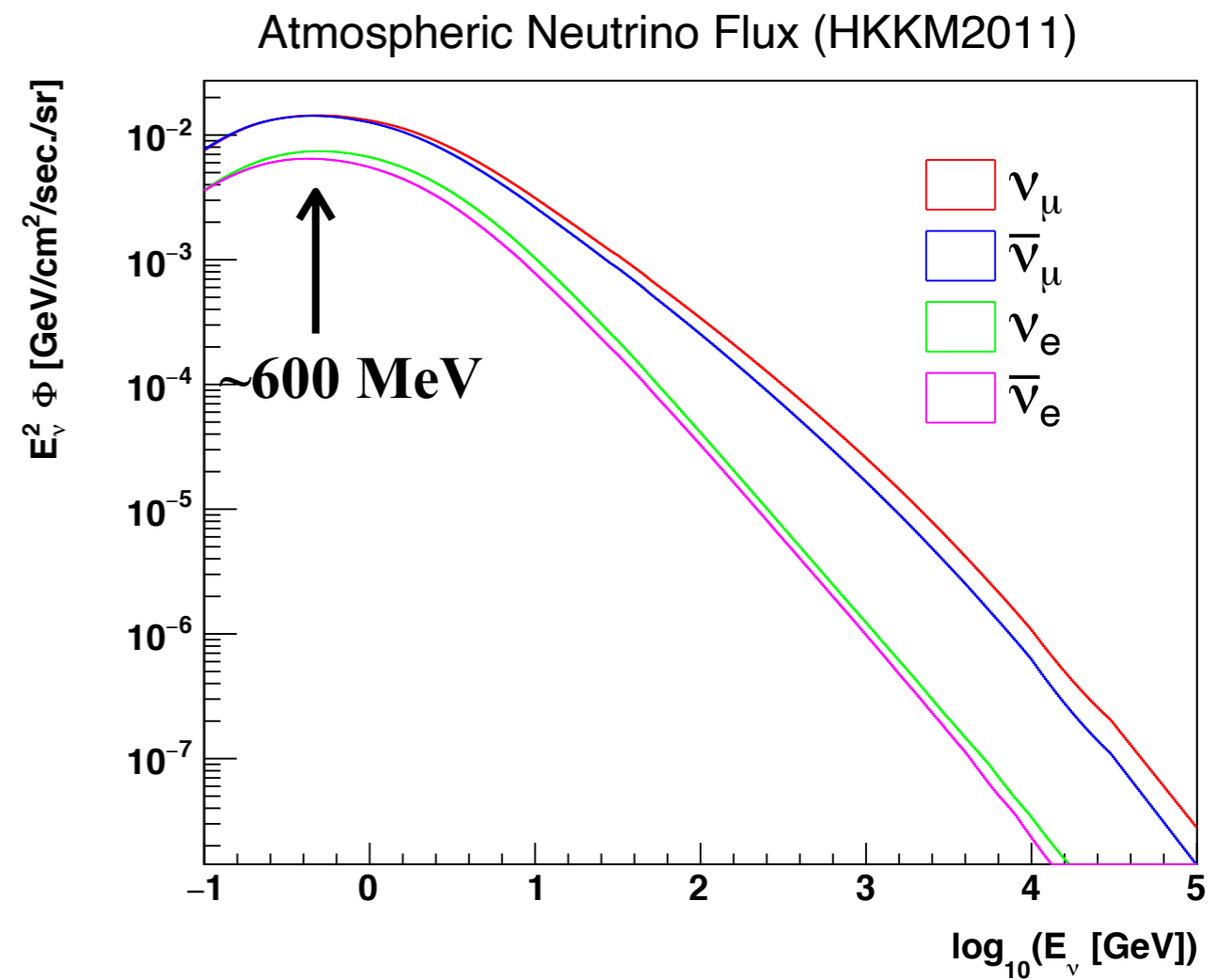
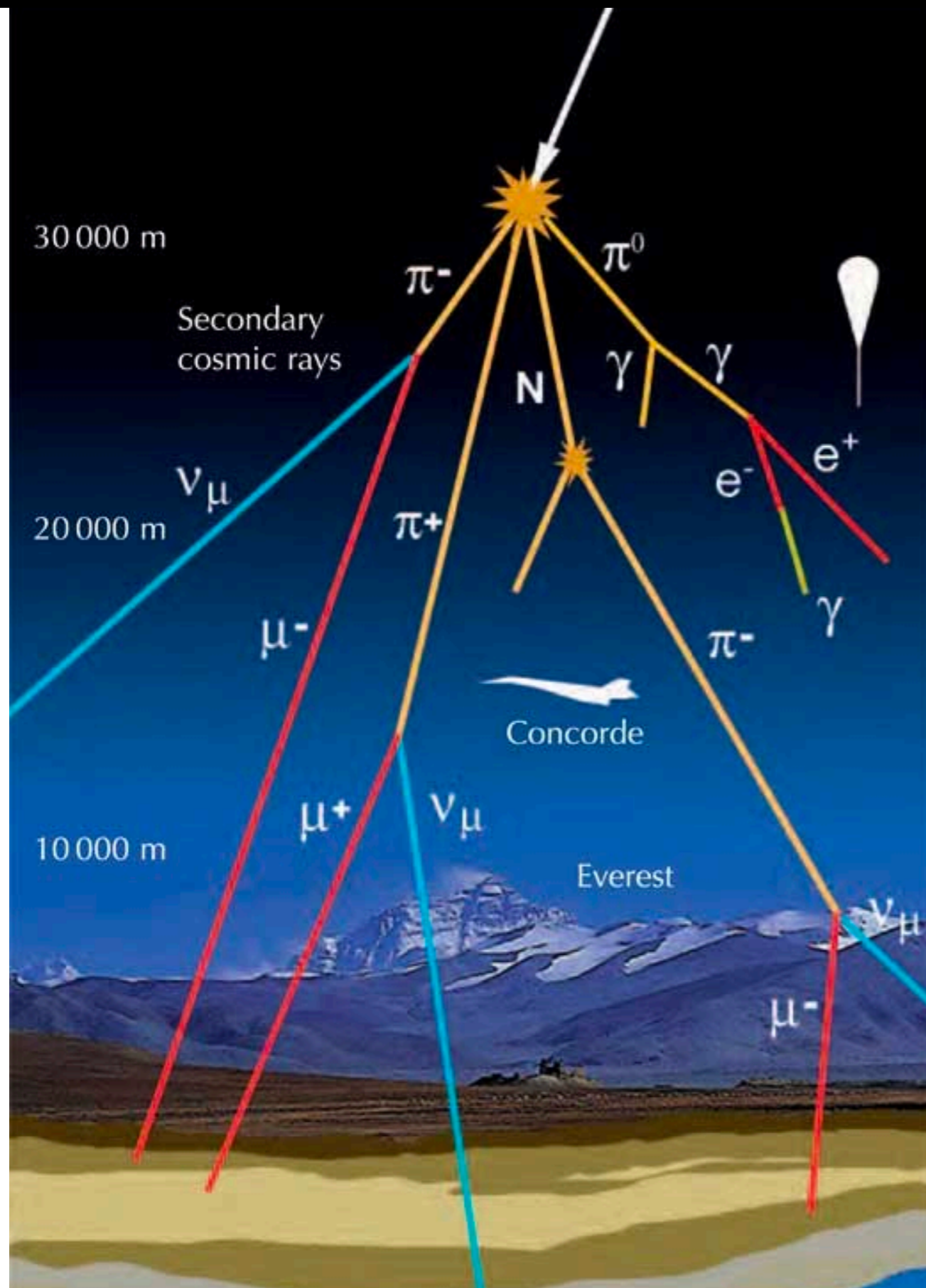
- A water Cherenkov detector located 1,000 m under the mountain.
- Fiducial volume: 22.5 kton
- Inner detector: 11,129 20-inch PMTs
- Outer detector: 1,885 8-inch PMTs, used for cosmic muon veto
- Operated since 1996 in five periods.
 - This work uses data from **SK-IV** (2008–2018).



- Inverse beta decay of electron antineutrinos ($\bar{\nu}_e + p \rightarrow e^+ + n$) is searched.
 - Larger than the other mode by >2 orders of magnitude.
 - Search region = [7.5, 29.5] MeV in visible energy ($E_\nu = [9.3, 31.3]$ MeV)
- Signal: “ $\beta+n$ ” events
 - Prompt signal = β
 - Delayed signal = **2.2 MeV γ** from neutron capture

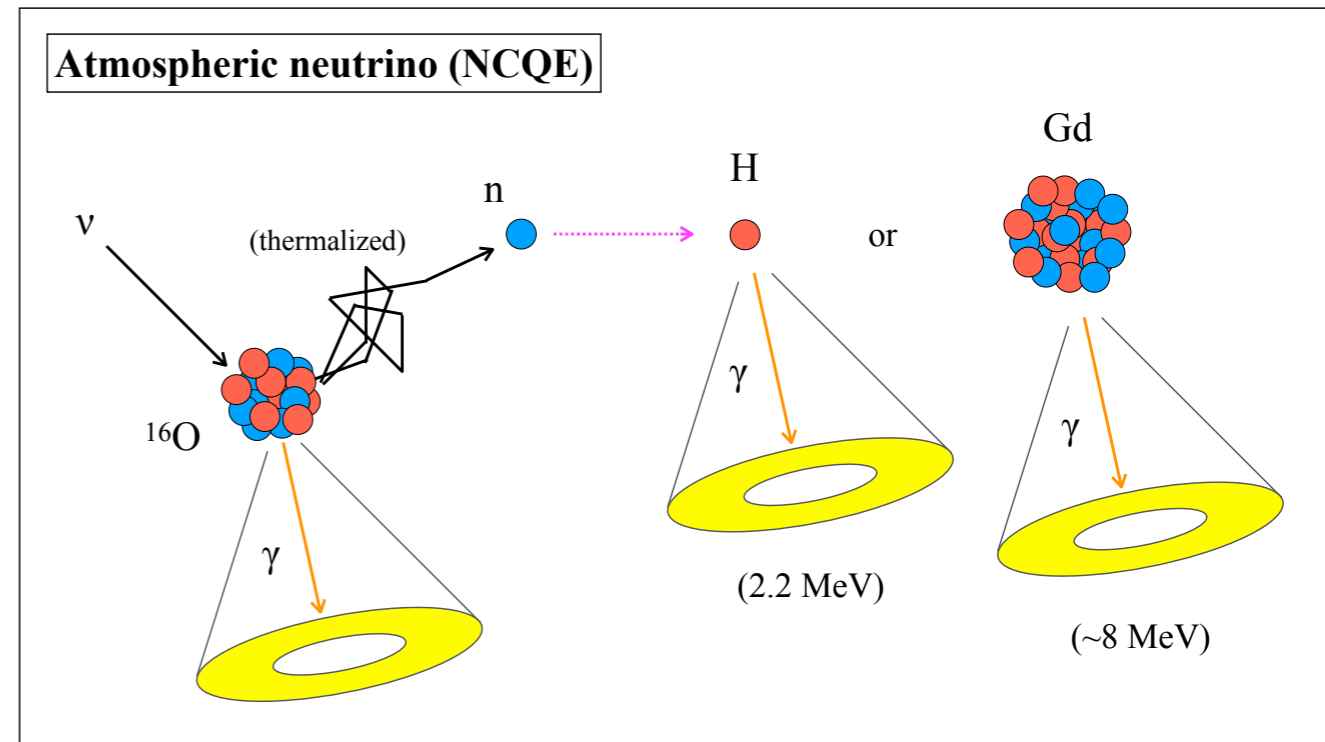
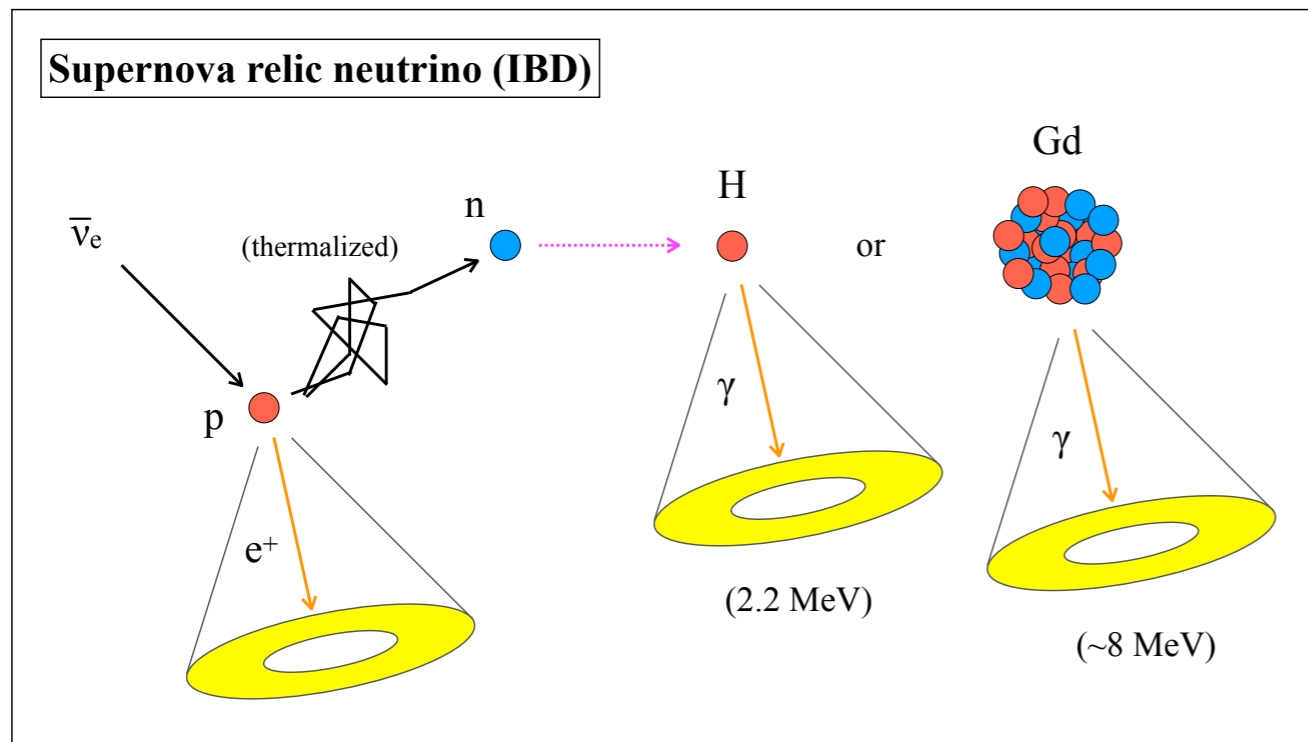


Background (1): Atmospheric Neutrinos

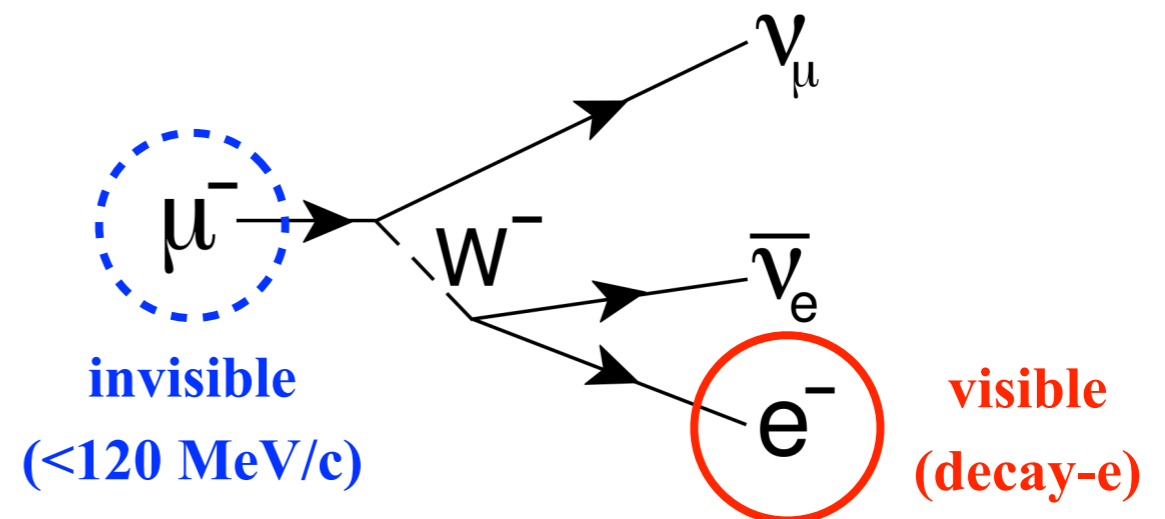


Background (1): Atmospheric Neutrinos

- **Neutral-current quasielastic (NCQE) interactions**
 - de-excitation γ -ray (+ n)
 - dominant below ~ 20 MeV

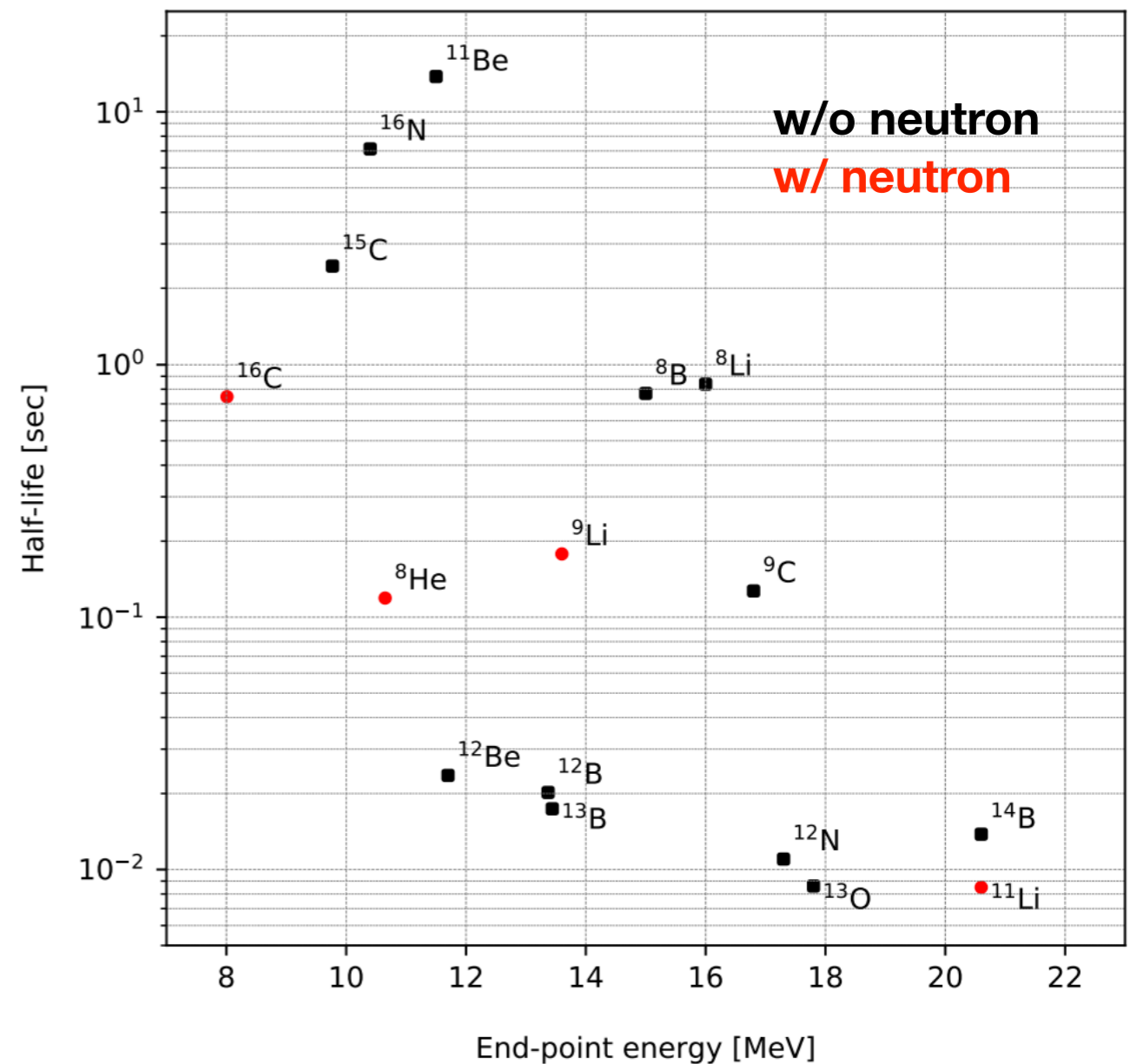
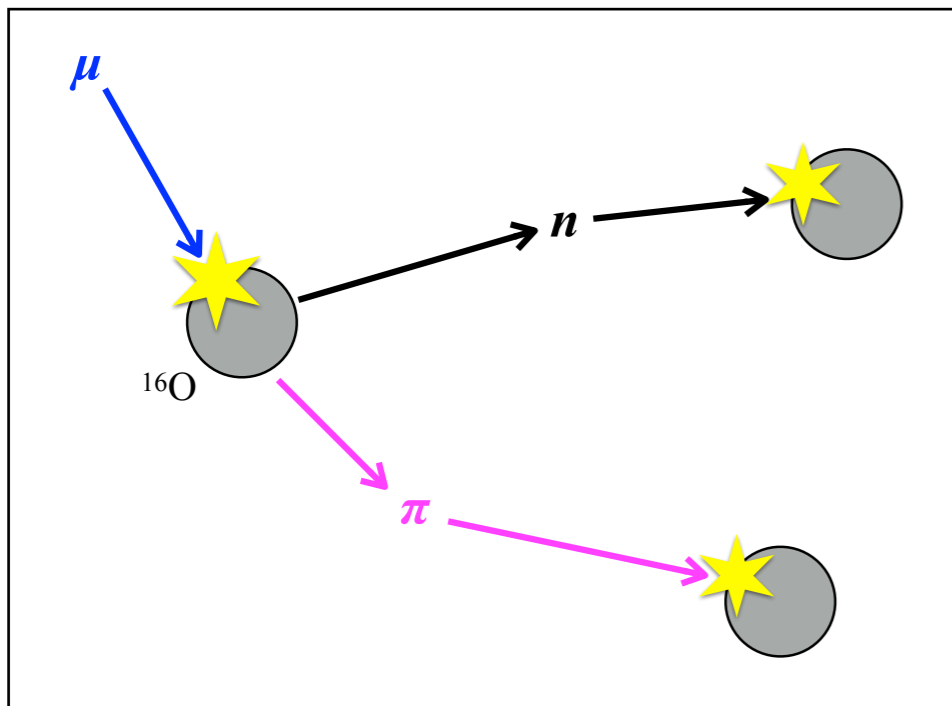


- **Muon-producing interactions (CC, NC)**
 - (invisible muon \rightarrow) decay electron (+ n)
 - dominant above ~ 20 MeV



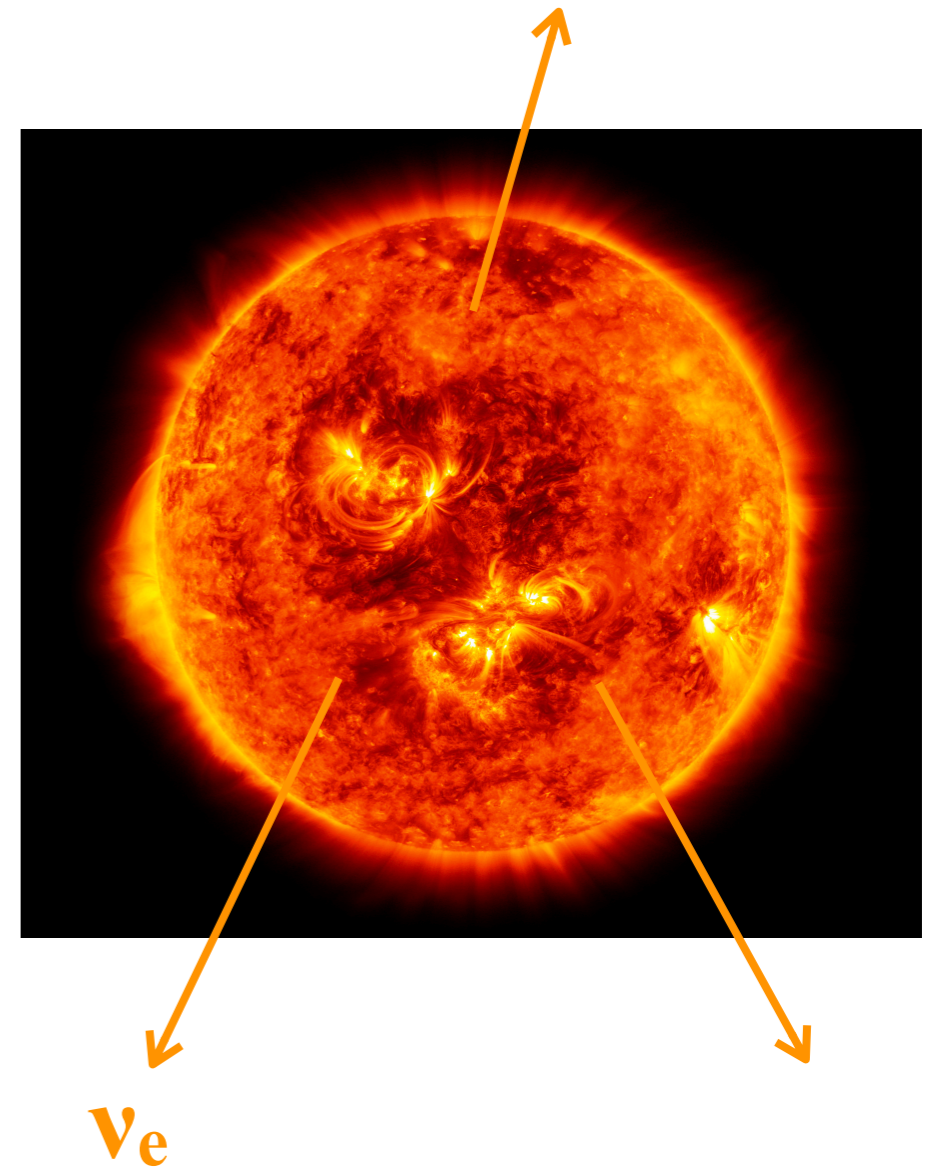
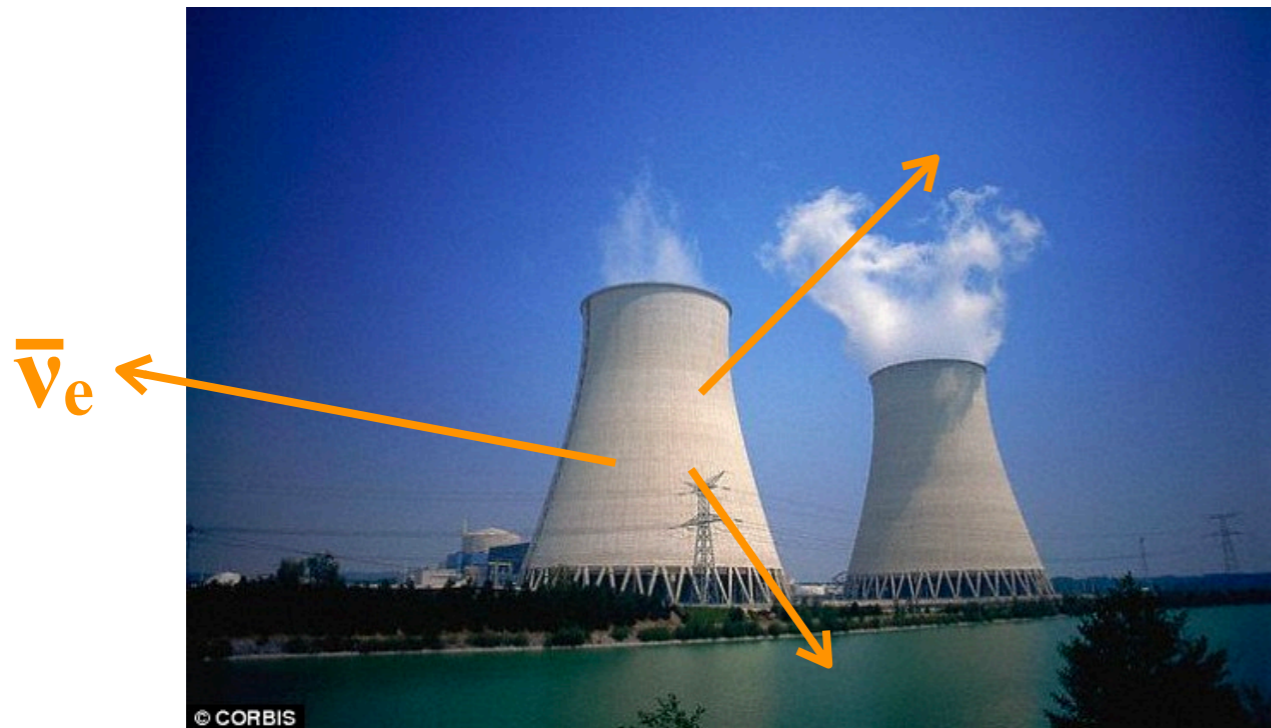
Background (2): Muon Spallation

- Cosmic-ray muons are coming at Super-K with ~ 2 Hz.
- Some of them break nuclei in water, producing radioactive isotopes.
- This is huge below 20 MeV, and especially ${}^9\text{Li}$ decays into $\beta+n$.

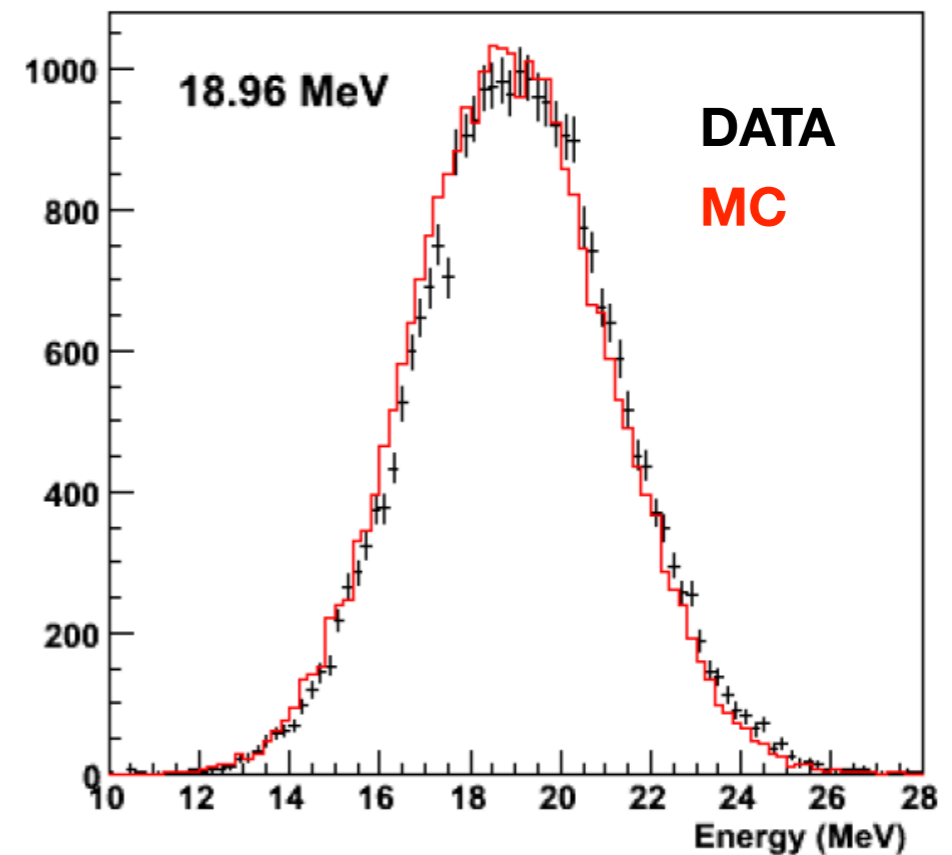
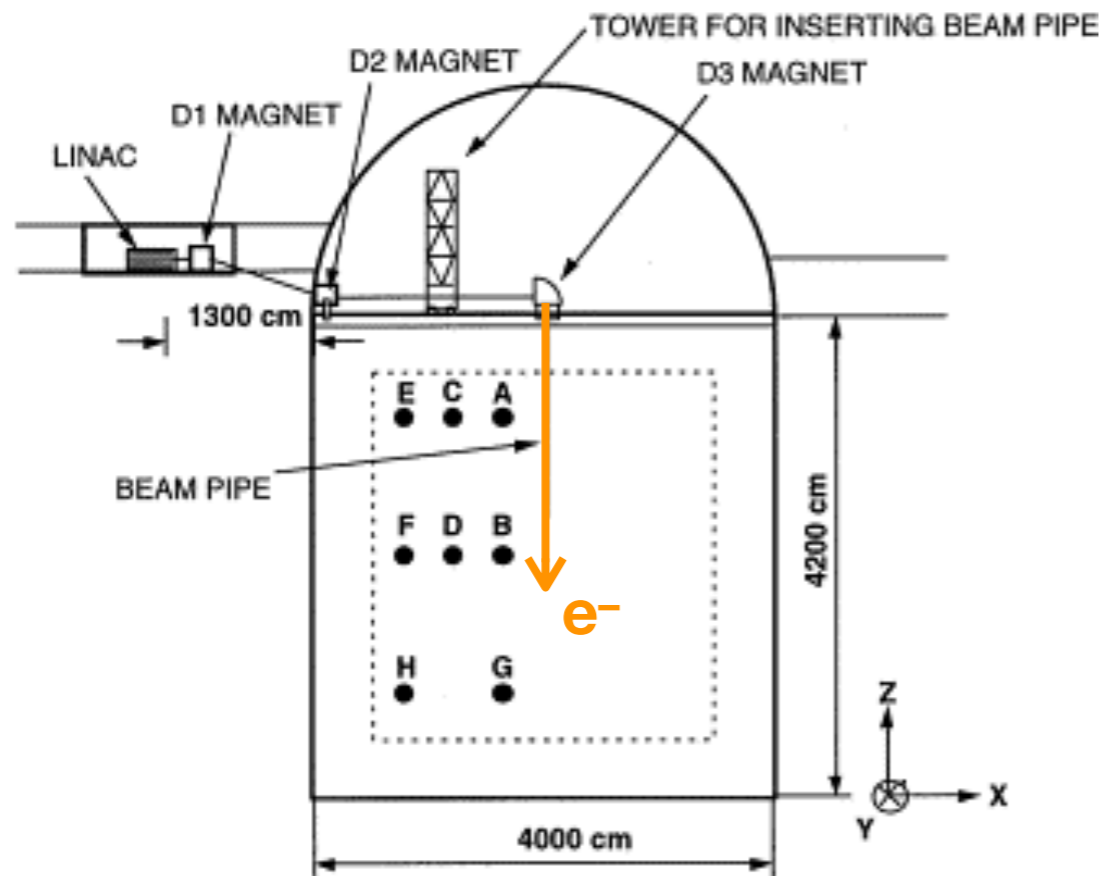


Background (3): Other Sources

- **Solar neutrinos**
 - Electron neutrinos from Sun.
 - Would make an accidental pair with a neutron-like signal.
- **Reactor neutrinos**
 - Electron antineutrinos from reactor plants
 - Only below 10 MeV



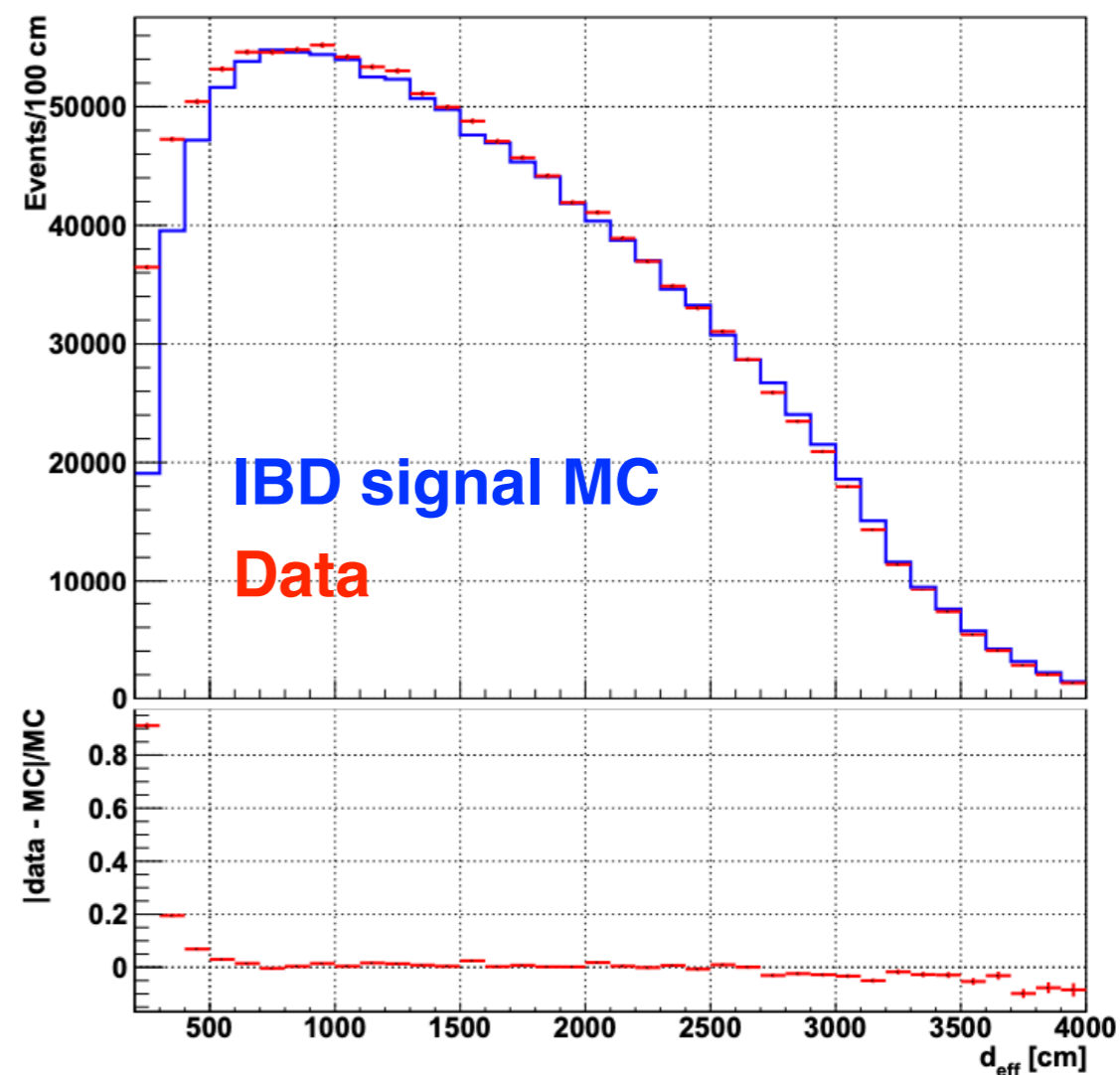
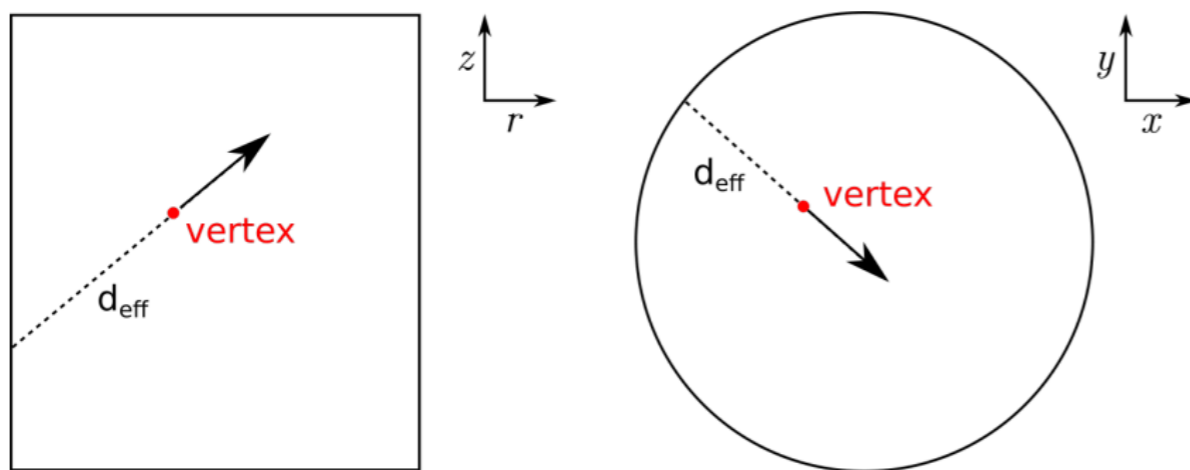
- Energy is reconstructed from the number of PMT hits.
- Detector calibration is performed in many ways.
 - Electron linear accelerator (LINAC): up to ~ 19 MeV
 - γ -ray source: $\sim O(10)$ MeV
 - Electrons from cosmic-ray muon decay (decay electrons): $>O(10)$ MeV



Position and Direction

- Huge amount of radioactive backgrounds near the wall.
- We require >2 m away from the wall and additional cuts on “effective wall distance”.

$$d_{\text{eff}} > \max \left\{ 300, 500 - \frac{E_{\text{rec}} - 15.5 \text{ MeV}}{1 \text{ MeV}} \times 50 \right\} \text{ cm.}$$



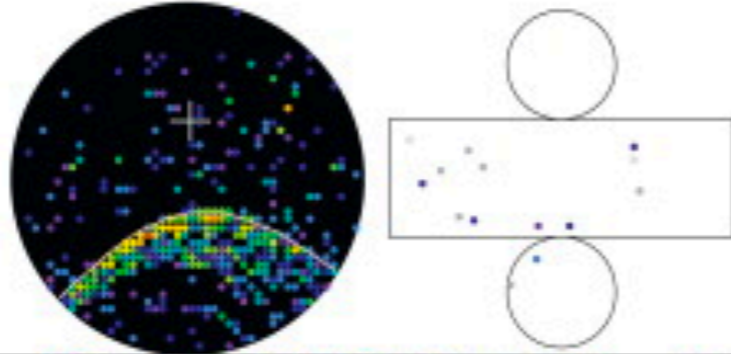
mu-like

e-like

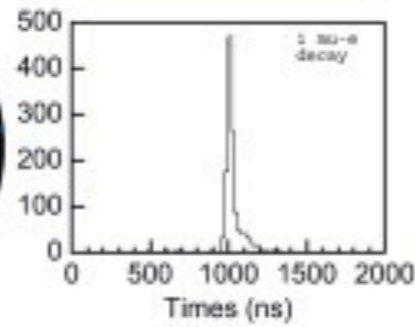
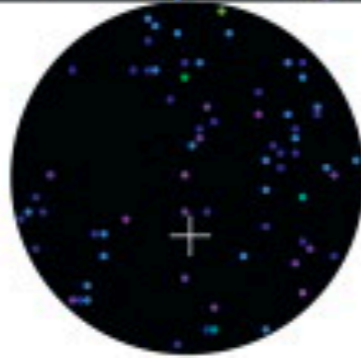
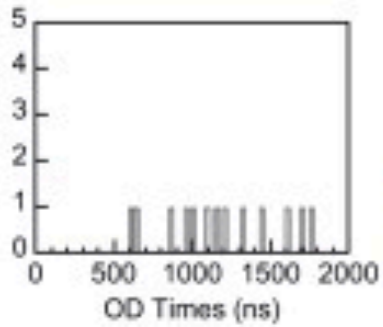
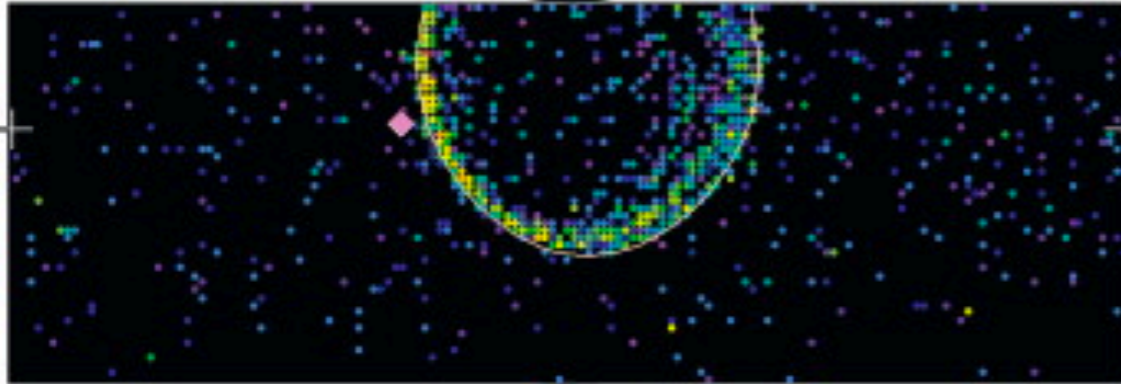
a

Super-Kamiokande IV

T2K Beam Run 0 Spill 797537
Run 66776 Sub 770 Event 178987674
10-05-11:12:14:31
T2K beam dt = 1899.2 ns
tsize: 1332 hits, 3282 pe
Outer: 6 hits, 5 pe
Trigger: 6x8000007
D_wall: 1136.5 cm
mu-like, p = 536.2 MeV/c

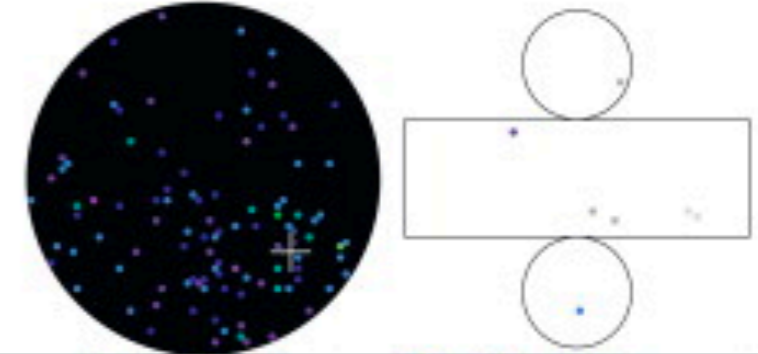
**Charge (pe)**

- >26.7
- 23.3-26.7
- 20.2-23.3
- 17.3-20.2
- 14.7-17.3
- 12.2-14.7
- 10.0-12.2
- 8.0-10.0
- 6.2-8.0
- 4.7-6.2
- 3.3-4.7
- 2.3-3.3
- 1.3-2.3
- 0.7-1.3
- 0.3-0.7
- = 0.2

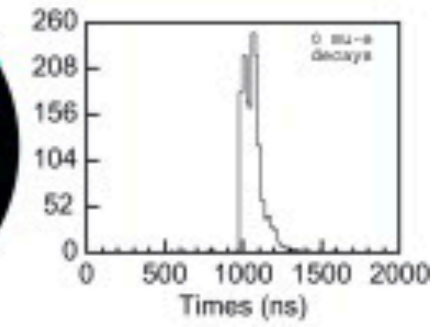
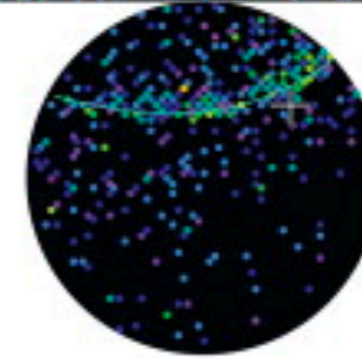
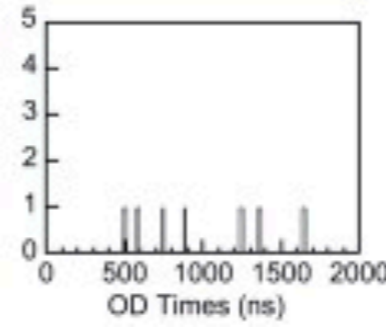
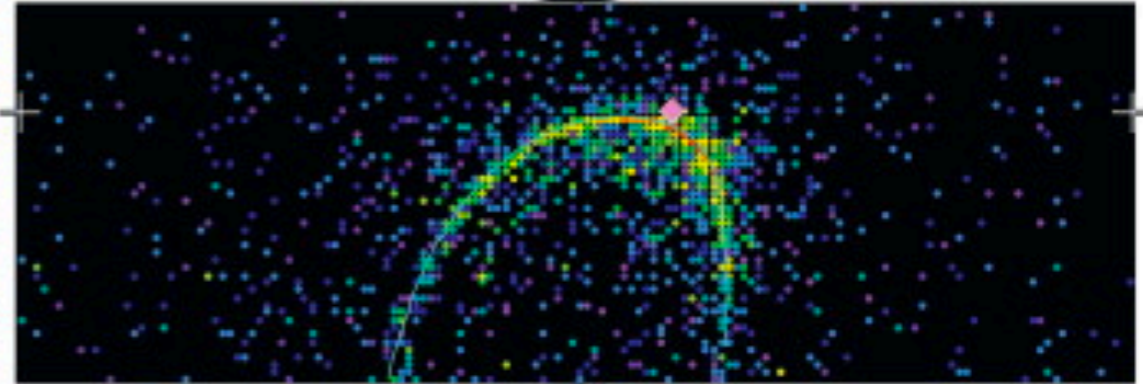
**b**

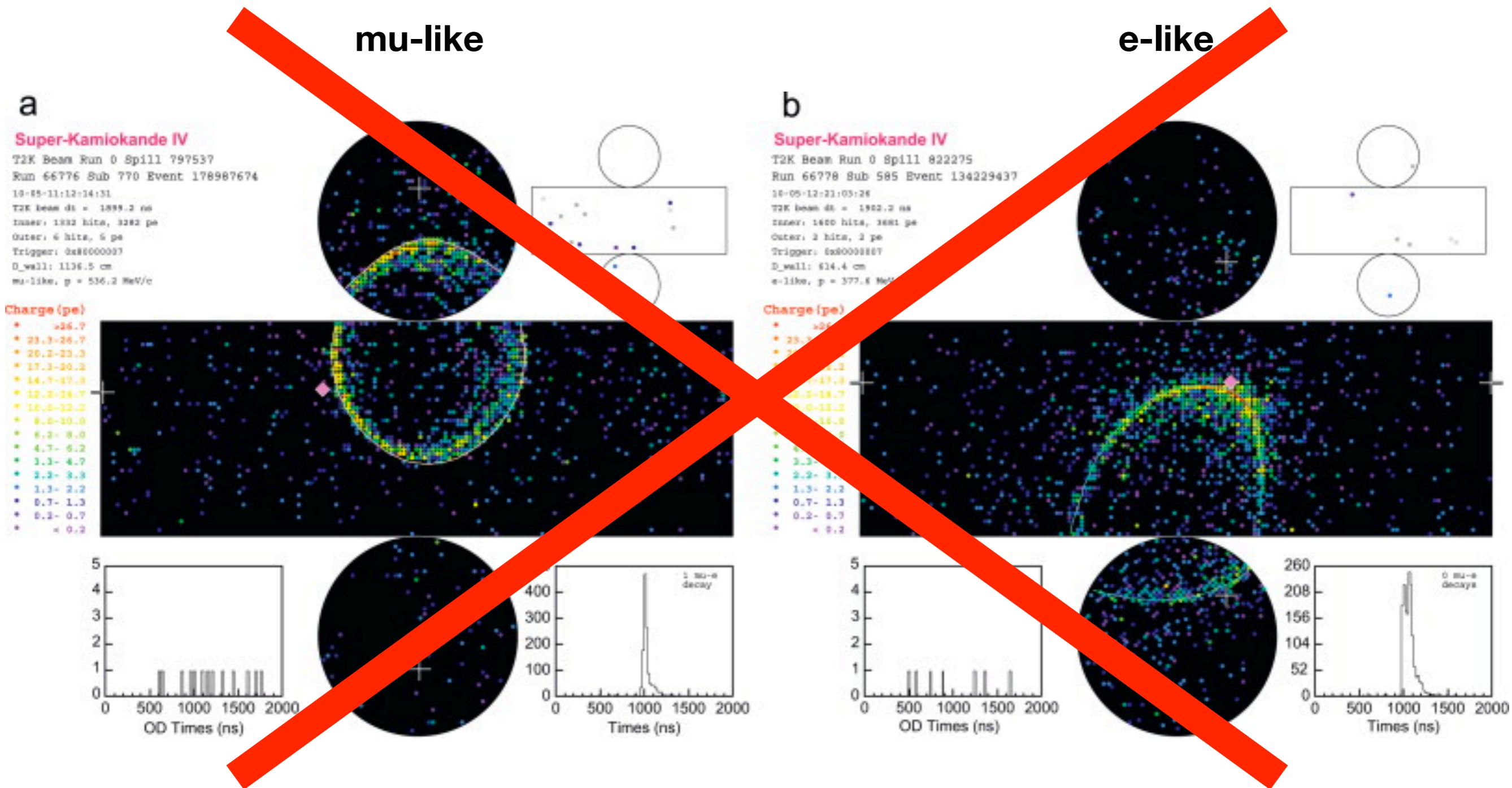
Super-Kamiokande IV

T2K Beam Run 0 Spill 822275
Run 66778 Sub 585 Event 134229437
10-05-12:21:03:28
T2K beam dt = 1902.2 ns
tsize: 1600 hits, 3681 pe
Outer: 2 hits, 2 pe
Trigger: 6x8000007
D_wall: 614.4 cm
e-like, p = 377.6 MeV/c

**Charge (pe)**

- >26.7
- 23.3-26.7
- 20.2-23.3
- 17.3-20.2
- 14.7-17.3
- 12.2-14.7
- 10.0-12.2
- 8.0-10.0
- 6.2-8.0
- 4.7-6.2
- 3.3-4.7
- 2.3-3.3
- 1.3-2.3
- 0.7-1.3
- 0.2-0.7
- = 0.2





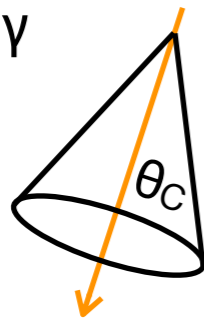
The current analysis region (<30 MeV) has only 100~200 hits!

Almost all PMTs have single p.e. hit.

Cherenkov Angle & Decay Electron

- Low energy muon events are likely to have their decay electrons at later times.
- Cherenkov opening angle is a nice discriminant for particle identification.

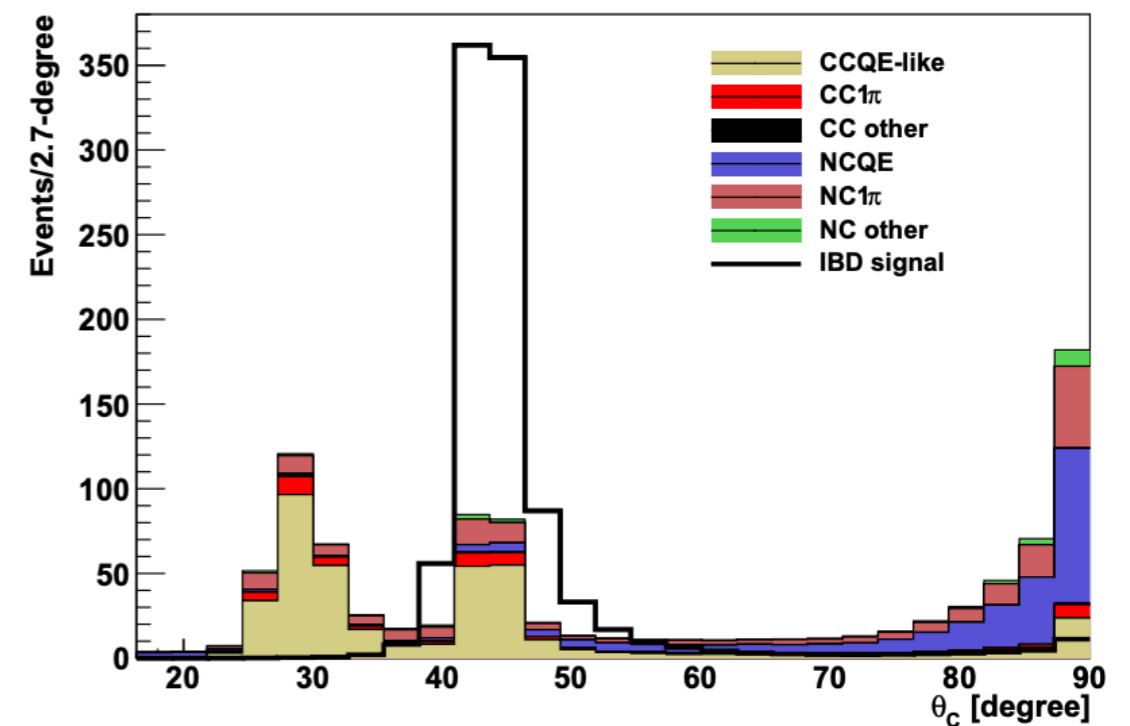
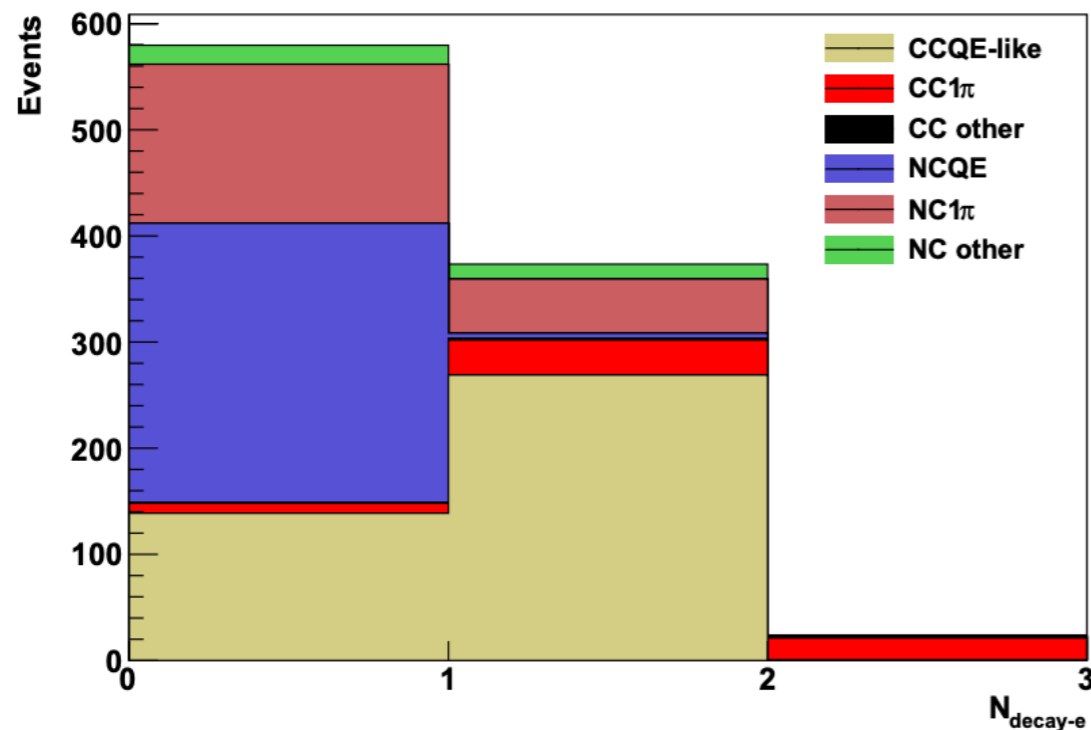
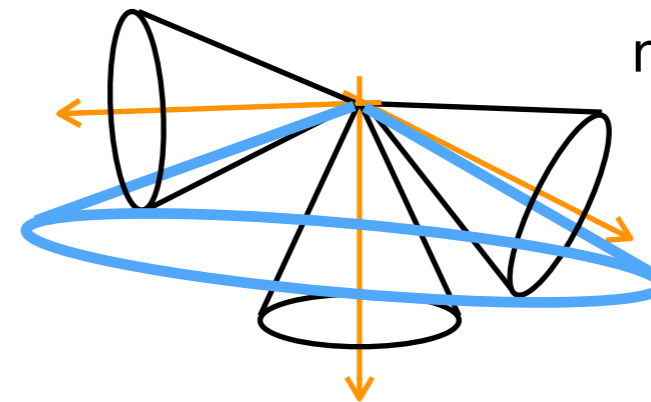
e, single- γ



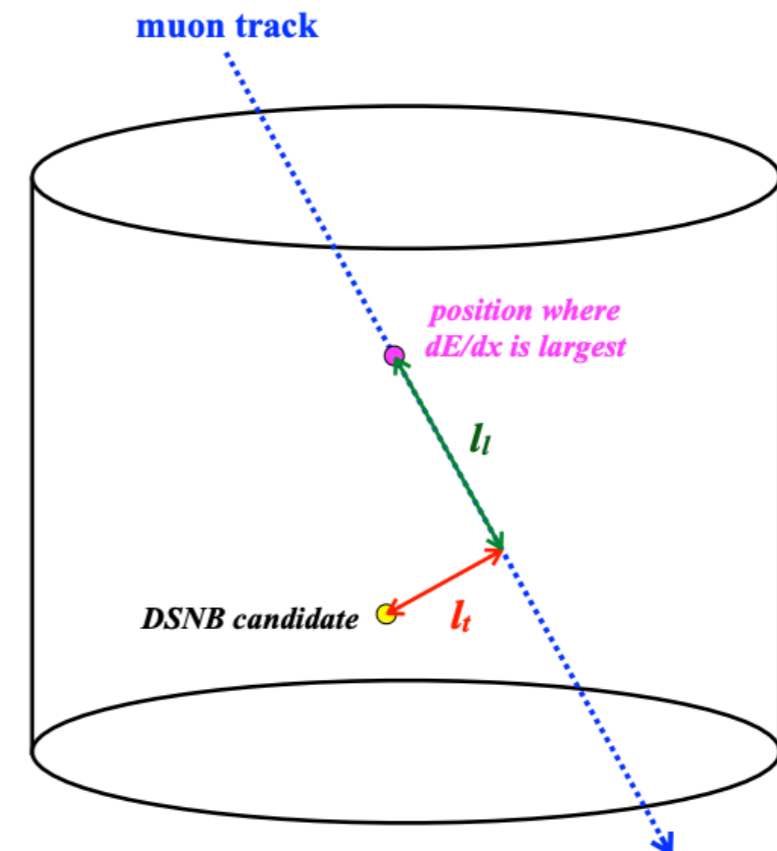
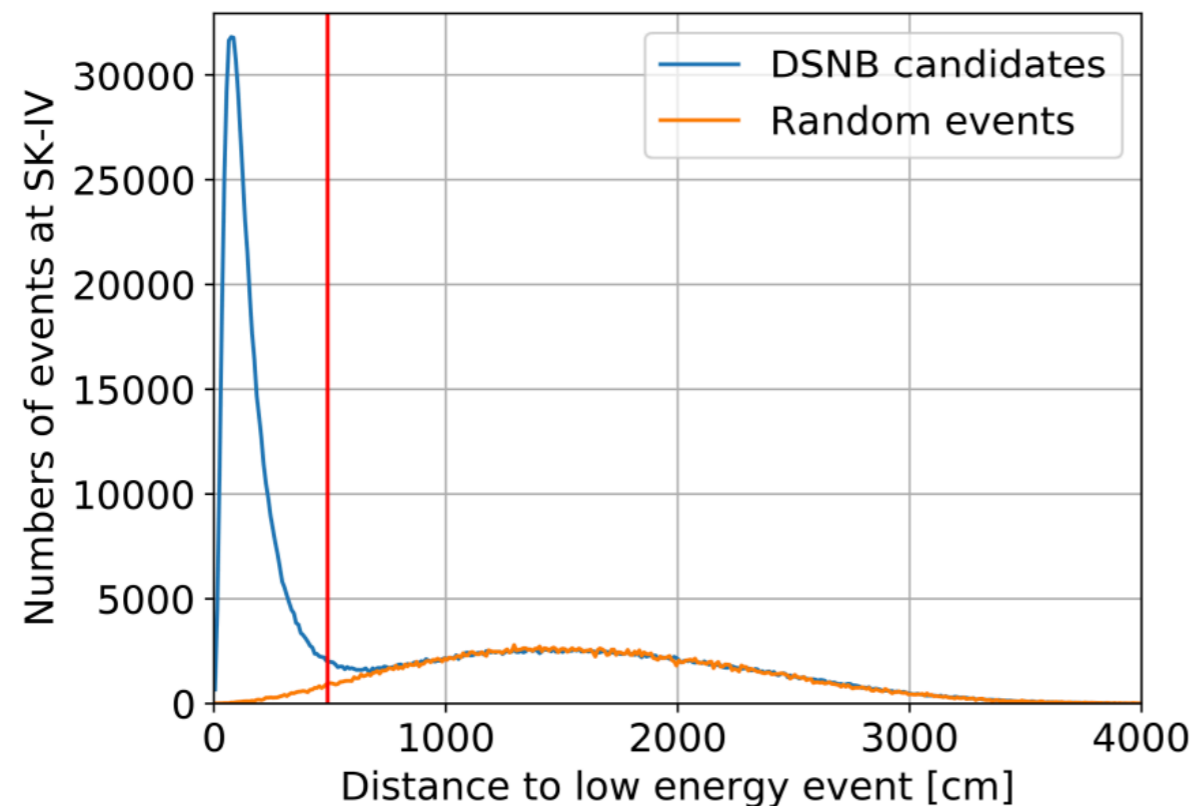
μ, π



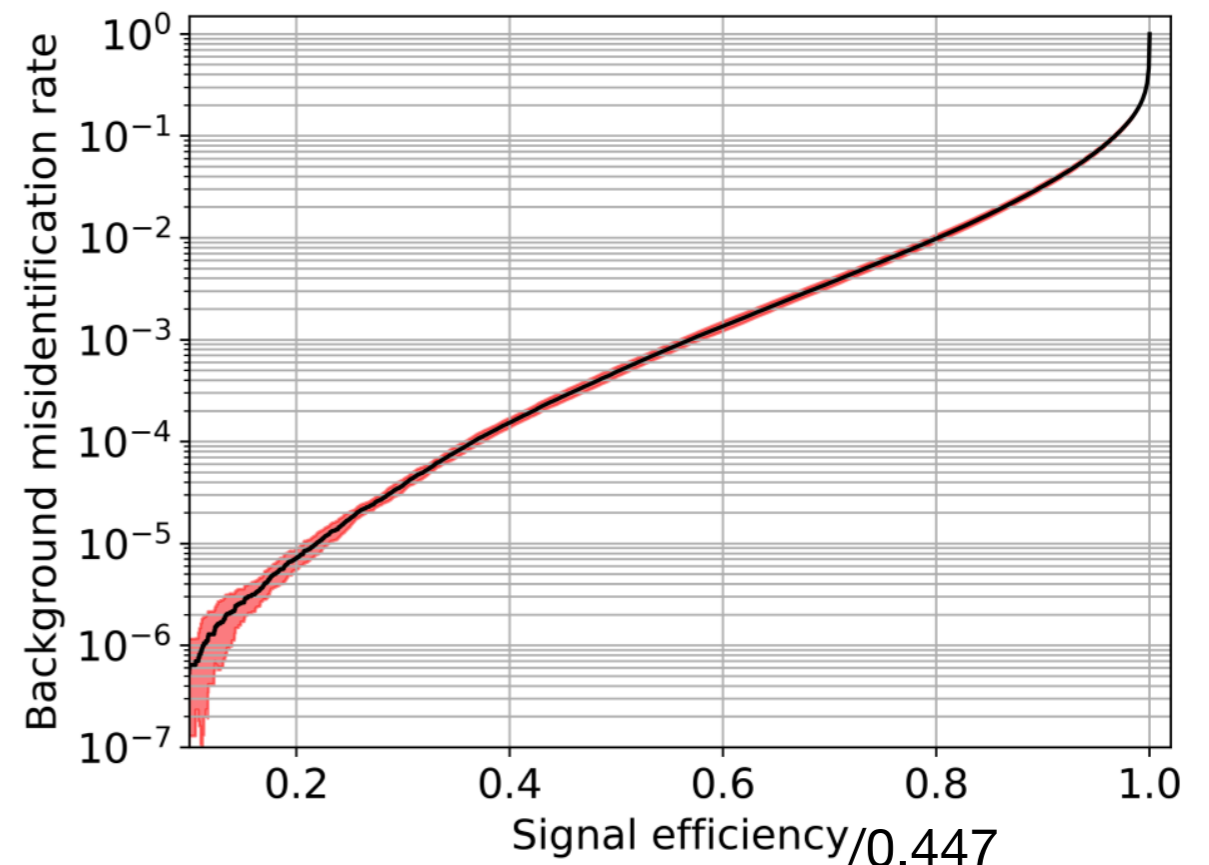
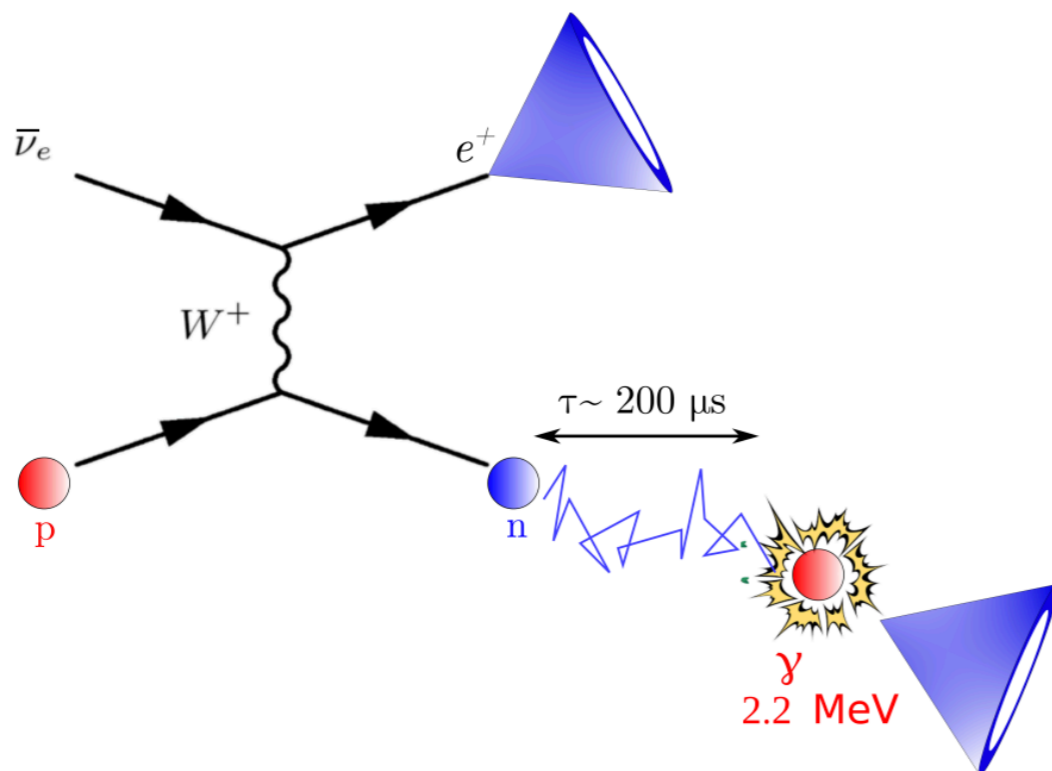
multiple- γ



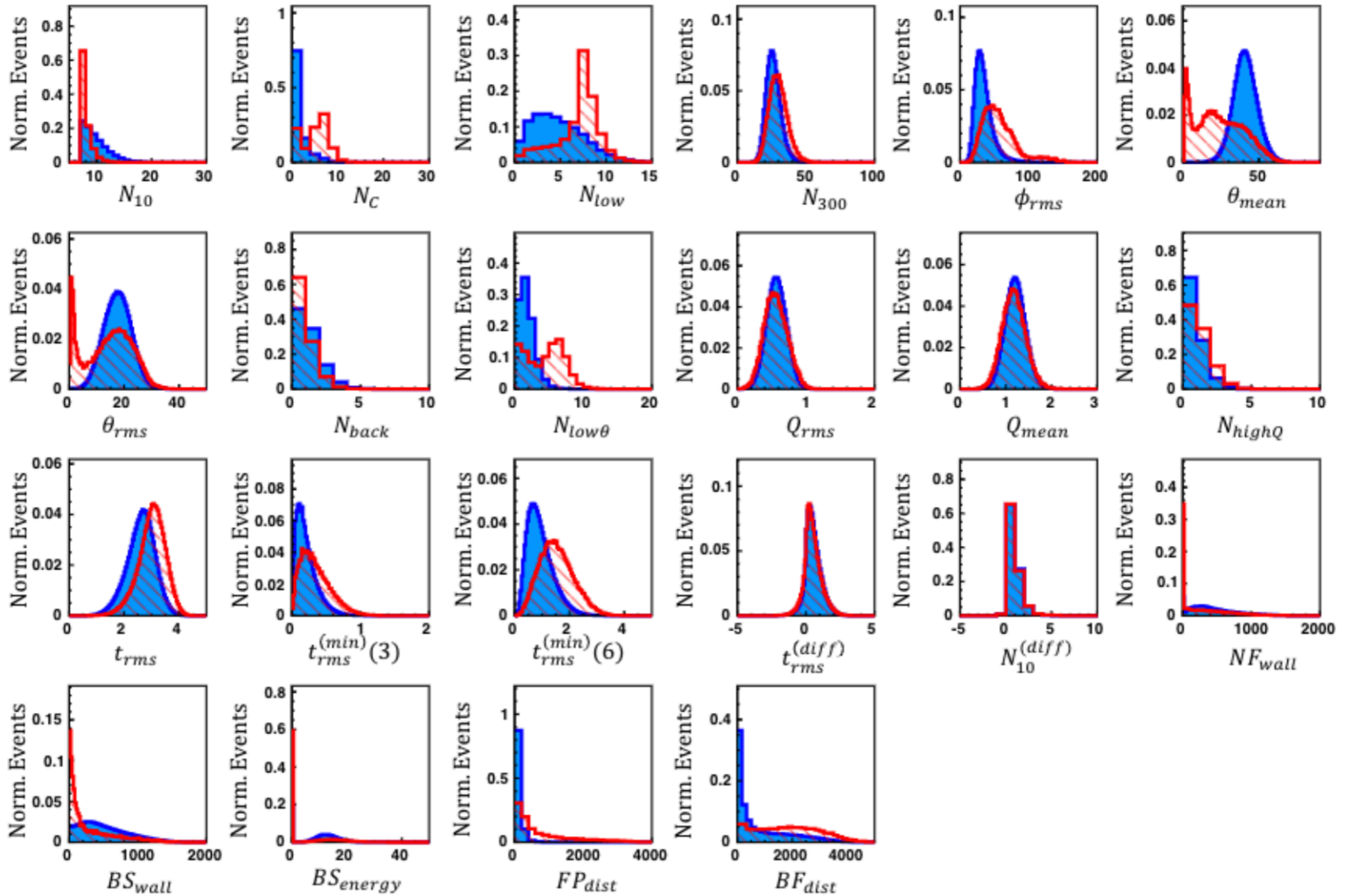
- Clustered events (in time and position) are likely to be spallation products.
- More powerful cuts are made by using muon reconstruction information.
 - Events close to muon track in time and position are likely spallation.
 - Large energy depositing muons would produce spallation.
 - **These efforts achieved to reject >95% spallation background.**



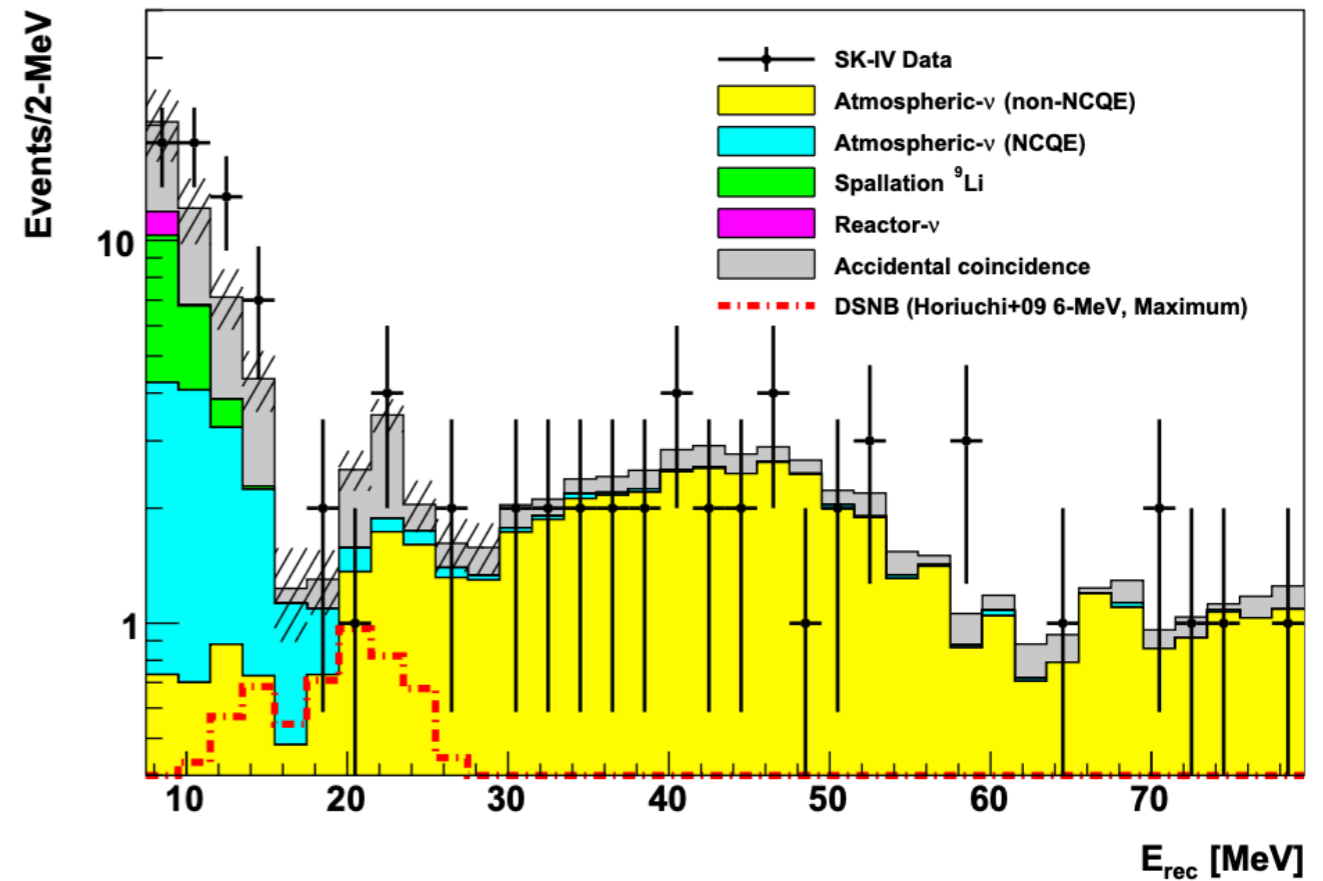
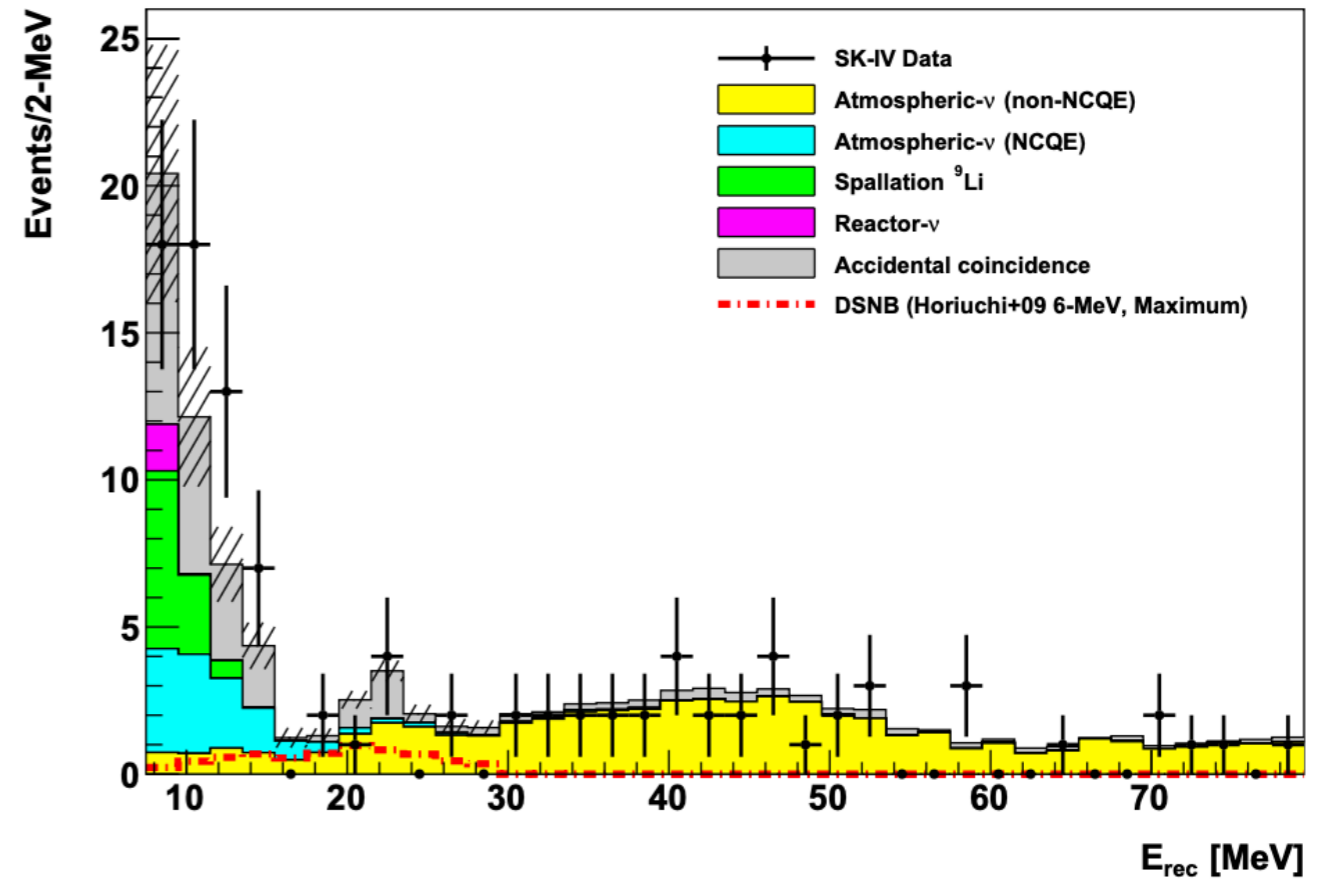
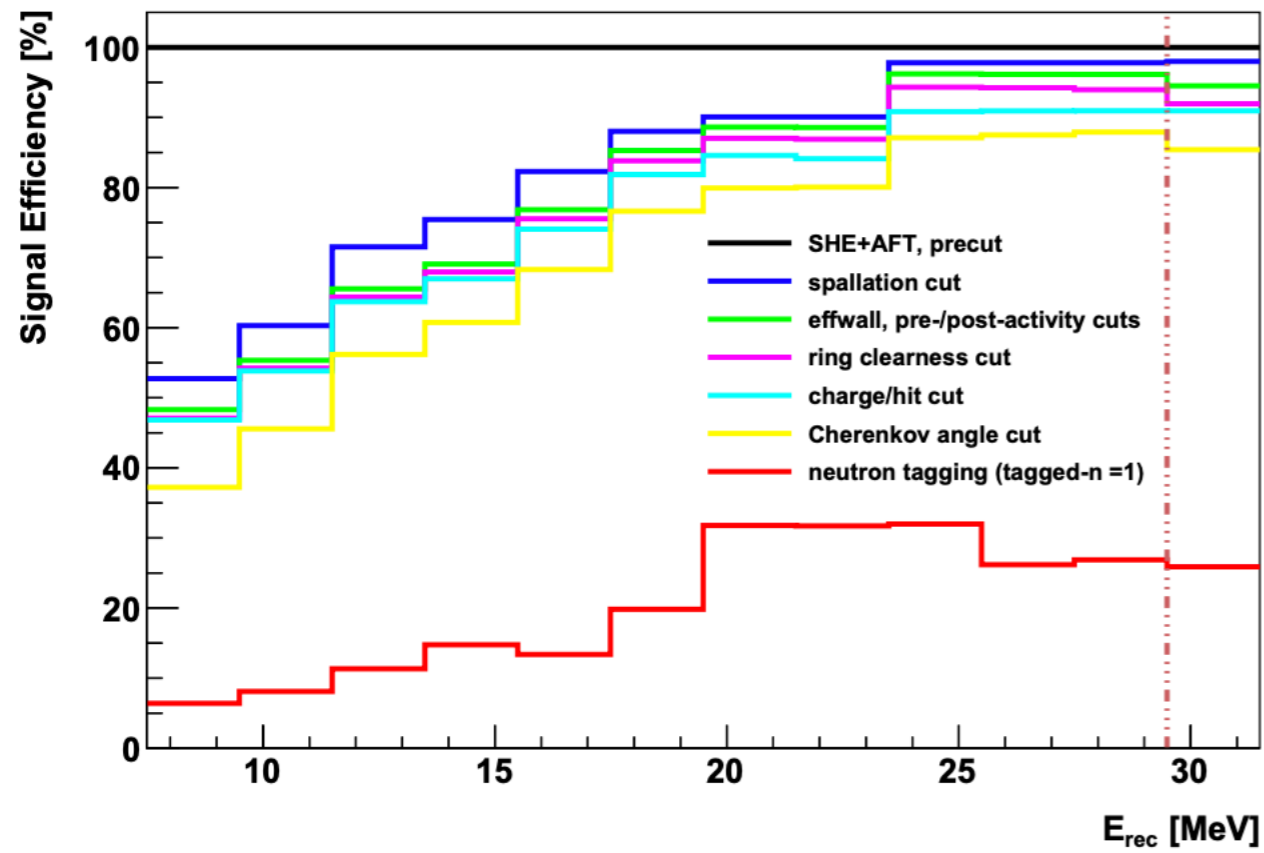
- An additional DAQ window is taken until 500 μs later than the primary event (\geq SK-IV).
- **Very subtle sign for the 2.2 MeV γ (visible is <2.2 MeV; only ~ 10 hits).**
 - SK reconstruction is possible above 3.5 MeV visible energy.
 - **BDT** is implemented to catch this subtle sign.
 - The 22 variables: hit pattern, geometrical information, etc
- **20~30% signal (=neutron) efficiency against $10^{-3}\sim 10^{-4}$ background (=no neutron) rejection.**



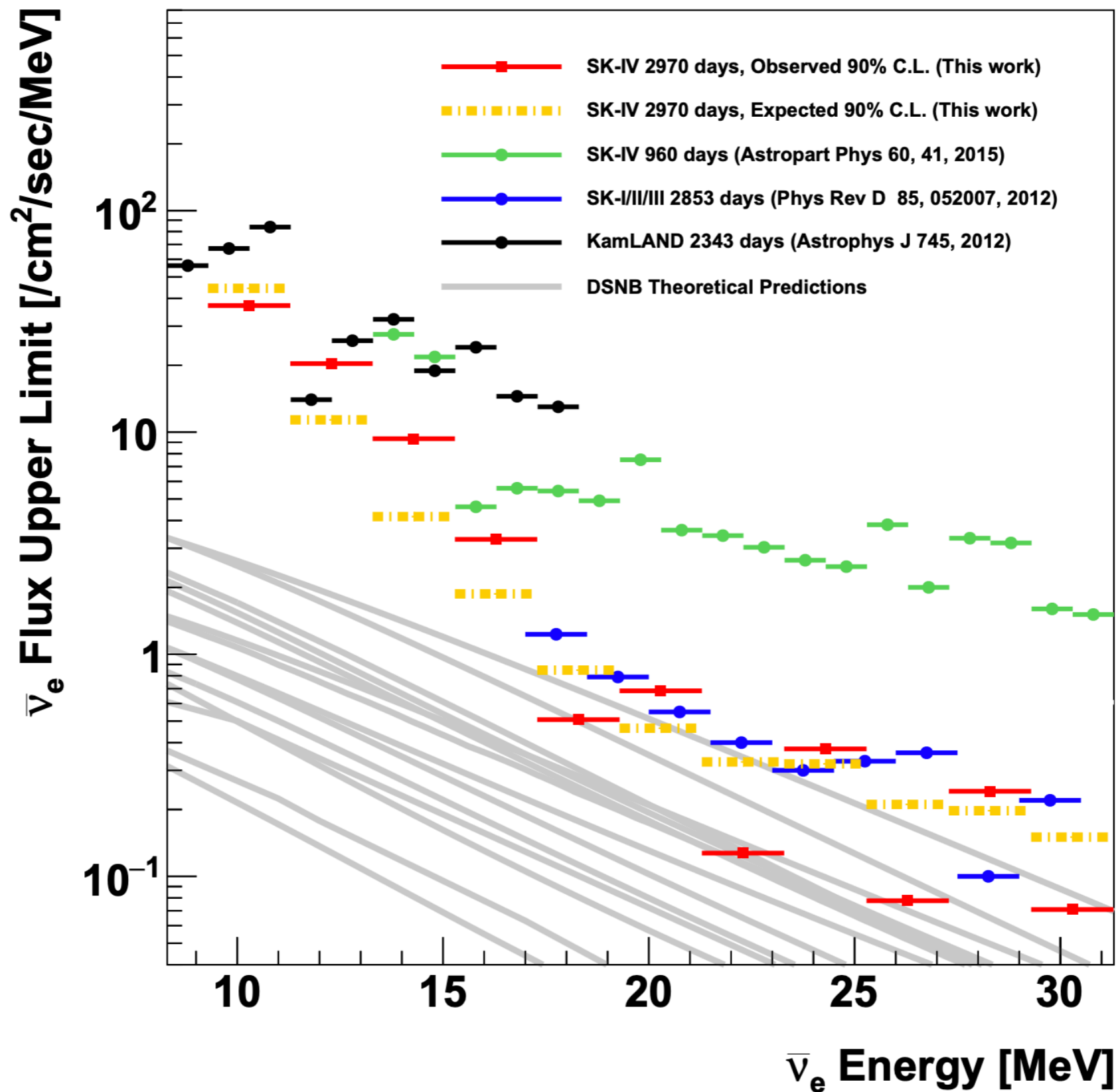
Neutron Tagging: The 22 Variables for BDT



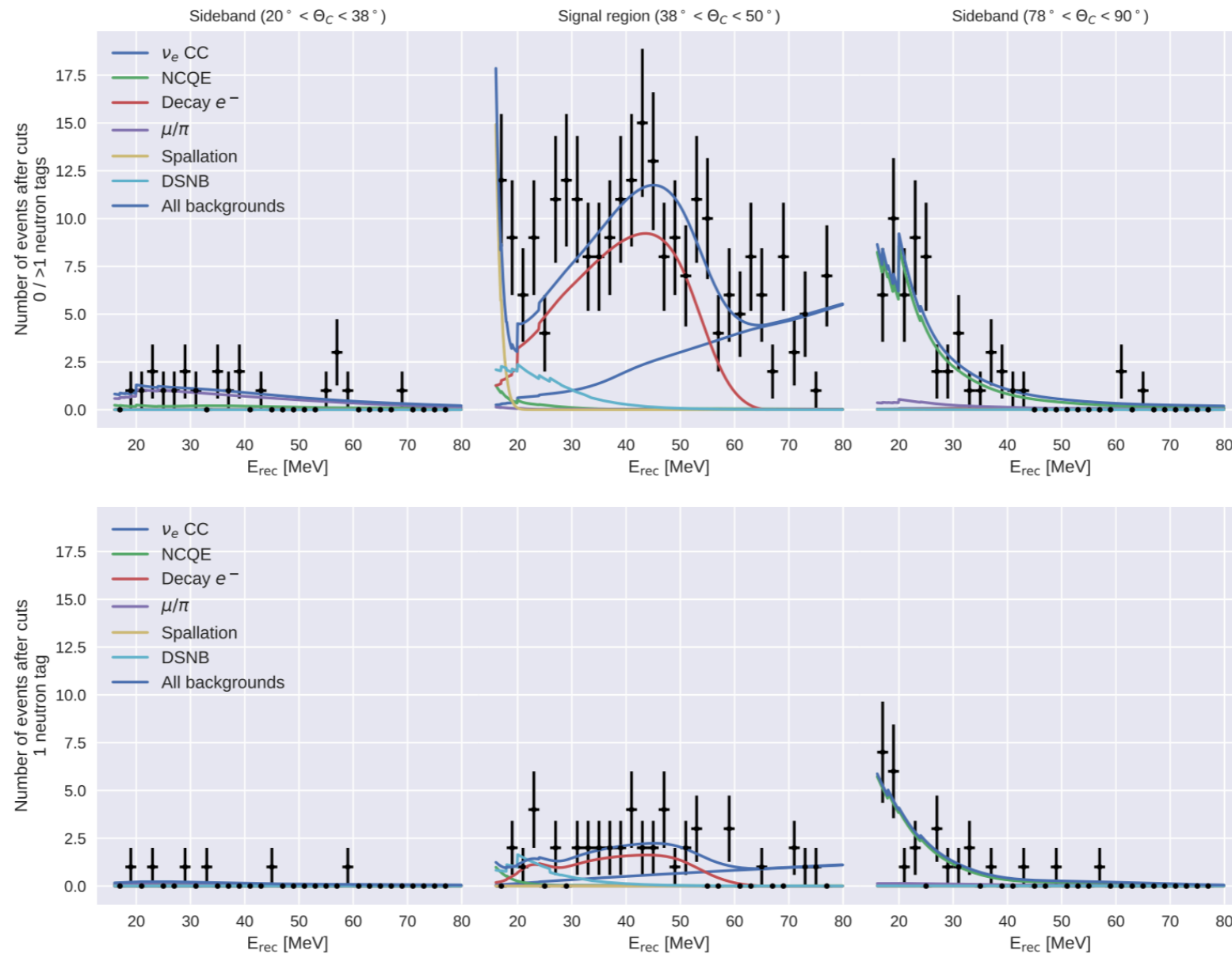
Selected Events



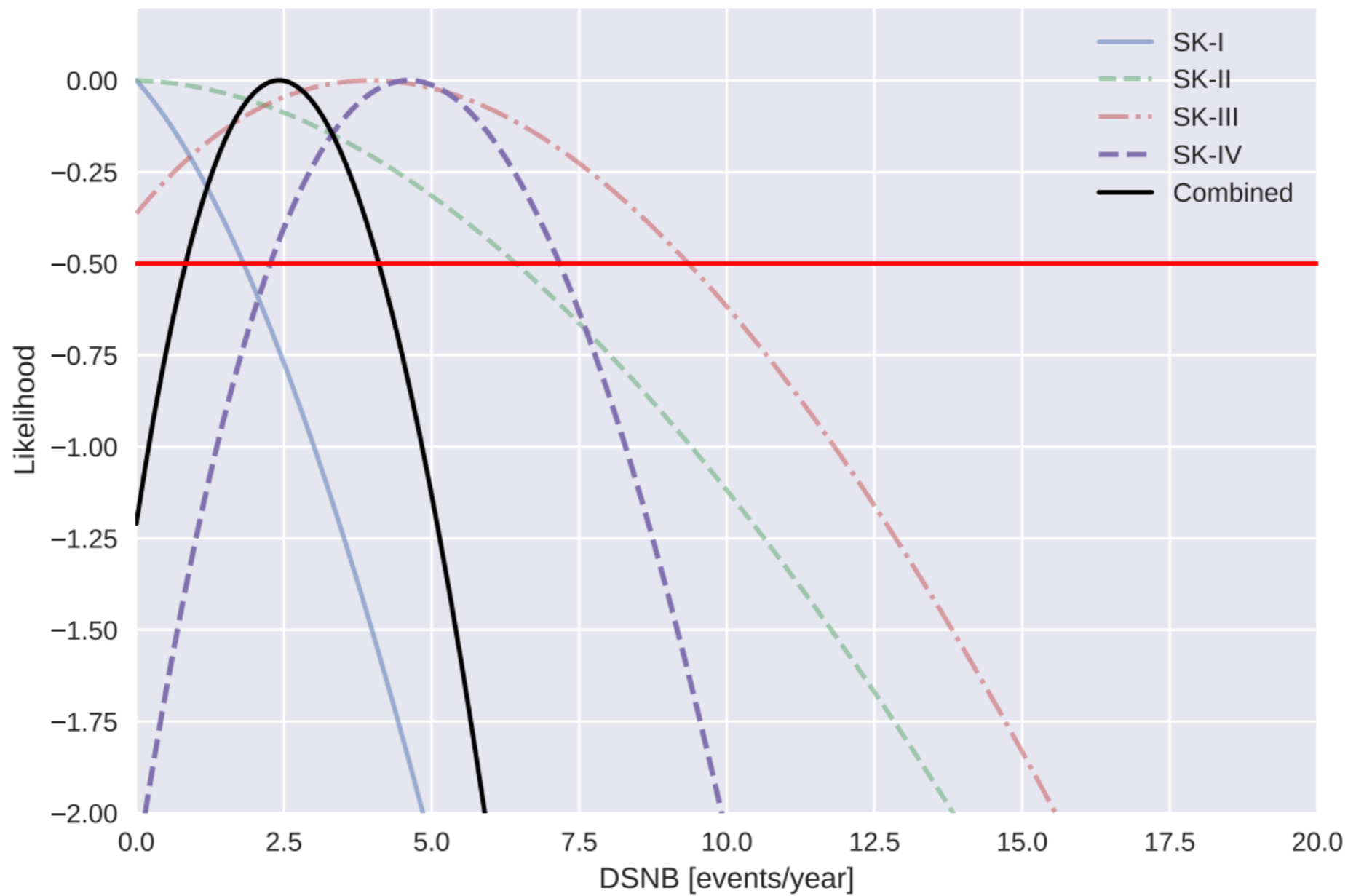
Model-Independent Upper Limit



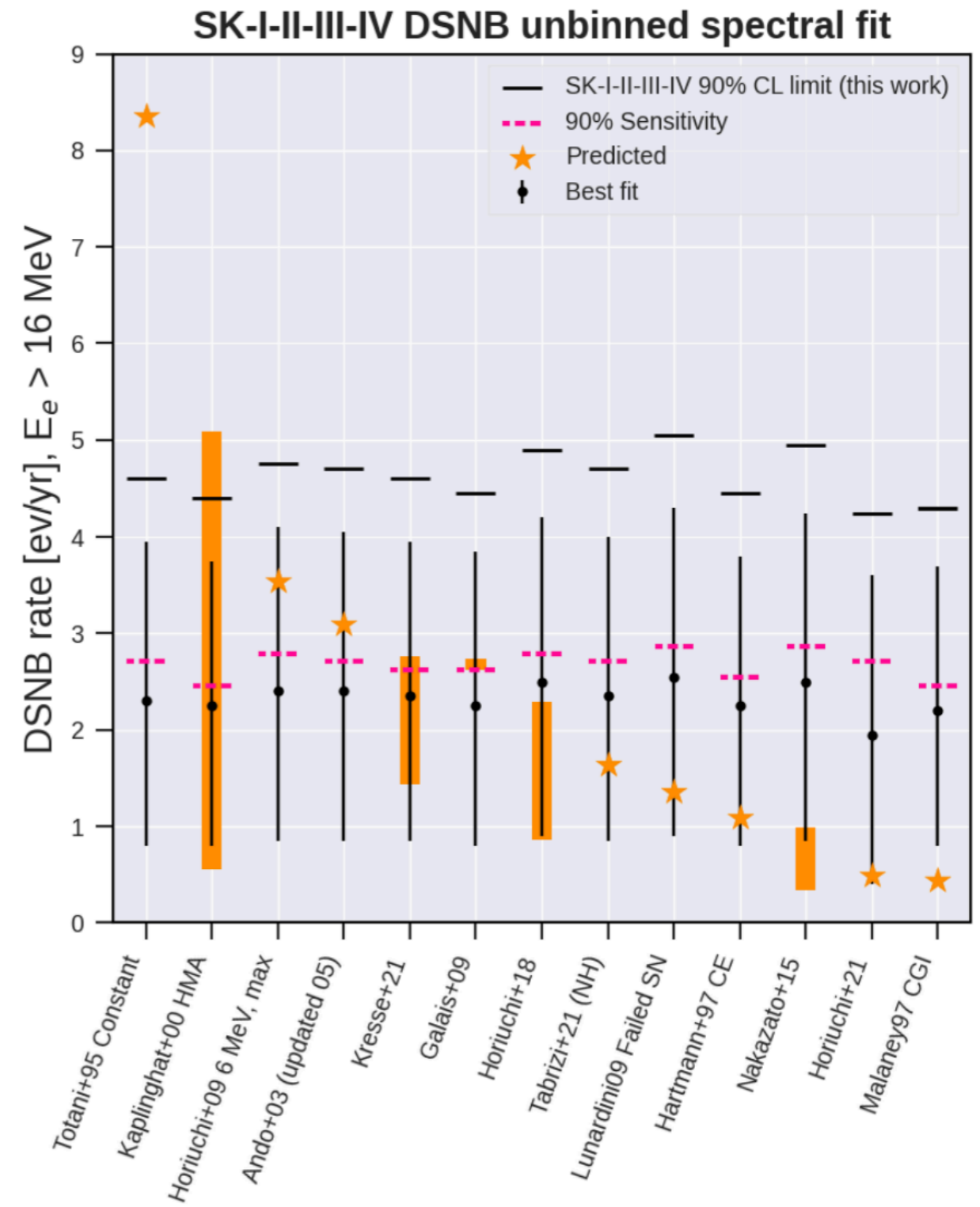
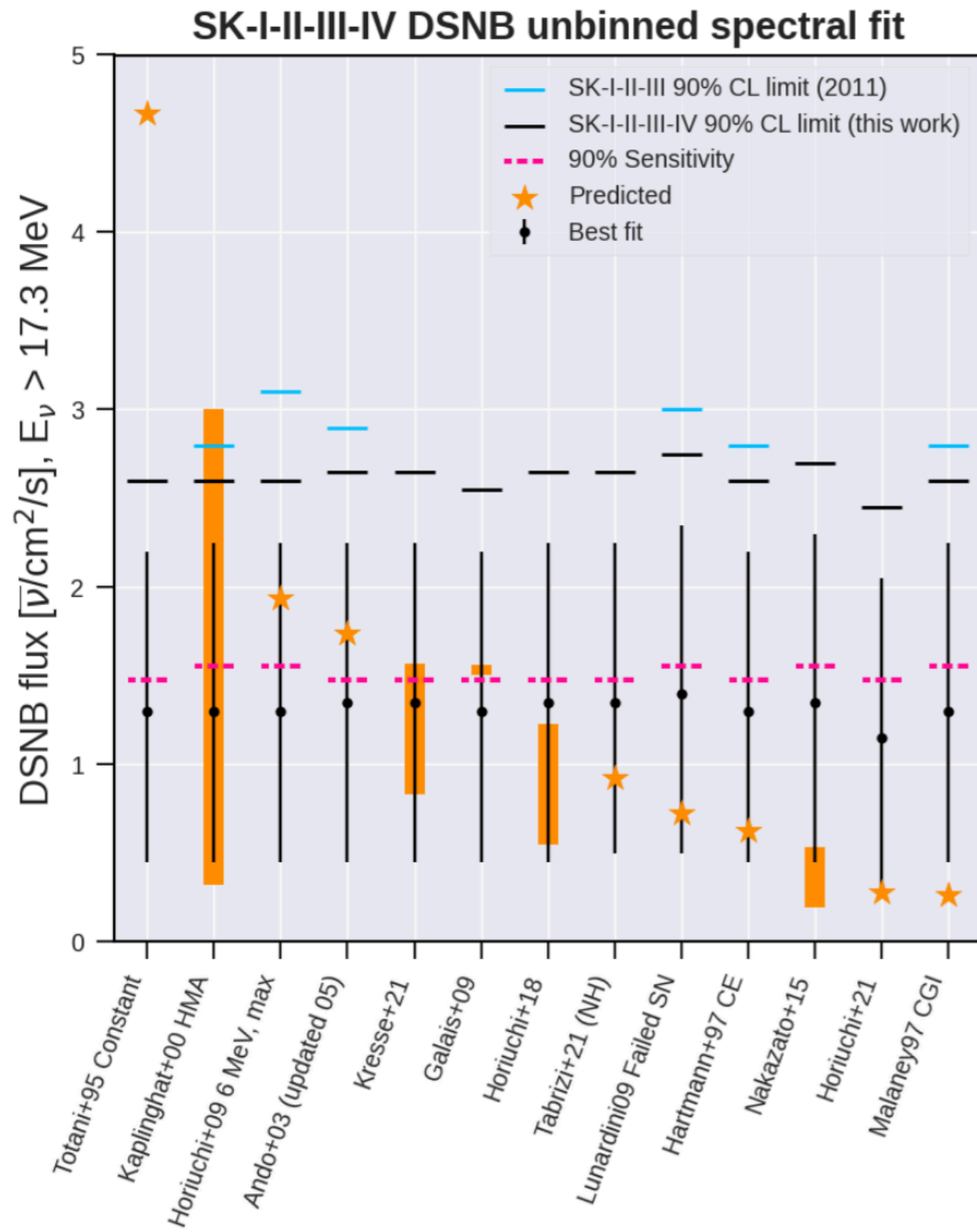
- We also performed more dedicated analysis for each DSNB model.
- We fit our observed data with signal and background PDFs.
- Here we make use of no tagged region as well.
- This fitting can be combined with SK-I,II,III data (where neutron tagging could not be used).



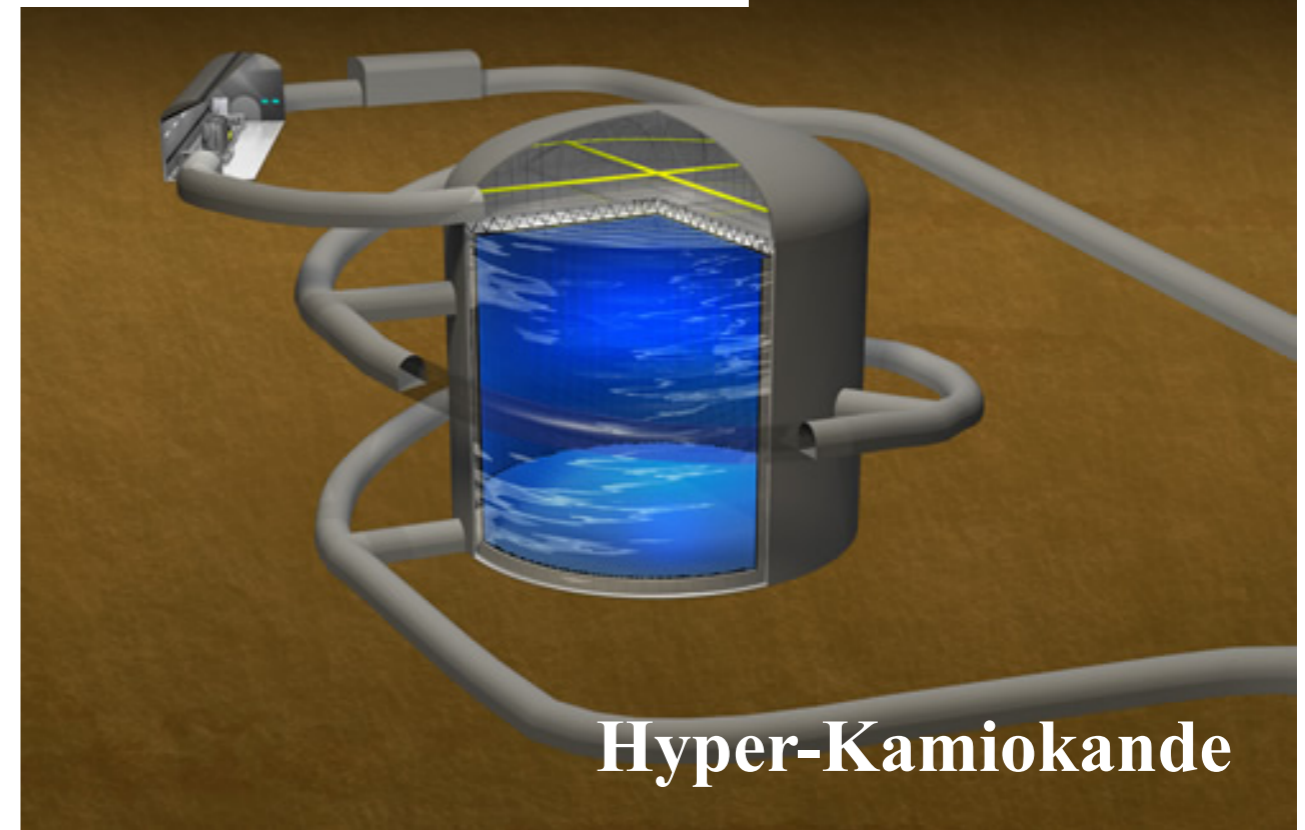
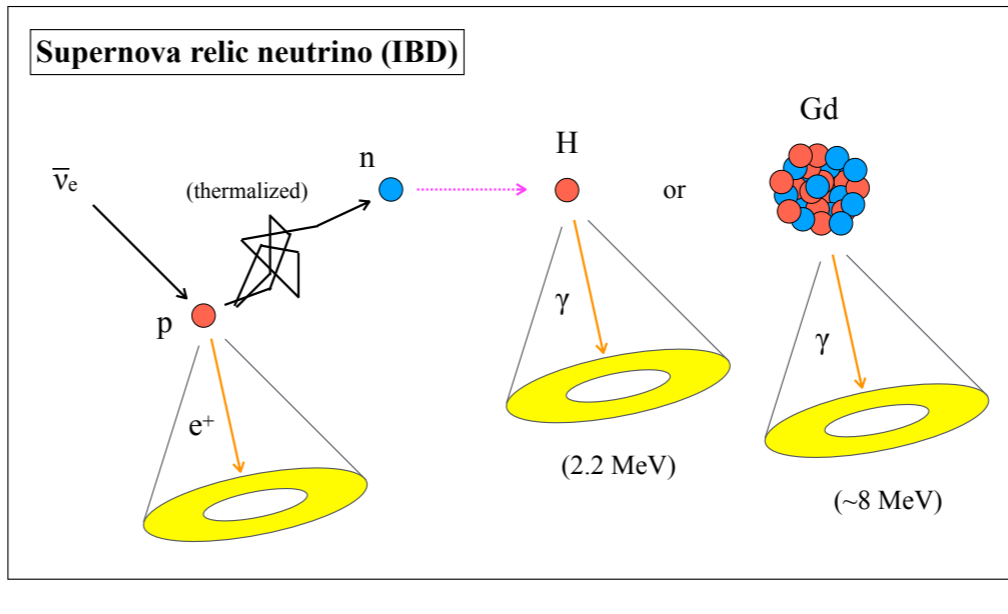
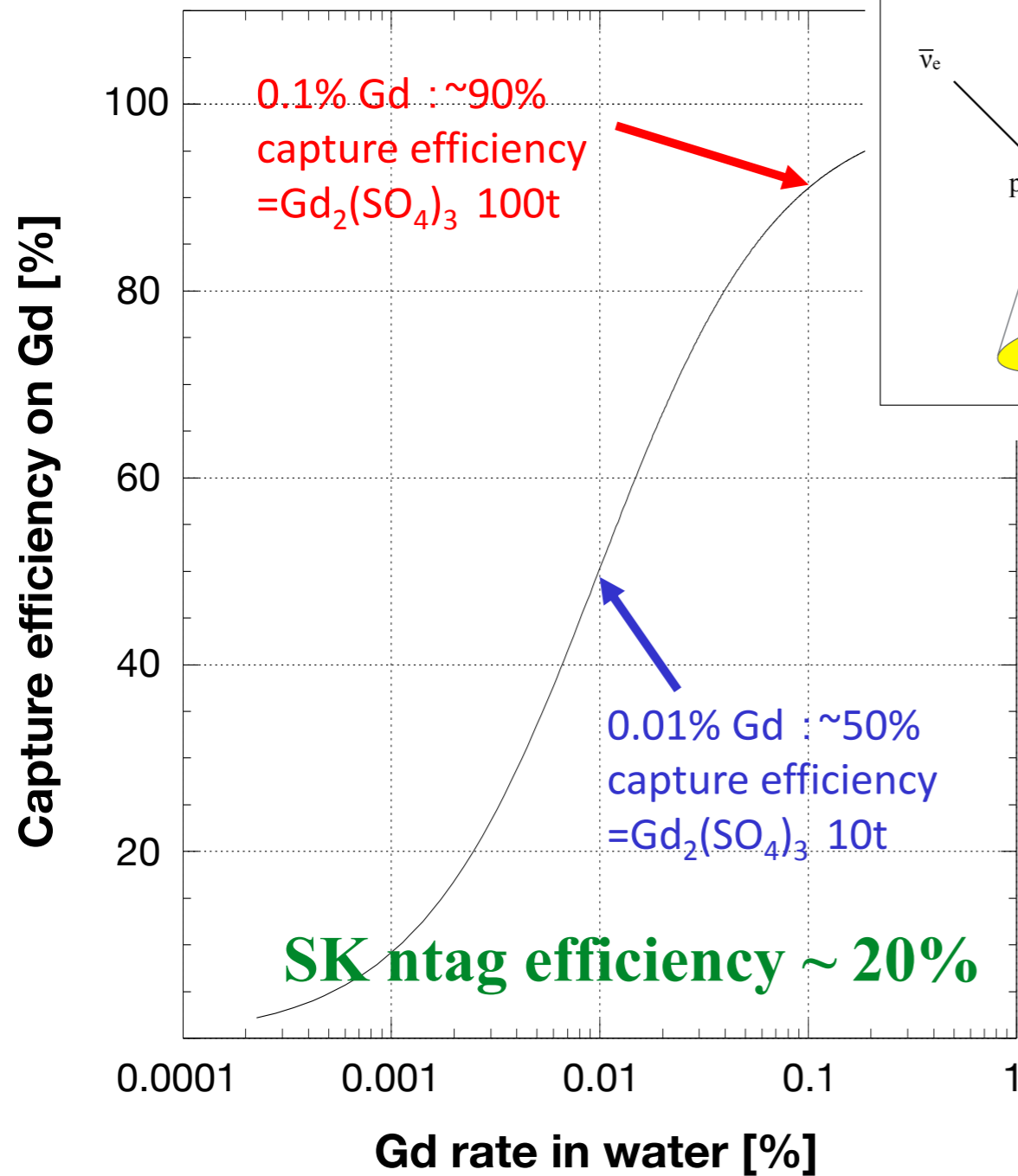
Combination with SK-I,II,III



Upper Limits by Spectral Fitting



SK-Gd

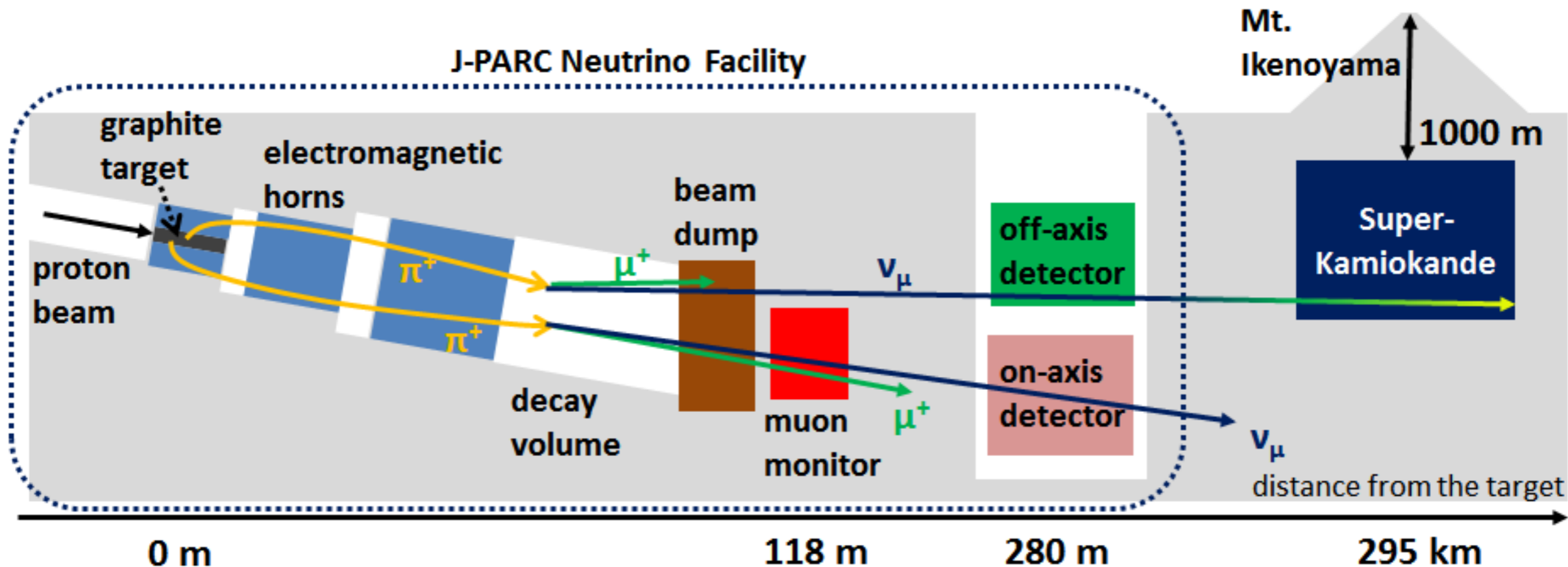


H: ~0.3 barn, 2.2 MeV γ
 Gd: ~50 kbarn, ~8 MeV γ

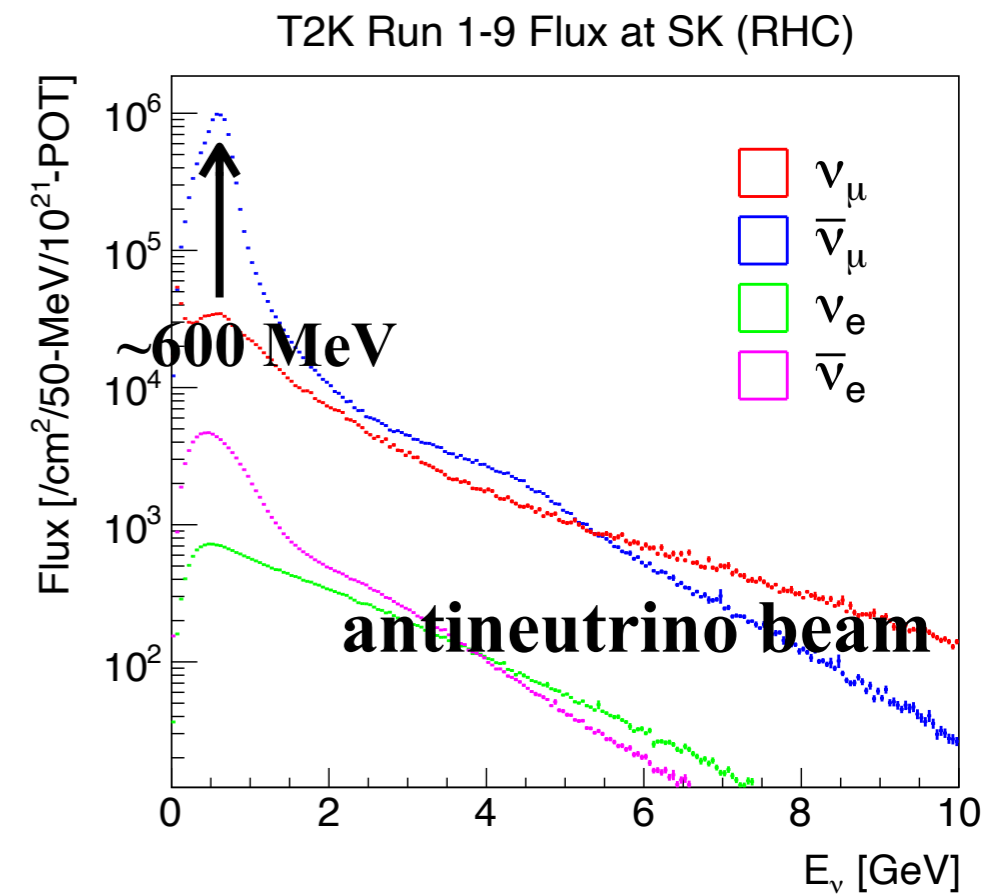
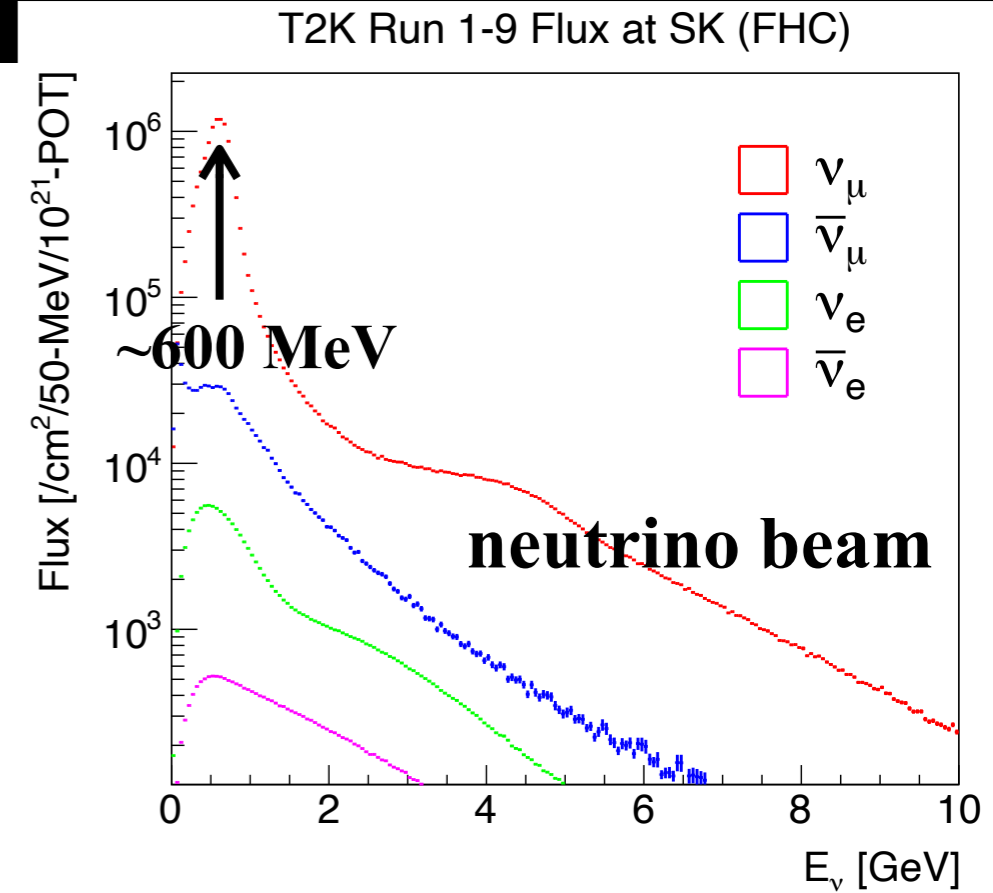
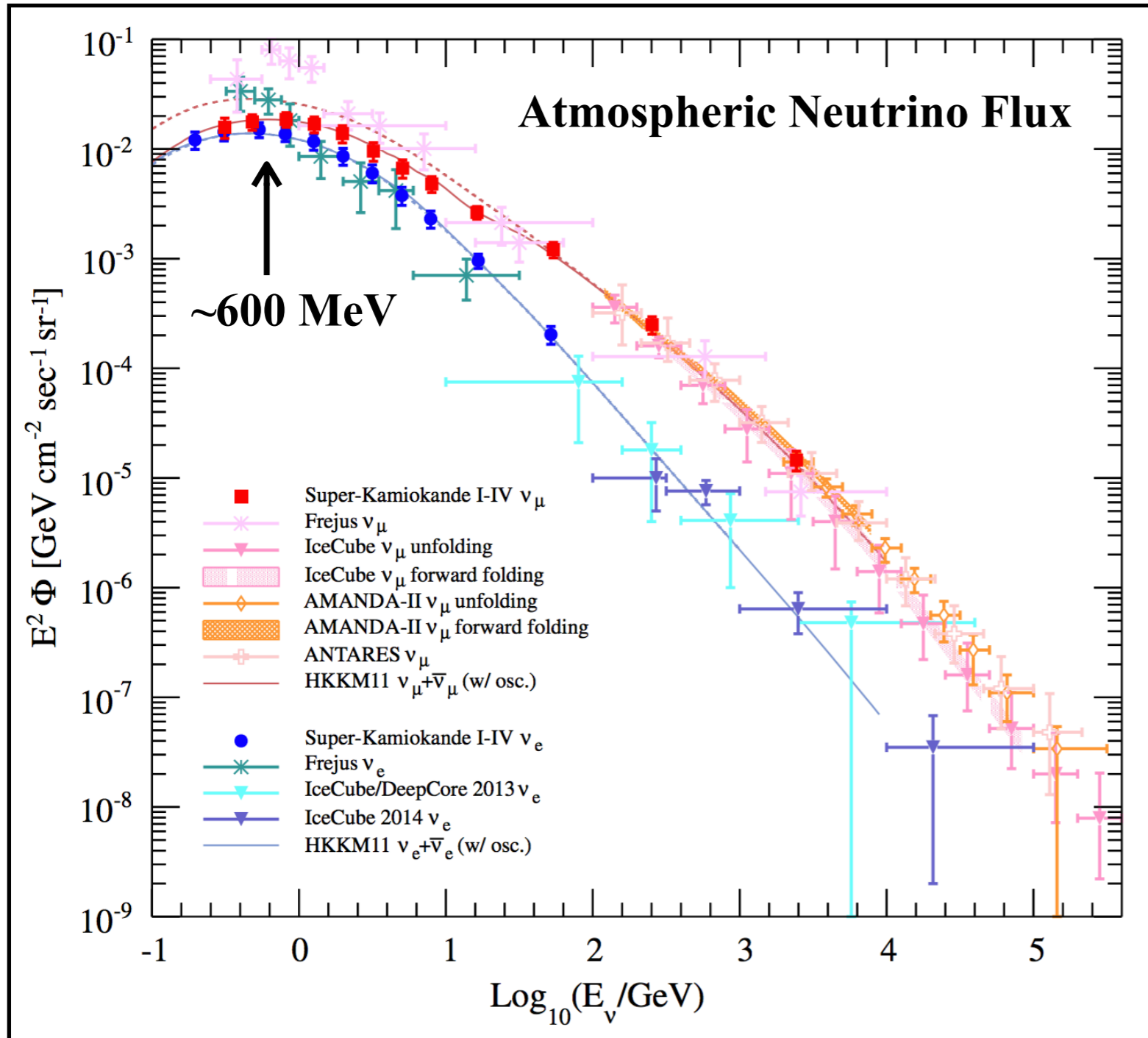
Fiducial mass: ~8.4 times larger than SK
 Better photosensor: higher ntag efficiency

Improvement from Beam Experiments

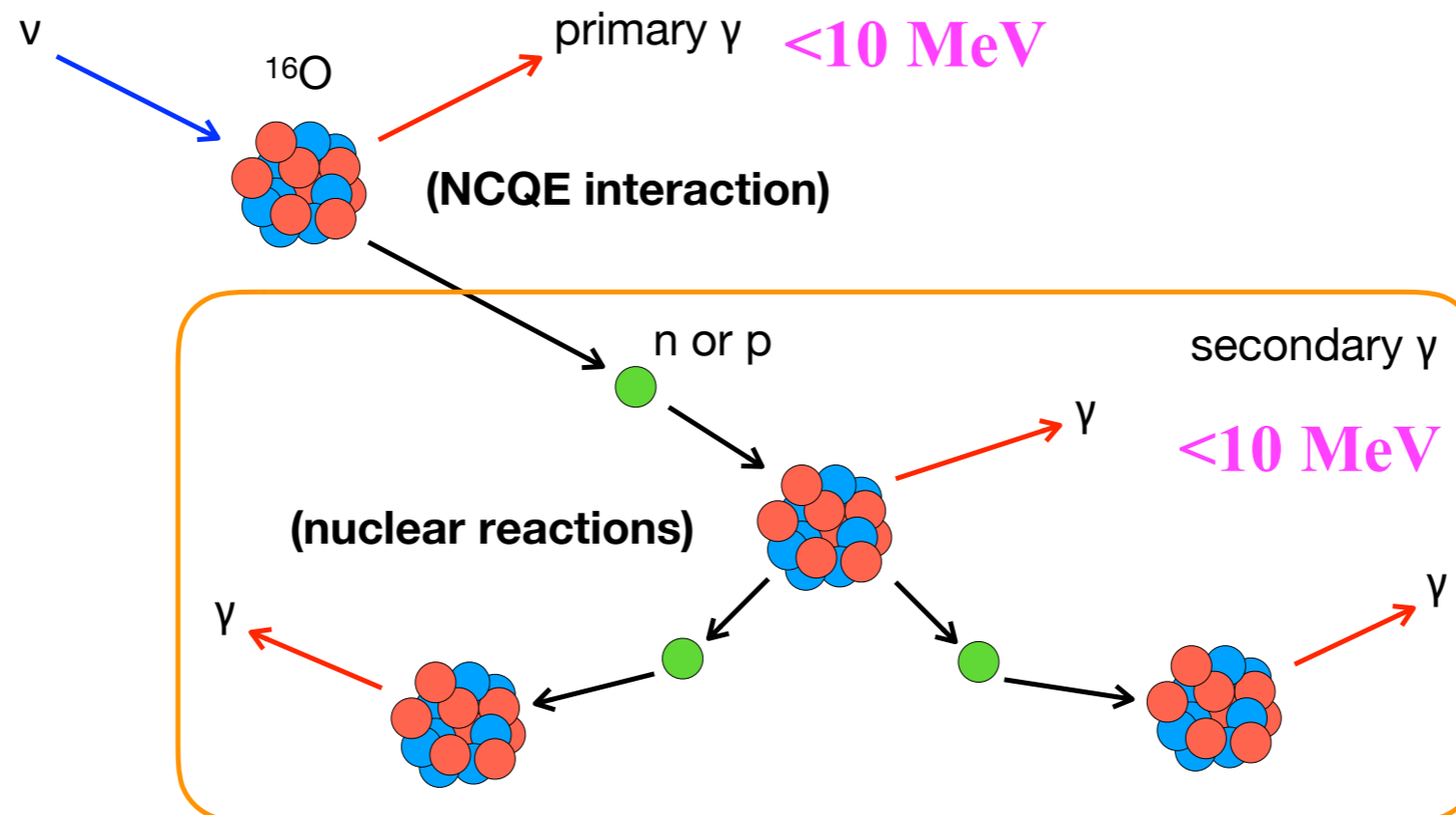
- Bunched proton beams (8 bunch per spill) are injected on the graphite target to produce hadrons (pions and kaons).
- Hadrons are focused by magnetic fields and decay to produce neutrino beams.
- **Beam polarity (neutrino or antineutrino) is changed by the magnetic field direction.**
- Neutrinos are detected at 295 km away Super-Kamiokande.



Flux: Atmospheric vs. J-PARC

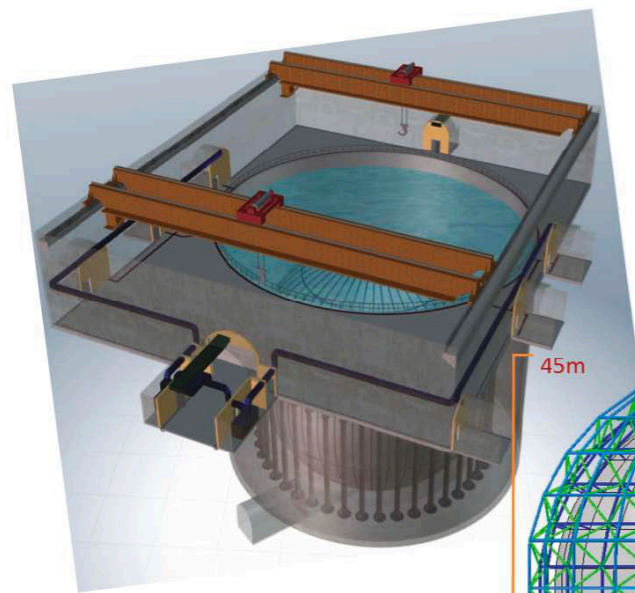


- So far NCQE background was estimated by the simulation based on theories.
 - A **100%** uncertainty was assigned to this channel because of little experimental data.
- Measurements of neutrino and antineutrino NCQE interactions are performed in T2K.
 - Similar energy region, large statistics, well known flux, pure sample
 - This improves the uncertainty **from 100% to 60%**.



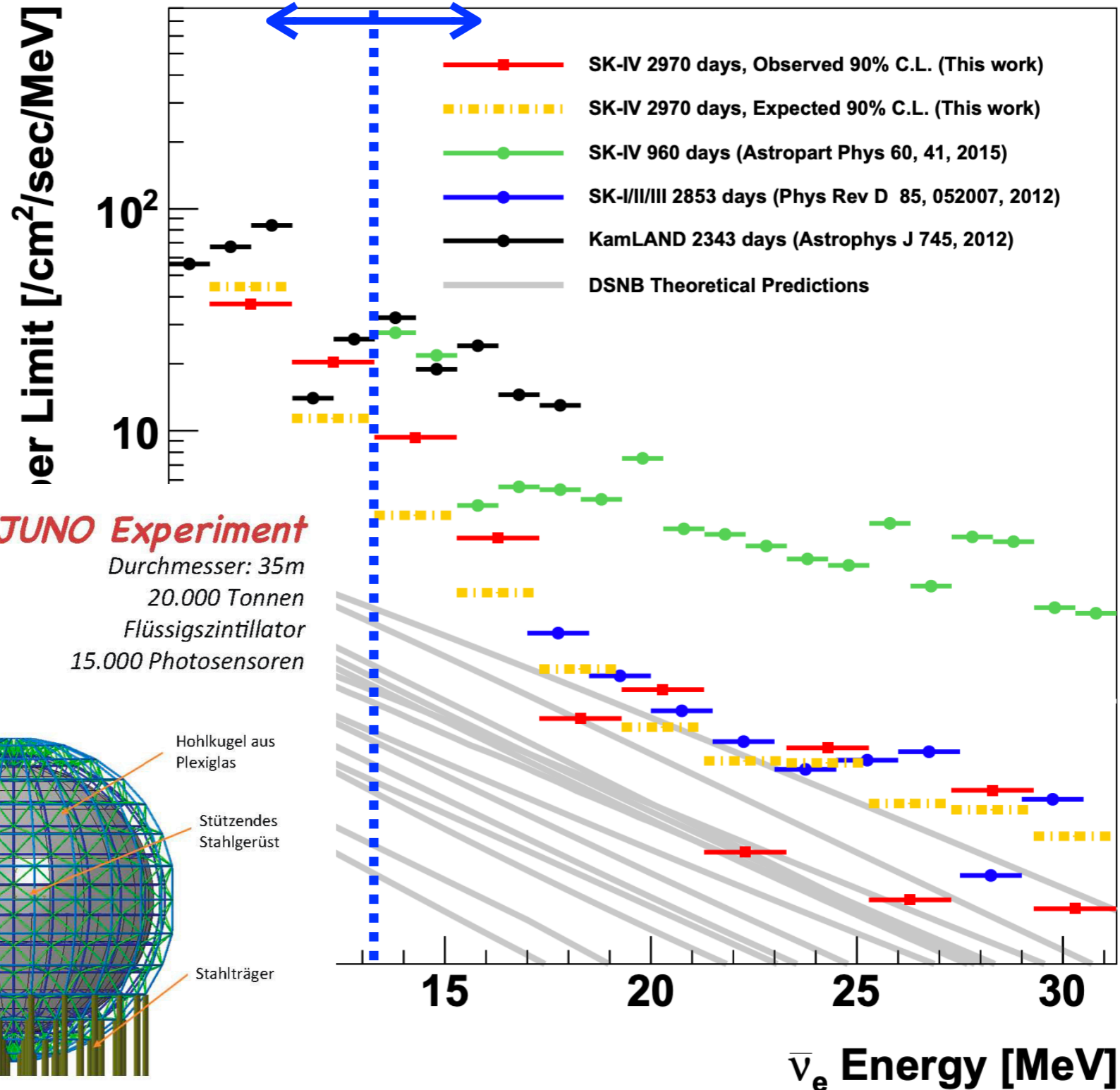
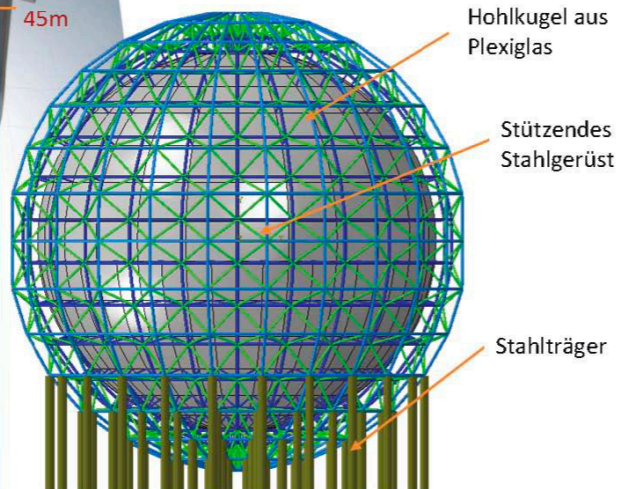
KamLAND, JUNO, DUNE?

SK-Gd, HK, HK-Gd?



JUNO Experiment

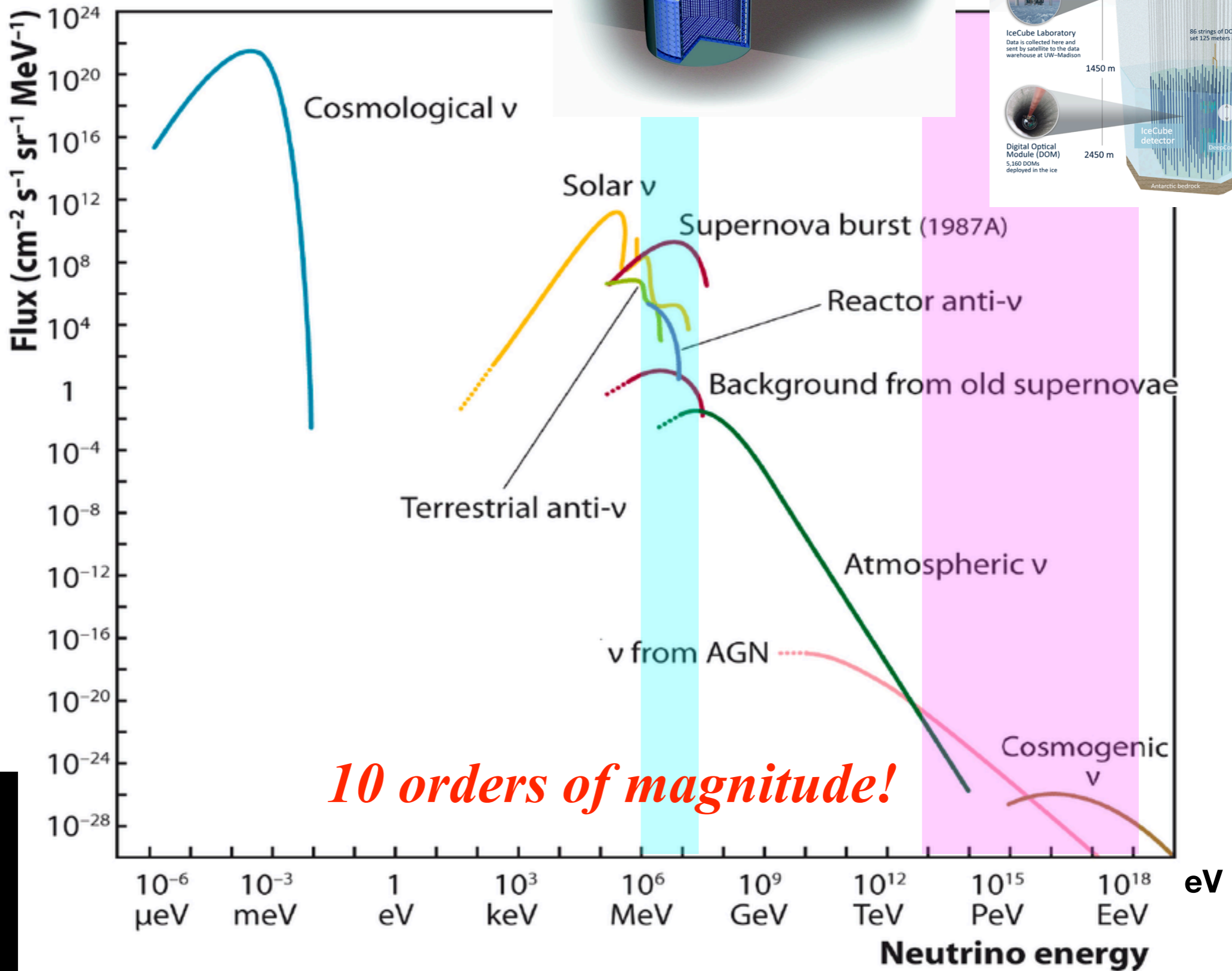
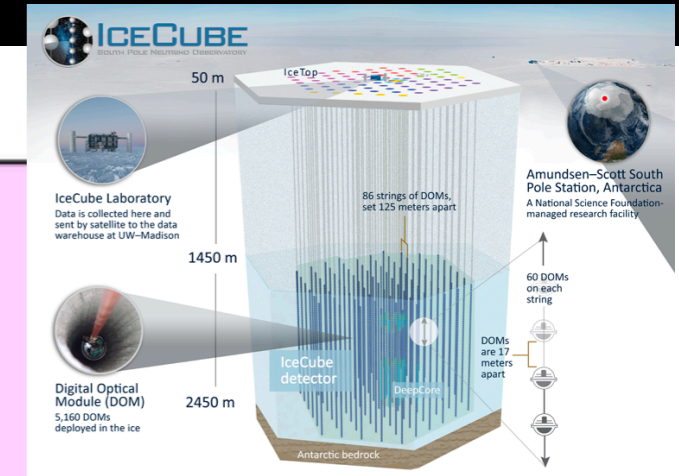
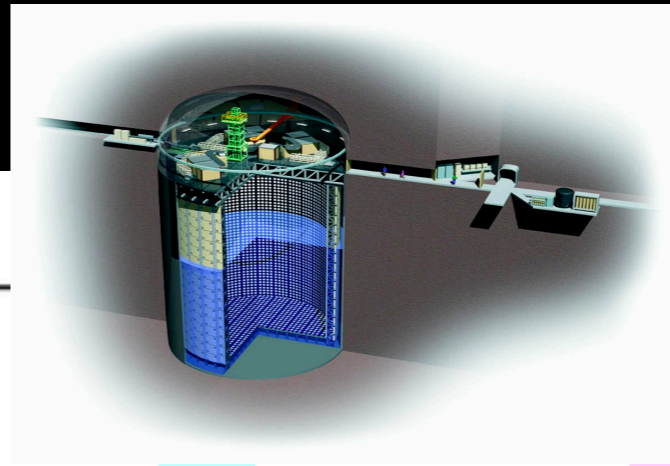
Durchmesser: 35m
20.000 Tonnen
Flüssigszintillator
15.000 Photosensoren



- A new DSNB search was performed at Super-Kamiokande with a lot of improvements on event selection and background estimation as well as larger statistics.
- Limits from both of model-independent and spectral fitting analyses excluded most optimistic models and are close to more realistic model predictions (within a factor).
- SK-Gd starting now, and Hyper-Kamiokande approved. *Future is bright!*

Thanks for your attention!

Same Neutrinos, but ...



Supplements

Neutrino Heating Scenario

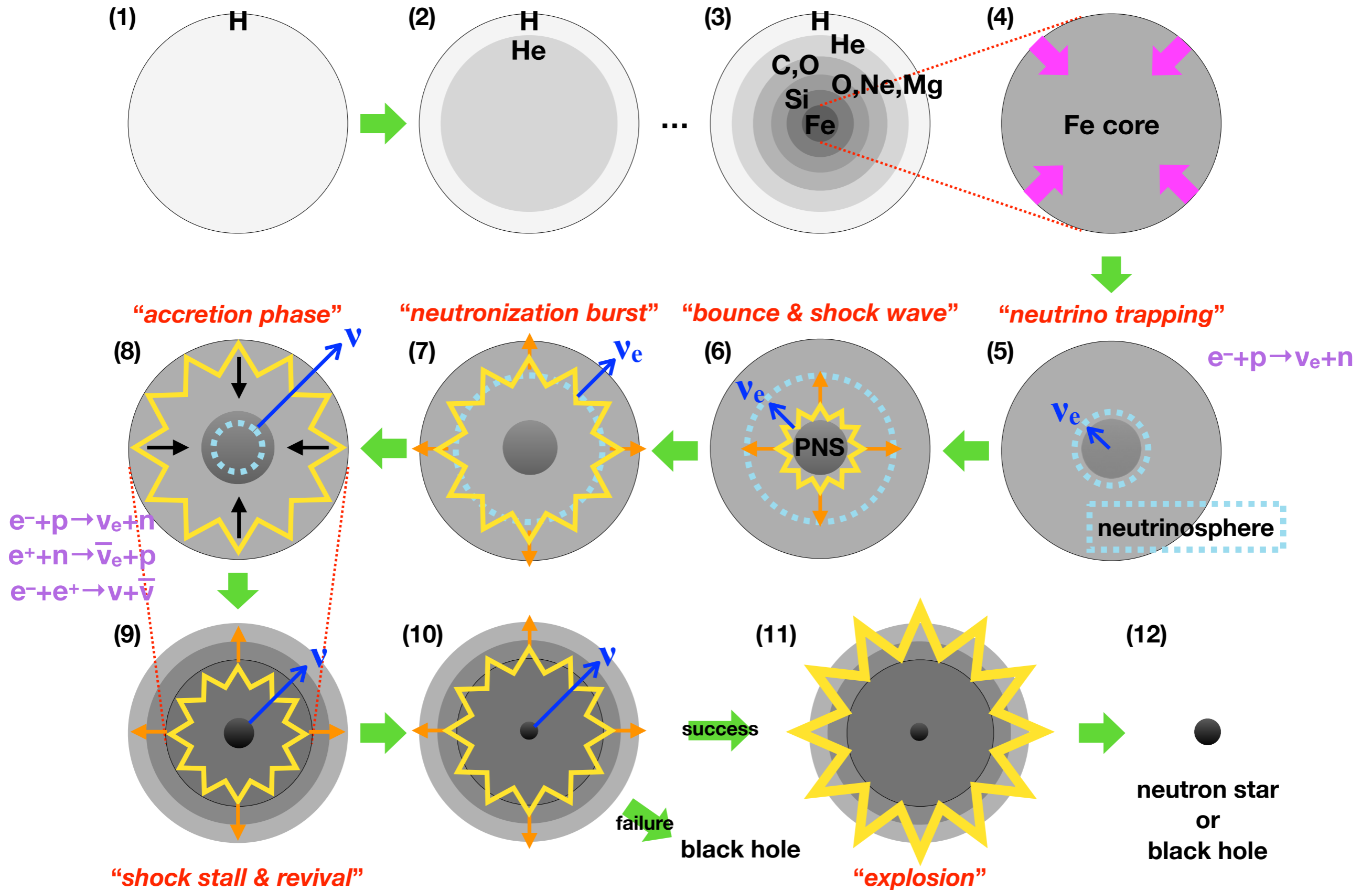


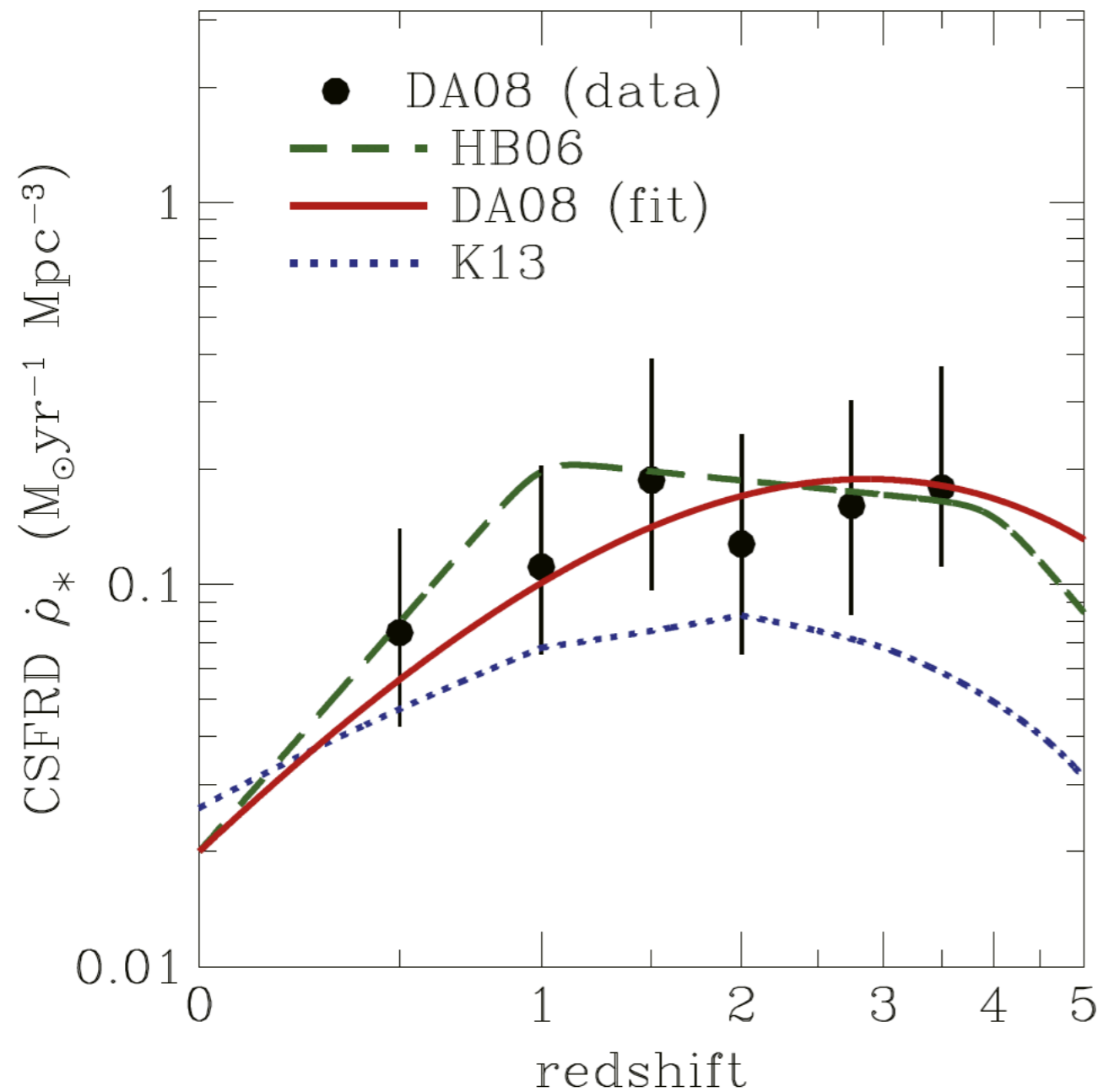
Table 3

SRN Event Rates in Various Ranges of Positron Energy in Super-Kamiokande Over 1 yr (i.e., per 22.5 kton yr) for Models With Metallicity Evolution of DA08+M08

| CSFRD | t_{revive} | EOS for BH | Normal Mass Hierarchy | | | Inverted Mass Hierarchy | | | Figure 12 |
|-------|---------------------|------------|-----------------------|-------|-----------|-------------------------|-------|-----------|-----------|
| | | | 18–26 | 10–18 | 10–26 MeV | 18–26 | 10–18 | 10–26 MeV | |
| HB06 | 100 ms | Shen | 0.286 | 0.704 | 0.990 | 0.375 | 0.832 | 1.207 | ... |
| | | LS | 0.227 | 0.635 | 0.863 | 0.351 | 0.806 | 1.156 | ... |
| | 200 ms | Shen | 0.361 | 0.833 | 1.193 | 0.429 | 0.920 | 1.349 | ... |
| | | LS | 0.302 | 0.764 | 1.066 | 0.404 | 0.893 | 1.297 | ... |
| | 300 ms | Shen | 0.432 | 0.938 | 1.370 | 0.463 | 0.967 | 1.431 | Maximum |
| | | LS | 0.374 | 0.869 | 1.242 | 0.439 | 0.941 | 1.379 | ... |
| DA08 | 100 ms | Shen | 0.219 | 0.515 | 0.734 | 0.286 | 0.598 | 0.885 | ... |
| | | LS | 0.178 | 0.464 | 0.642 | 0.269 | 0.578 | 0.847 | ... |
| | 200 ms | Shen | 0.274 | 0.604 | 0.879 | 0.326 | 0.660 | 0.986 | Reference |
| | | LS | 0.233 | 0.554 | 0.787 | 0.308 | 0.640 | 0.948 | ... |
| | 300 ms | Shen | 0.326 | 0.677 | 1.003 | 0.350 | 0.694 | 1.044 | ... |
| | | LS | 0.285 | 0.627 | 0.911 | 0.333 | 0.674 | 1.007 | ... |
| K13 | 100 ms | Shen | 0.203 | 0.443 | 0.645 | 0.264 | 0.505 | 0.769 | ... |
| | | LS | 0.171 | 0.410 | 0.581 | 0.252 | 0.492 | 0.744 | Minimum |
| | 200 ms | Shen | 0.252 | 0.514 | 0.767 | 0.298 | 0.554 | 0.853 | ... |
| | | LS | 0.221 | 0.482 | 0.703 | 0.286 | 0.542 | 0.827 | ... |
| | 300 ms | Shen | 0.298 | 0.570 | 0.868 | 0.319 | 0.580 | 0.899 | ... |
| | ... | LS | 0.266 | 0.537 | 0.804 | 0.306 | 0.568 | 0.874 | ... |

Table 1.1: Best-fit values of the neutrino oscillation parameters from PDG2018 [22]. NH and IH represent the normal and inverted neutrino mass hierarchy, respectively.

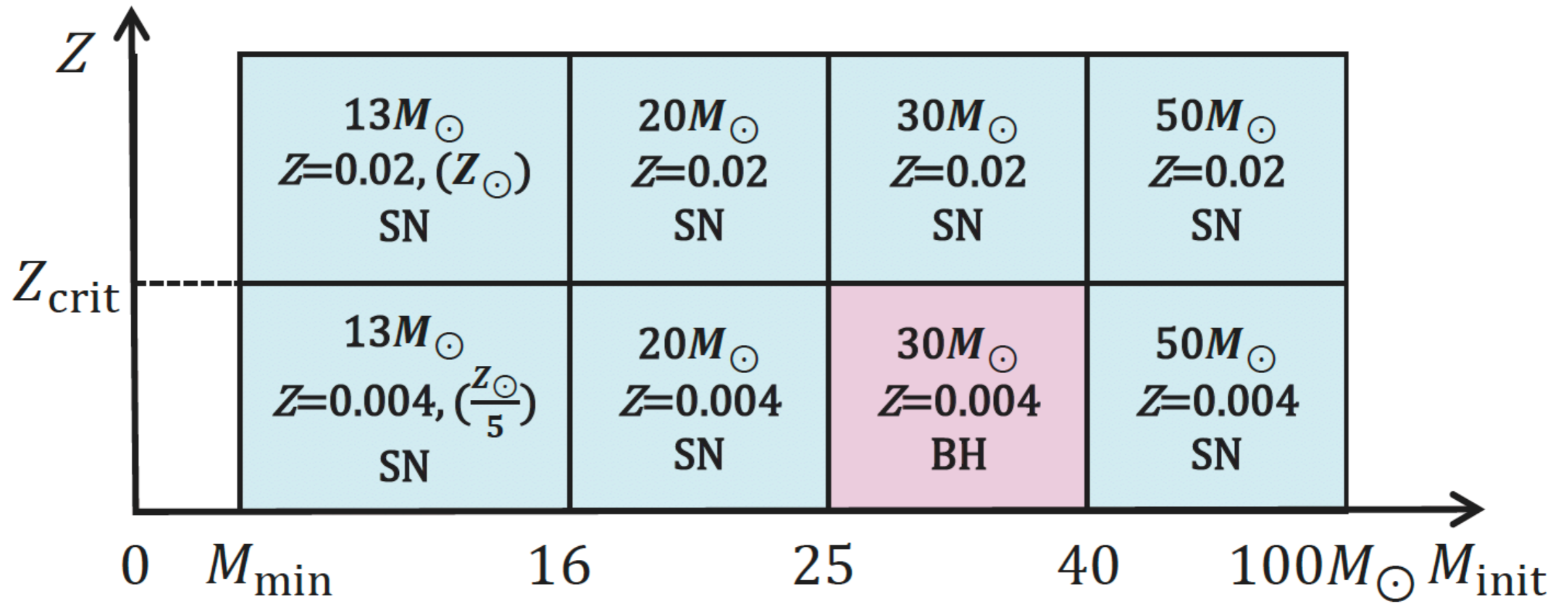
| Oscillation parameter | Best-fit value |
|--------------------------------------|--|
| $\sin^2 \theta_{12}$ | 0.307 ± 0.013 |
| $\sin^2 \theta_{23}$ (NH, Octant I) | $0.417^{+0.025}_{-0.028}$ |
| $\sin^2 \theta_{23}$ (NH, Octant II) | $0.597^{+0.024}_{-0.030}$ |
| $\sin^2 \theta_{23}$ (IH, Octant I) | $0.421^{+0.033}_{-0.025}$ |
| $\sin^2 \theta_{23}$ (IH, Octant II) | $0.592^{+0.023}_{-0.030}$ |
| $\sin^2 \theta_{13}$ | $(2.12 \pm 0.08) \times 10^{-2}$ |
| Δm_{12}^2 | $(7.53 \pm 0.18) \times 10^{-5} \text{ eV}^2$ |
| Δm_{32}^2 (NH) | $(2.51 \pm 0.05) \times 10^{-3} \text{ eV}^2$ |
| Δm_{32}^2 (IH) | $(-2.56 \pm 0.04) \times 10^{-3} \text{ eV}^2$ |




$$R_{\text{CCSN}}(z) = \zeta_{\text{CCSN}} \dot{\rho}_*(z),$$


$$\zeta_{\text{CCSN}} = \frac{\int_{M_{\min}}^{M_{\max}} \Psi_{\text{IMF}}(M) dM}{\int_{0.1 M_{\text{sun}}}^{100 M_{\text{sun}}} M \Psi_{\text{IMF}}(M) dM},$$

Figure 2. CSFRD as a function of redshift. Dashed, solid and dotted lines correspond to the models in HB06, DA08 and K13, respectively. Plots are calculated from the data in Tables 1 and 2 in DA08.



$$\begin{aligned}\frac{dN_{\bar{\nu}_e}}{dE_\nu} &= |U_{e1}|^2 \frac{dN_{\bar{\nu}_1}}{dE_\nu} + |U_{e2}|^2 \frac{dN_{\bar{\nu}_2}}{dE_\nu} + |U_{e3}|^2 \frac{dN_{\bar{\nu}_3}}{dE_\nu} \\ &= \cos^2 \theta_{12} \cos^2 \theta_{13} \frac{dN_{\bar{\nu}_1}}{dE_\nu} + \sin^2 \theta_{12} \cos^2 \theta_{13} \frac{dN_{\bar{\nu}_2}}{dE_\nu} + \sin^2 \theta_{13} \frac{dN_{\bar{\nu}_3}}{dE_\nu} \\ &\sim 0.68 \cdot \frac{dN_{\bar{\nu}_1}}{dE_\nu} + 0.30 \cdot \frac{dN_{\bar{\nu}_2}}{dE_\nu} + 0.02 \cdot \frac{dN_{\bar{\nu}_3}}{dE_\nu},\end{aligned}$$

 $\frac{dN_{\bar{\nu}_e}}{dE_\nu} \sim 0.68 \cdot \frac{dN_{\bar{\nu}_e}^0}{dE_\nu} + 0.32 \cdot \frac{dN_{\bar{\nu}_x}^0}{dE_\nu}$ **Normal Hierarchy**

 $\frac{dN_{\bar{\nu}_e}}{dE_\nu} \sim \frac{dN_{\bar{\nu}_x}^0}{dE_\nu}$ **Inverted Hierarchy**

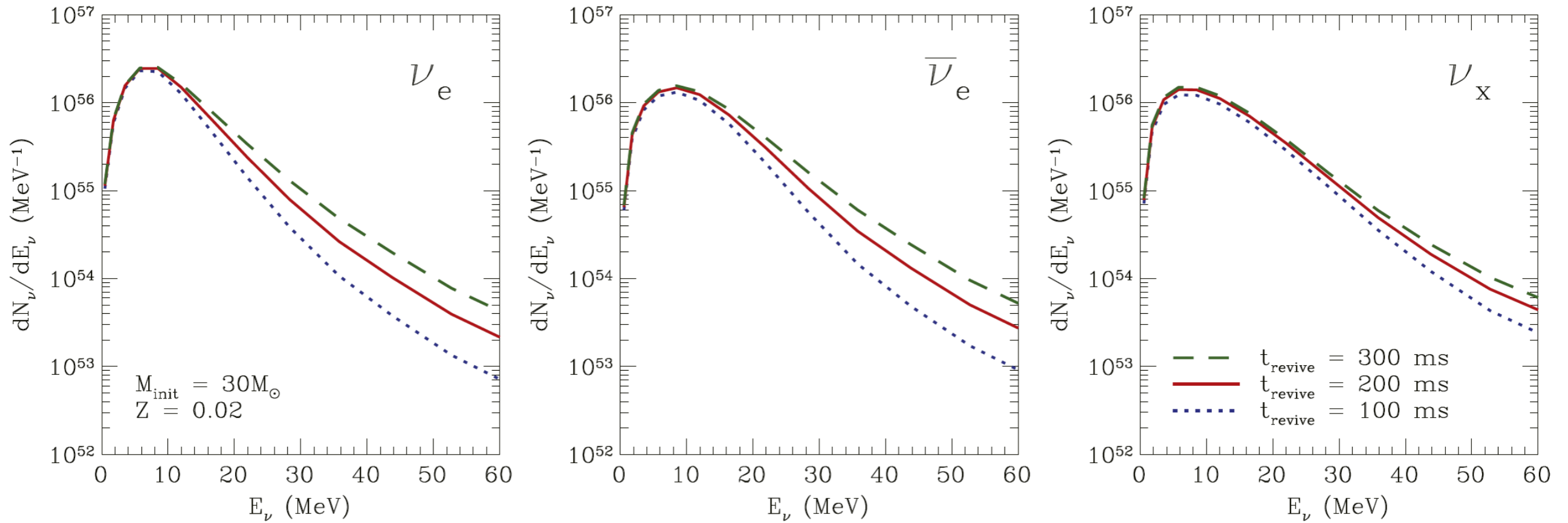


Figure 4. Neutrino number spectra of supernova with $30M_\odot$, $Z = 0.02$ and shock revival times of $t_{\text{revive}} = 100$ ms (dotted), 200 ms (solid), and 300 ms (dashed). The left, central, and right panels correspond to ν_e , $\bar{\nu}_e$, and ν_x ($=\nu_\mu = \bar{\nu}_\mu = \nu_\tau = \bar{\nu}_\tau$), respectively.

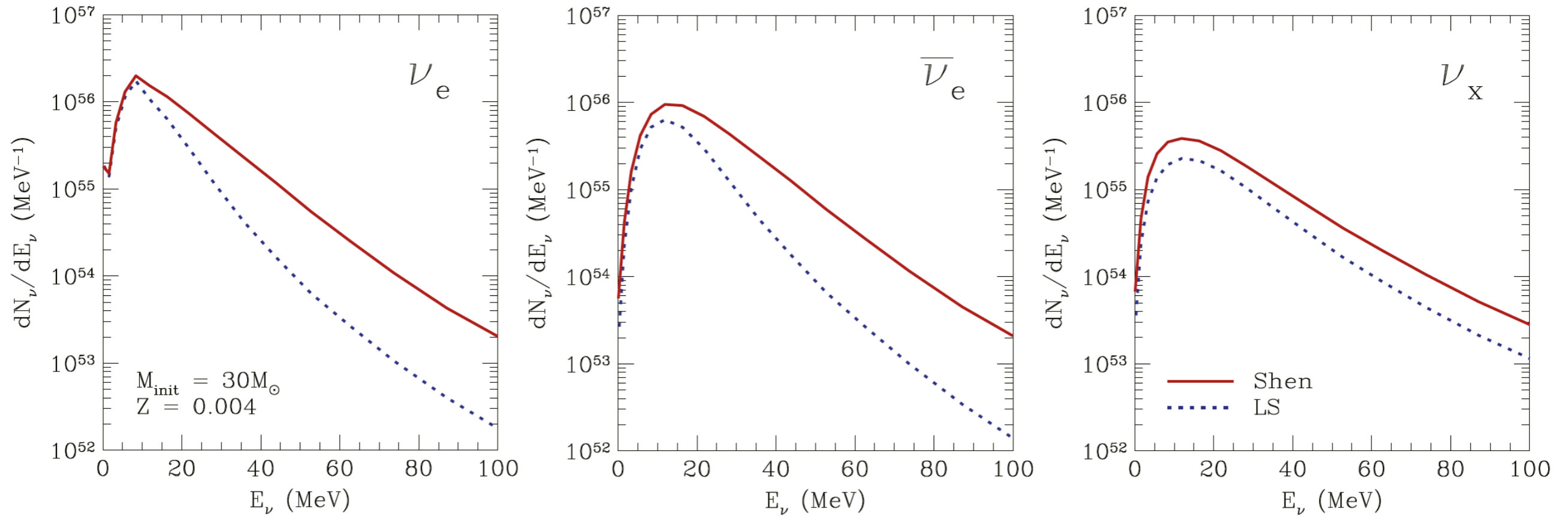


Figure 6. Neutrino number spectra for black hole formation with $30M_\odot$, $Z = 0.004$ and Shen EOS (solid) and LS EOS (dotted). The left, central, and right panels correspond to ν_e , $\bar{\nu}_e$, and ν_x ($=\nu_\mu = \bar{\nu}_\mu = \nu_\tau = \bar{\nu}_\tau$), respectively.

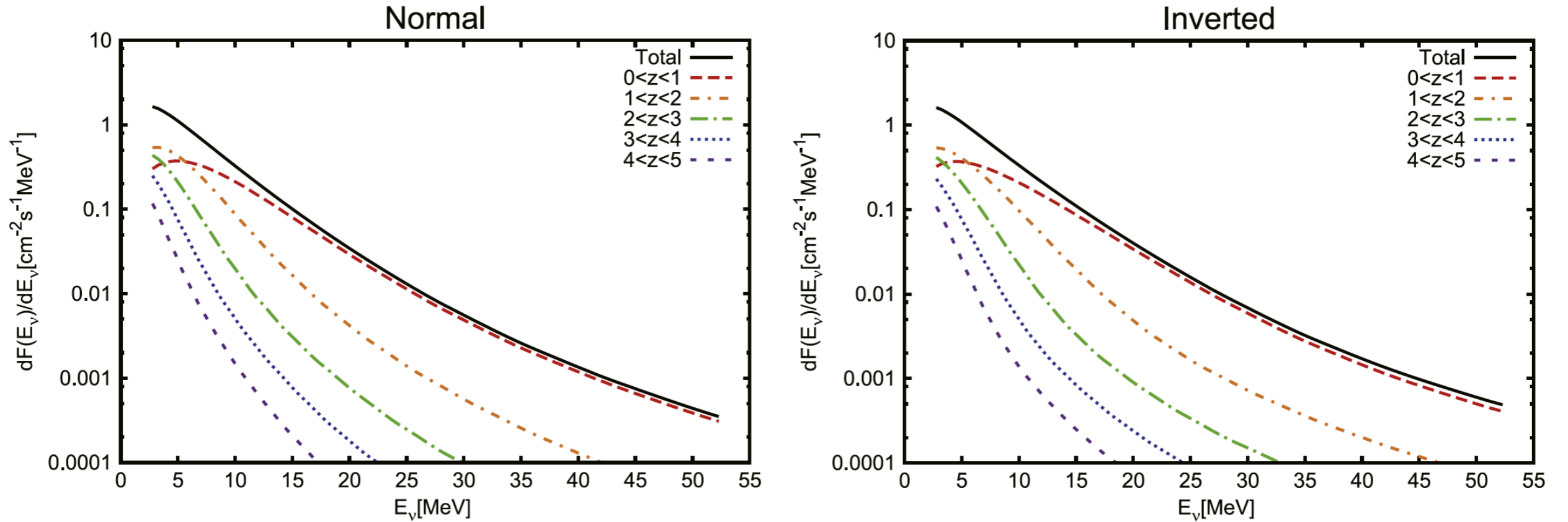
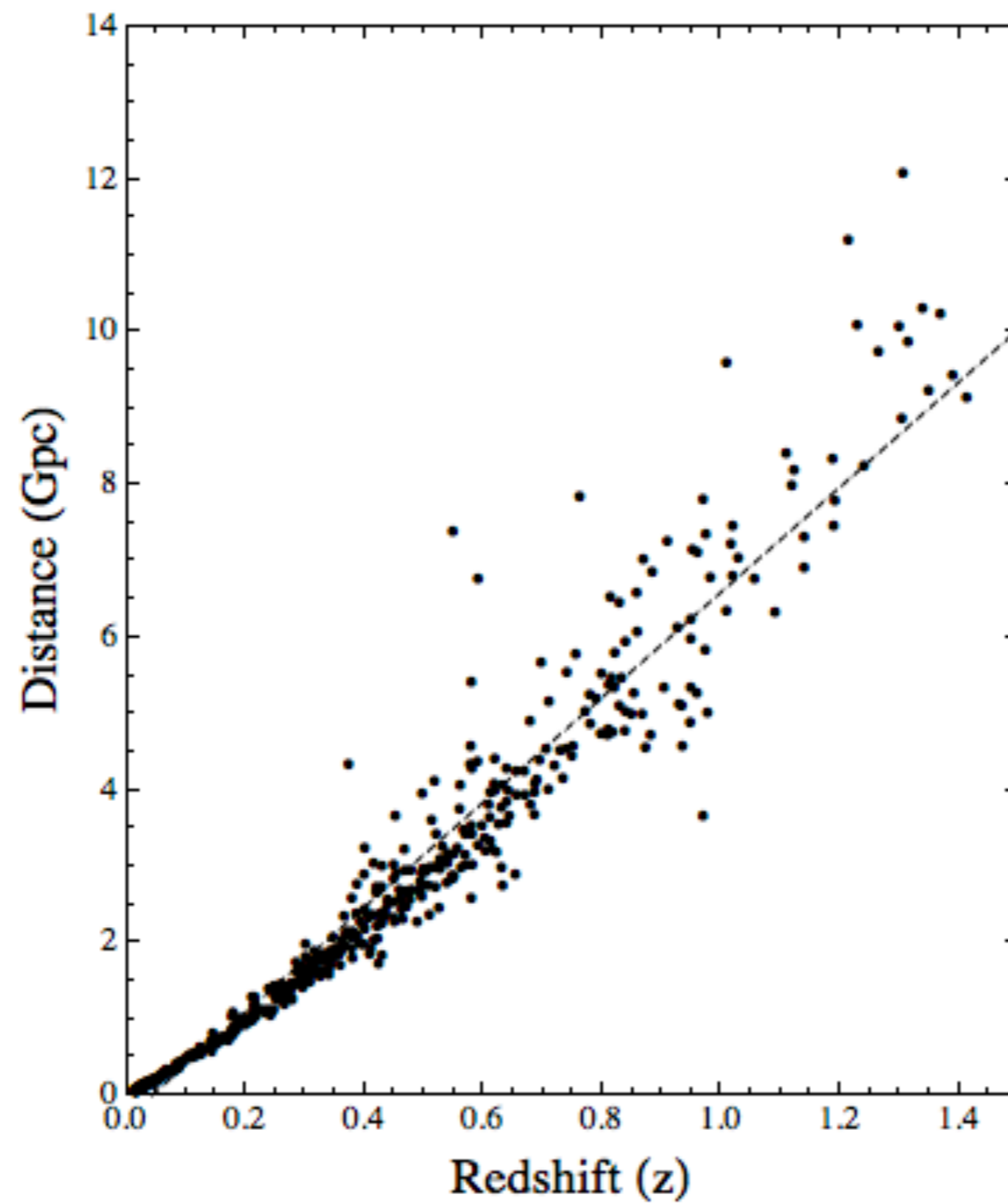


Figure 10. Total fluxes of SRNs (solid) and contributions from various redshift ranges for the reference model. The lines except for the solid line correspond, from top to bottom, to the redshift ranges $0 < z < 1$, $1 < z < 2$, $2 < z < 3$, $3 < z < 4$, and $4 < z < 5$, for $E_\nu > 10$ MeV. The left and right panels show the cases for normal and inverted mass hierarchies, respectively.

1 pc ~ 3.26 light-year

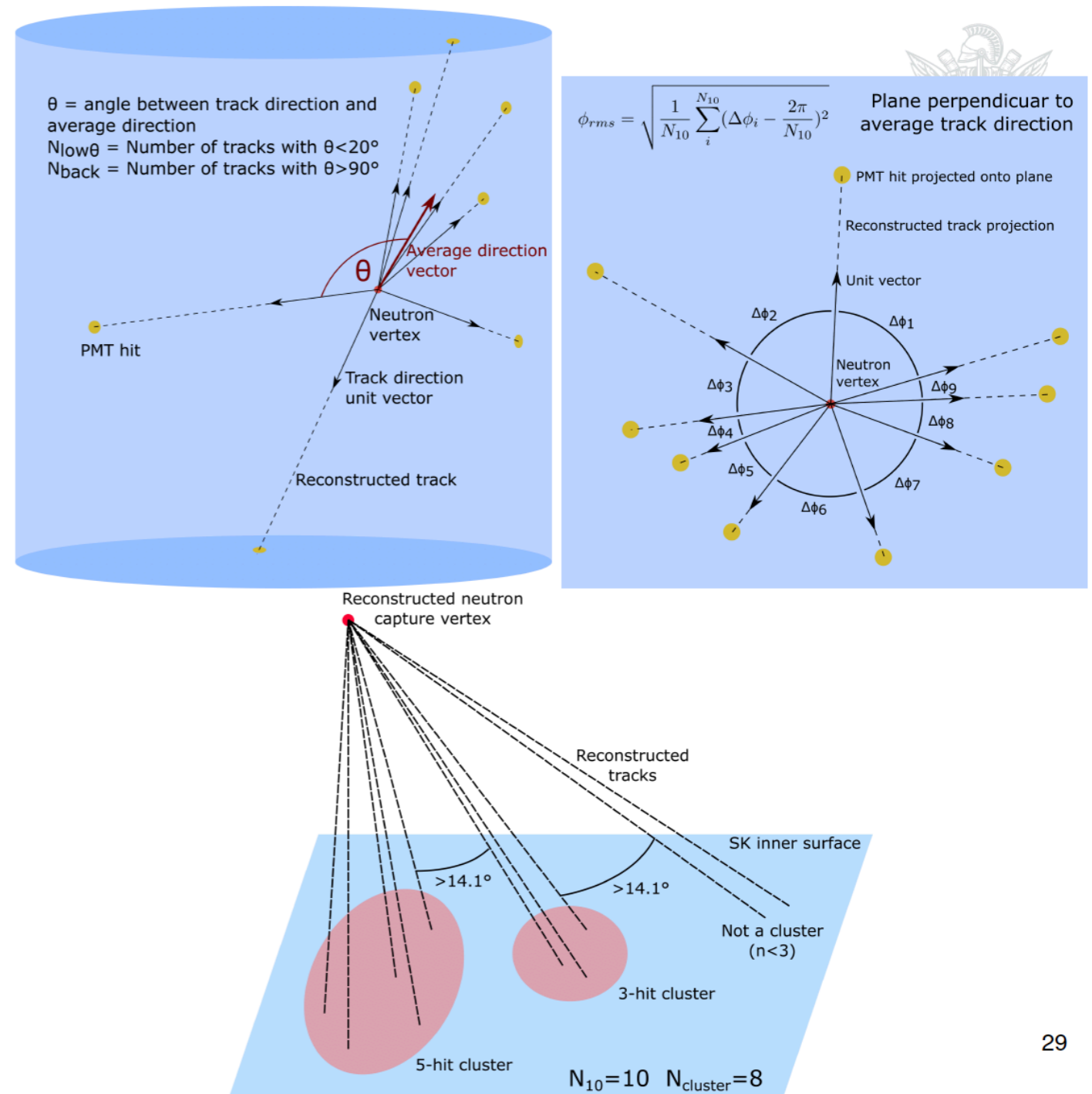


SK Operation Periods

| Phase | SK-I | SK-II | SK-III | SK-IV | SK-V |
|-------------------|------------|------------|------------|------------|------------|
| Start | Apr., 1996 | Oct., 2002 | Jul., 2006 | Sep., 2008 | Jan., 2019 |
| End | Jul., 2001 | Oct., 2005 | Aug., 2008 | May., 2018 | (running) |
| Live time [days] | 1496 | 791 | 548 | 2970 | - |
| Number of ID PMTs | 11,146 | 5,182 | 11,129 | 11,129 | 11,129 |
| ID PMT coverage | 40% | 19% | 40% | 40% | 40% |
| Number of OD PMTs | 1,885 | 1,885 | 1,885 | 1,885 | 1,885 |
| PMT protection | No | Yes | Yes | Yes | Yes |
| Neutron tagging | No | No | No | Yes | Yes |
| Threshold [MeV] | 4.5 | 6.5 | 4.0 | 3.5 | 3.5 |

DISCRIMINATING VARIABLES (1)

- N_{10} : number of PMT hits in 10 ns window
- Geometrical variables
 - $\theta_{mean}, \theta_{rms}$
 - ϕ_{rms}
 - N_{low}
 - $N_{cluster}$
 - $N_{low\theta}$
 - N_{back}
- PMT noise variables
 - N_{300}
 - N_{highQ}
 - Q_{mean}, Q_{rms}
 - $T_{rms}, \min T_{rms}(3), \min T_{rms}(6)$



DISCRIMINATING VARIABLES (2)



Additional variables to refine the zeroth-order vertex:

- Neut-Fit variables

- NF_{wall}
- δN_{10}
- δT_{rms}

- BONSAI vertex fit Variables

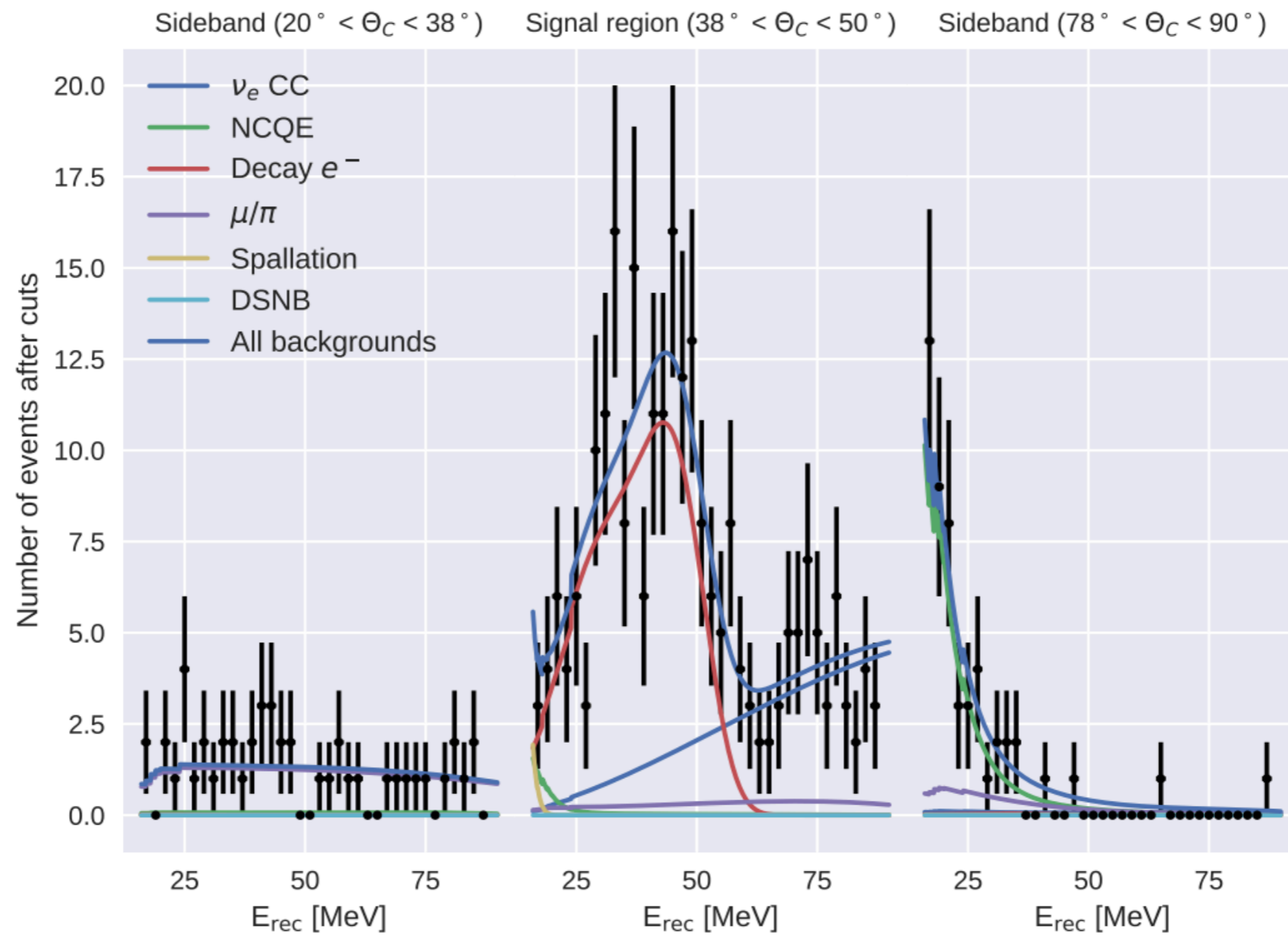
- BS_{wall}
- BS_{energy}

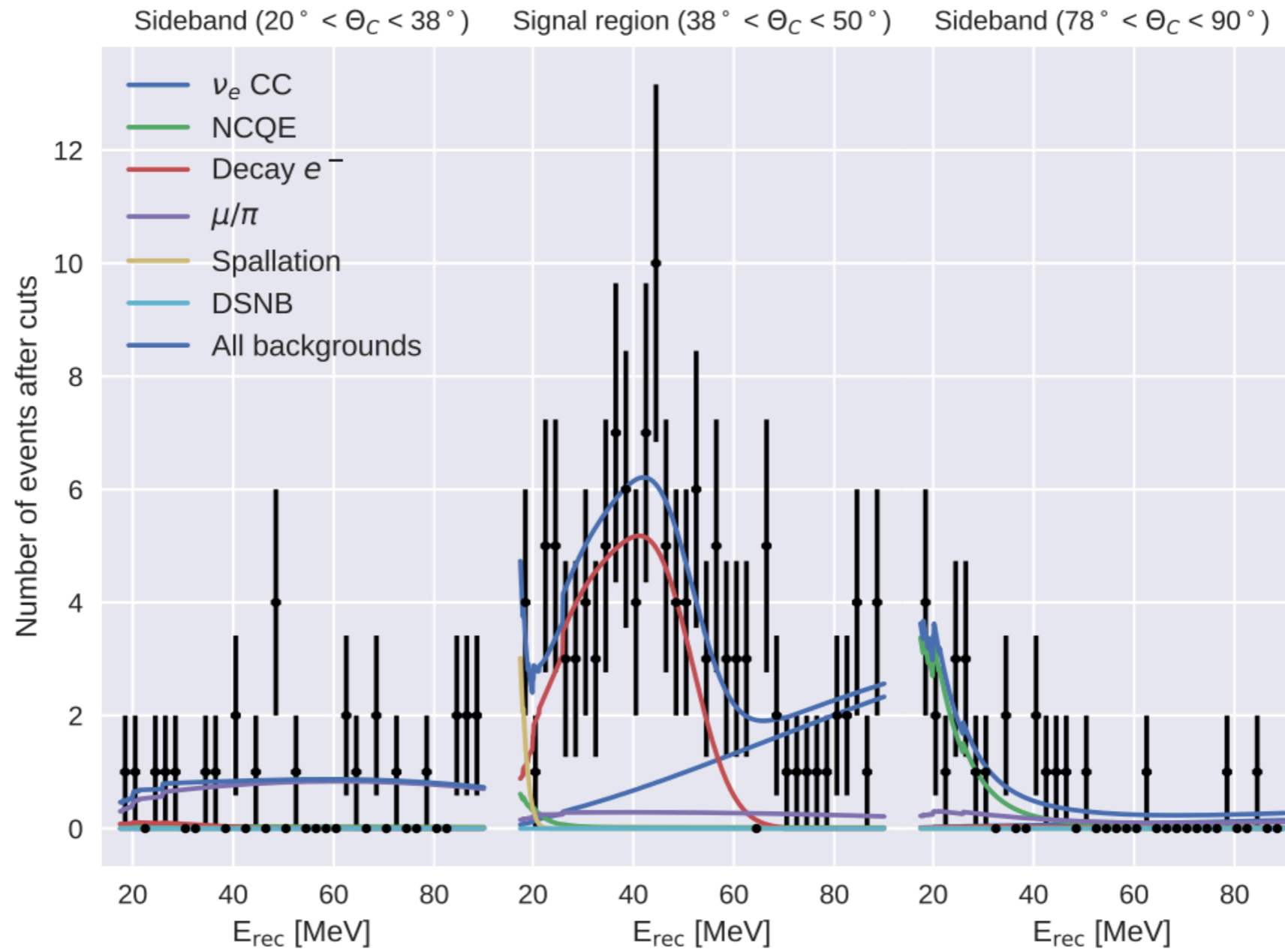
- Fit agreement variables

- BF_{dist}
- FP_{dist}

- Combined-fit variables

- $\mathcal{L}_{ratio} = \frac{\mathcal{L}_{combined}}{\mathcal{L}_{prompt} \times \mathcal{L}_{neutron}}$
- \mathcal{L}_{window}





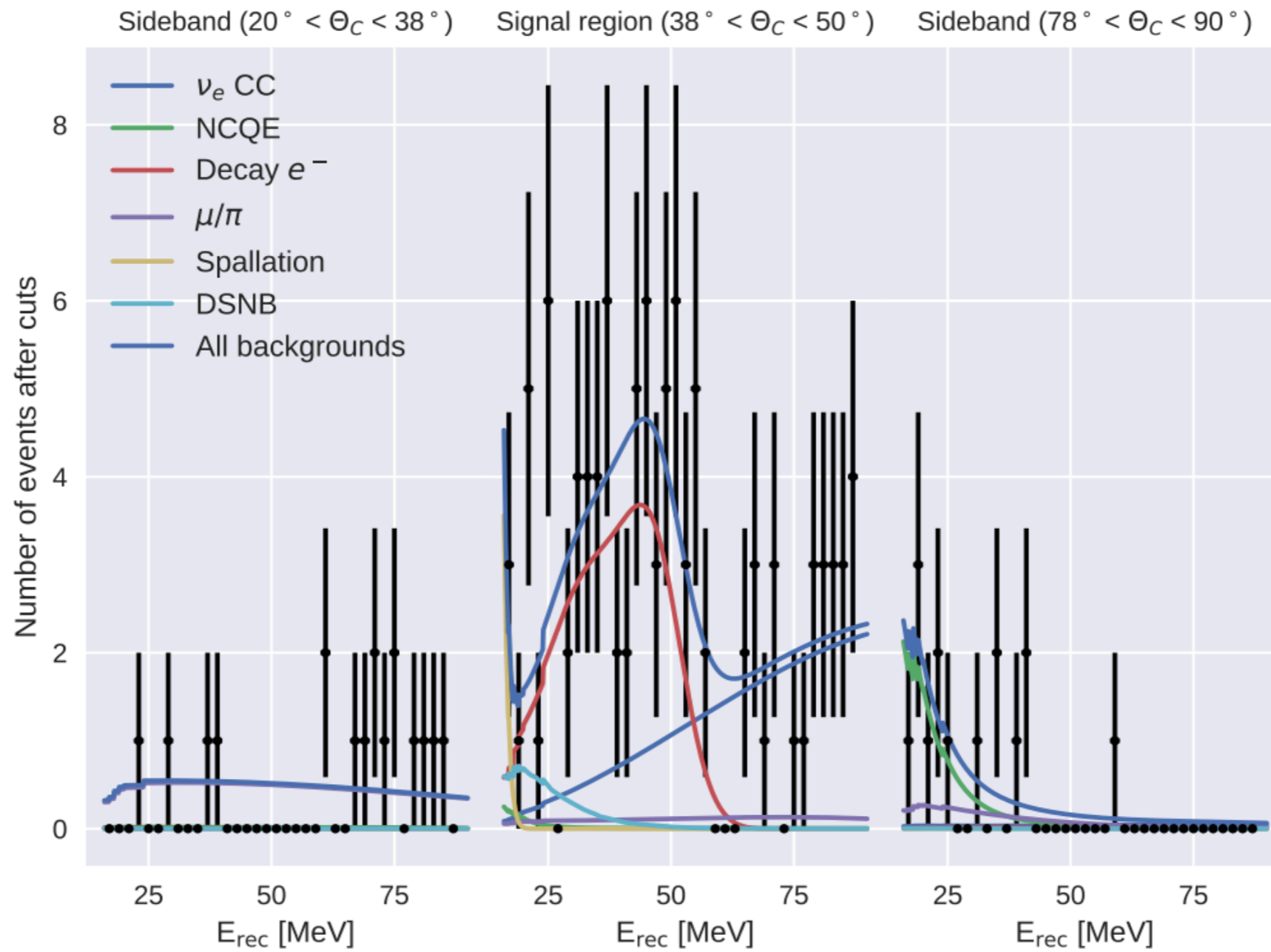


TABLE VIII. Best-fit values and the 90% C.L. upper limits on the DSNB fluxes (in $\text{cm}^{-2}\cdot\text{sec}^{-1}$) for the theoretical models for phases SK-I to IV as well as for the combined analysis. Here the upper limits are given for $E_\nu > 17.3$ MeV.

| Model | Best fit | | 90% CL limit | | | | | Pred. |
|-------------------------------|---------------------|---------------------|--------------|-----|-----|-----|-----|-------|
| | SK4 | All | SK1 | SK2 | SK3 | SK4 | All | |
| Totani+95 Constant | $2.5^{+1.4}_{-1.3}$ | $1.3^{+0.9}_{-0.9}$ | 2.3 | 6.3 | 7.0 | 4.5 | 2.6 | 4.67 |
| Kaplinghat+00 HMA (max) | $2.6^{+1.5}_{-1.3}$ | $1.3^{+0.9}_{-0.9}$ | 2.3 | 6.7 | 7.1 | 4.7 | 2.6 | 3.00 |
| Horiuchi+09 6 MeV, max | $2.6^{+1.4}_{-1.3}$ | $1.3^{+0.9}_{-0.9}$ | 2.4 | 6.0 | 7.0 | 4.6 | 2.6 | 1.94 |
| Ando+03 (updated 05) | $2.7^{+1.5}_{-1.4}$ | $1.4^{+0.9}_{-0.9}$ | 2.3 | 6.6 | 7.2 | 4.7 | 2.7 | 1.74 |
| Kresse+21 (High, NH) | $2.7^{+1.5}_{-1.3}$ | $1.4^{+0.9}_{-0.9}$ | 2.3 | 6.7 | 7.2 | 4.7 | 2.7 | 1.57 |
| Galais+09 (NH) | $2.5^{+1.4}_{-1.3}$ | $1.3^{+0.9}_{-0.9}$ | 2.3 | 6.3 | 7.0 | 4.5 | 2.6 | 1.56 |
| Galais+09 (IH) | $2.6^{+1.4}_{-1.3}$ | $1.3^{+0.9}_{-0.9}$ | 2.3 | 6.4 | 7.0 | 4.5 | 2.6 | 1.50 |
| Horiuchi+18 $\xi_{2.5} = 0.1$ | $2.6^{+1.4}_{-1.3}$ | $1.4^{+0.9}_{-0.9}$ | 2.4 | 6.1 | 7.1 | 4.6 | 2.7 | 1.23 |
| Kresse+21 (High, IH) | $2.7^{+1.5}_{-1.3}$ | $1.4^{+0.9}_{-0.9}$ | 2.3 | 6.7 | 7.1 | 4.7 | 2.7 | 1.21 |
| Kresse+21 (Fid, NH) | $2.7^{+1.5}_{-1.3}$ | $1.4^{+0.9}_{-0.9}$ | 2.3 | 6.8 | 7.2 | 4.7 | 2.7 | 1.20 |
| Kresse+21 (Fid, IH) | $2.7^{+1.5}_{-1.3}$ | $1.4^{+0.9}_{-0.9}$ | 2.3 | 6.8 | 7.2 | 4.7 | 2.7 | 1.02 |
| Kresse+21 (Low, NH) | $2.7^{+1.5}_{-1.4}$ | $1.4^{+0.9}_{-0.9}$ | 2.3 | 6.8 | 7.2 | 4.8 | 2.7 | 0.96 |
| Tabrizi+21 (NH) | $2.7^{+1.5}_{-1.3}$ | $1.4^{+0.9}_{-0.9}$ | 2.4 | 6.6 | 7.1 | 4.7 | 2.7 | 0.92 |
| Kresse+21 (Low, IH) | $2.7^{+1.5}_{-1.4}$ | $1.4^{+0.9}_{-0.9}$ | 2.3 | 6.8 | 7.2 | 4.8 | 2.7 | 0.84 |
| Lunardini09 Failed SN | $2.8^{+1.5}_{-1.4}$ | $1.4^{+0.9}_{-0.9}$ | 2.4 | 6.8 | 7.3 | 4.8 | 2.8 | 0.73 |
| Hartmann+97 CE | $2.6^{+1.4}_{-1.3}$ | $1.3^{+0.9}_{-0.9}$ | 2.3 | 6.5 | 7.1 | 4.6 | 2.6 | 0.63 |
| Nakazato+15 (max, IH) | $2.7^{+1.5}_{-1.4}$ | $1.4^{+1.0}_{-0.9}$ | 2.4 | 6.5 | 7.2 | 4.8 | 2.7 | 0.53 |
| Horiuchi+18 $\xi_{2.5} = 0.5$ | $2.7^{+1.5}_{-1.4}$ | $1.3^{+0.9}_{-0.9}$ | 2.2 | 7.1 | 7.1 | 4.8 | 2.6 | 0.55 |
| Horiuchi+21 | $2.1^{+1.3}_{-1.2}$ | $1.2^{+0.9}_{-0.9}$ | 3.4 | 4.3 | 5.9 | 3.9 | 2.5 | 0.28 |
| Malaney97 CGI | $2.7^{+1.5}_{-1.3}$ | $1.3^{+0.9}_{-0.9}$ | 2.3 | 6.8 | 7.1 | 4.7 | 2.6 | 0.26 |
| Nakazato+15 (min, NH) | $2.8^{+1.5}_{-1.4}$ | $1.4^{+1.0}_{-0.9}$ | 2.3 | 6.8 | 7.2 | 4.8 | 2.7 | 0.19 |